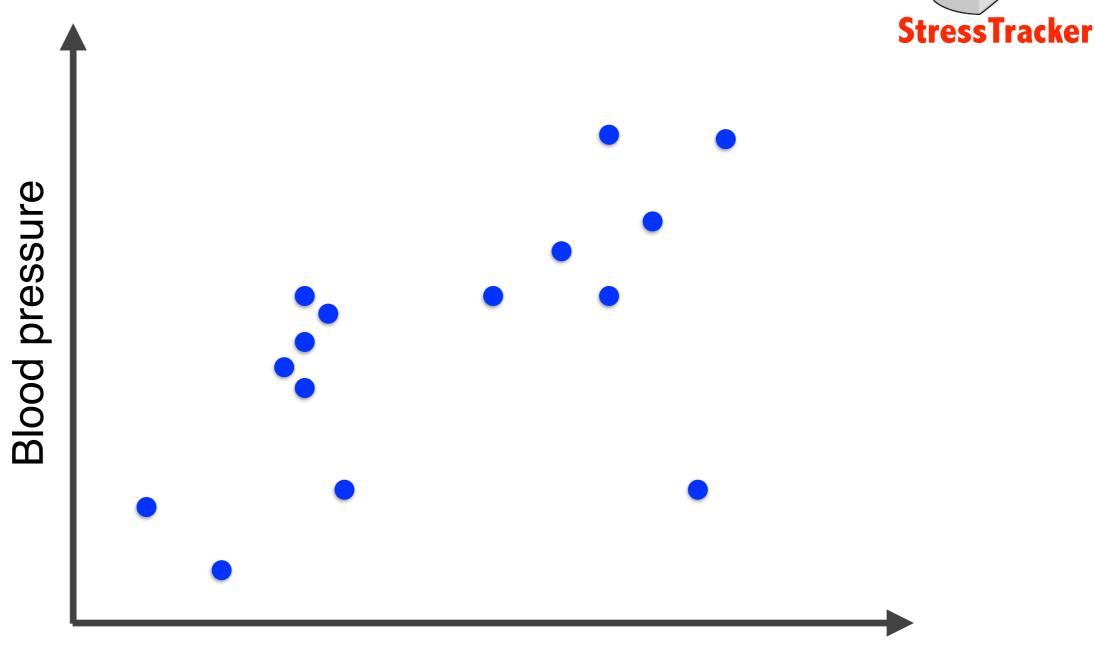
Prio: Private, Robust, and Efficient Computation of Aggregate Statistics

Henry Corrigan-Gibbs and Dan Boneh Stanford University

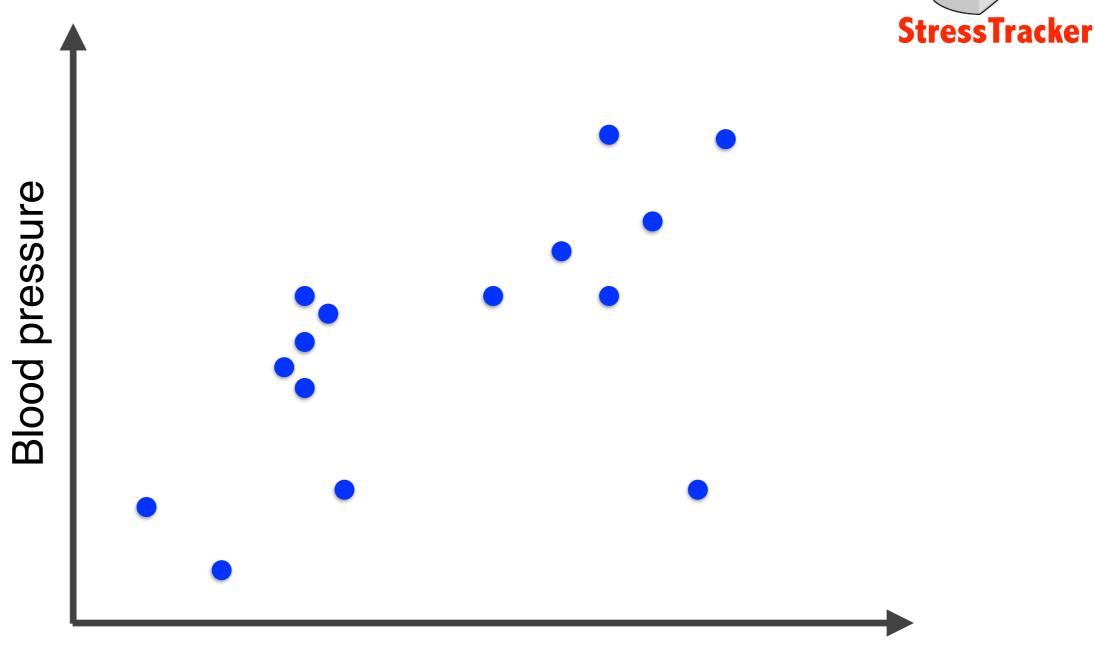
Appeared at NSDI 2017

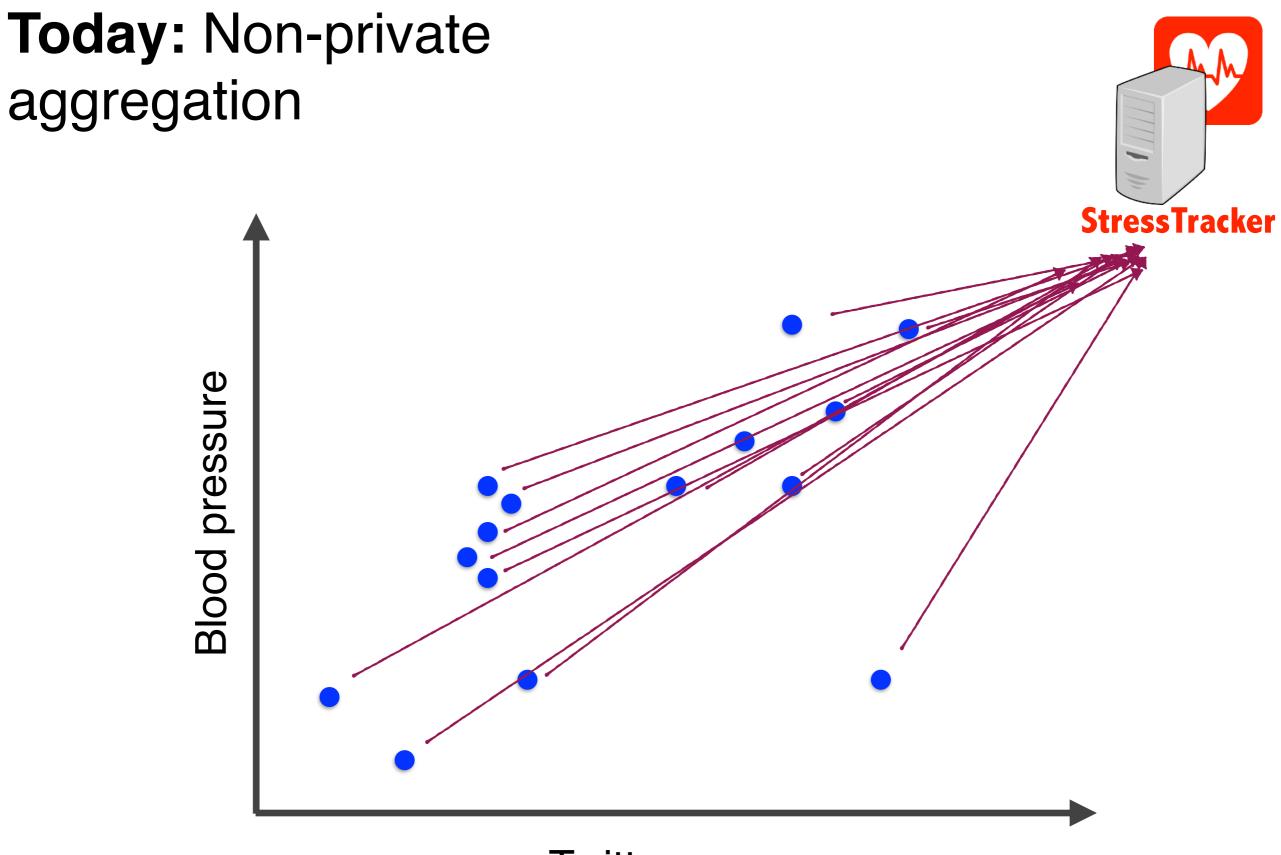
Today: Non-private aggregation

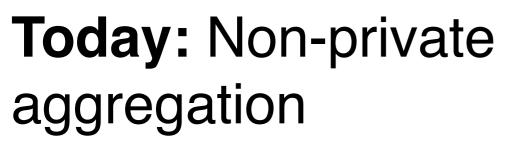


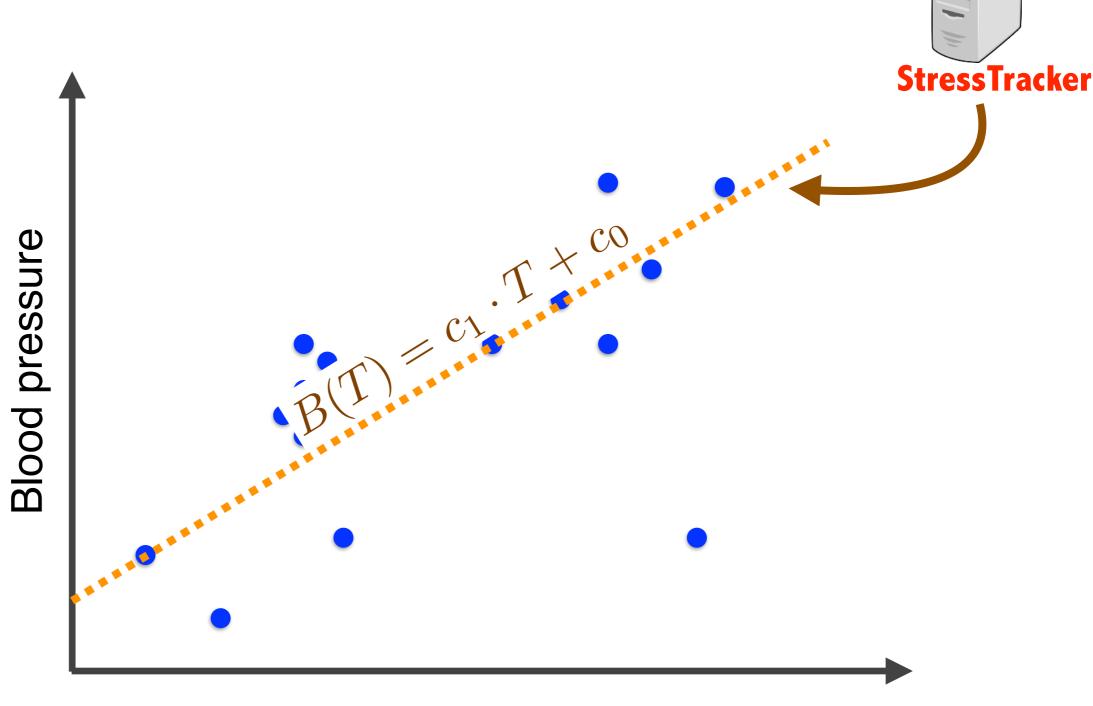
Today: Non-private aggregation **StressTracker** Blood pressure Each user has a private data point

Today: Non-private aggregation

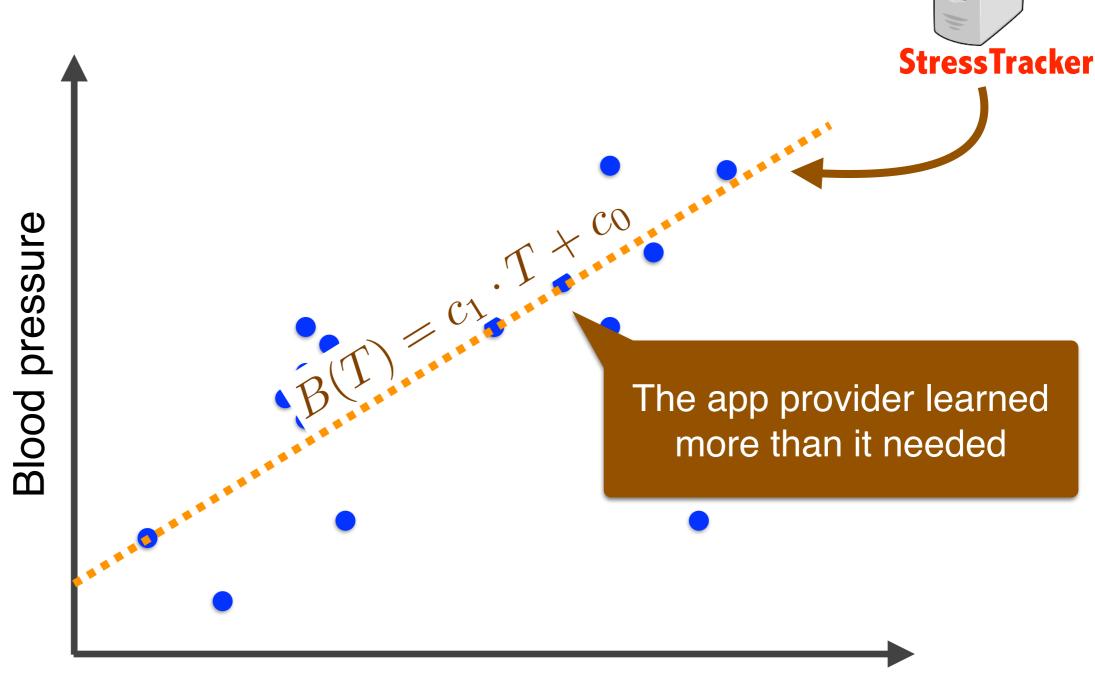




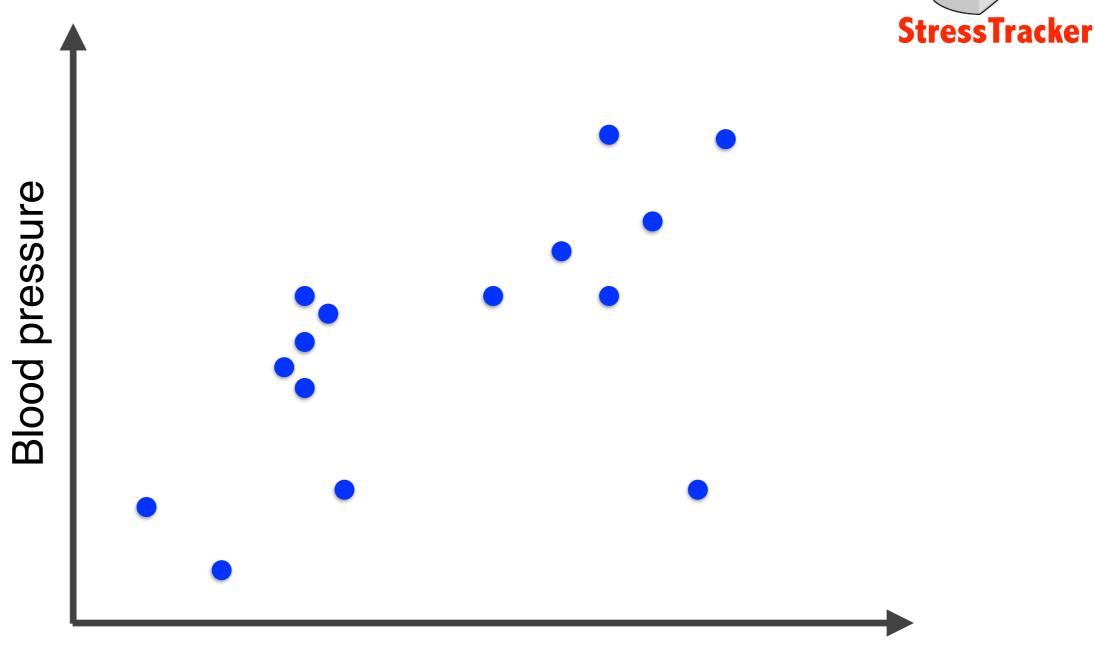


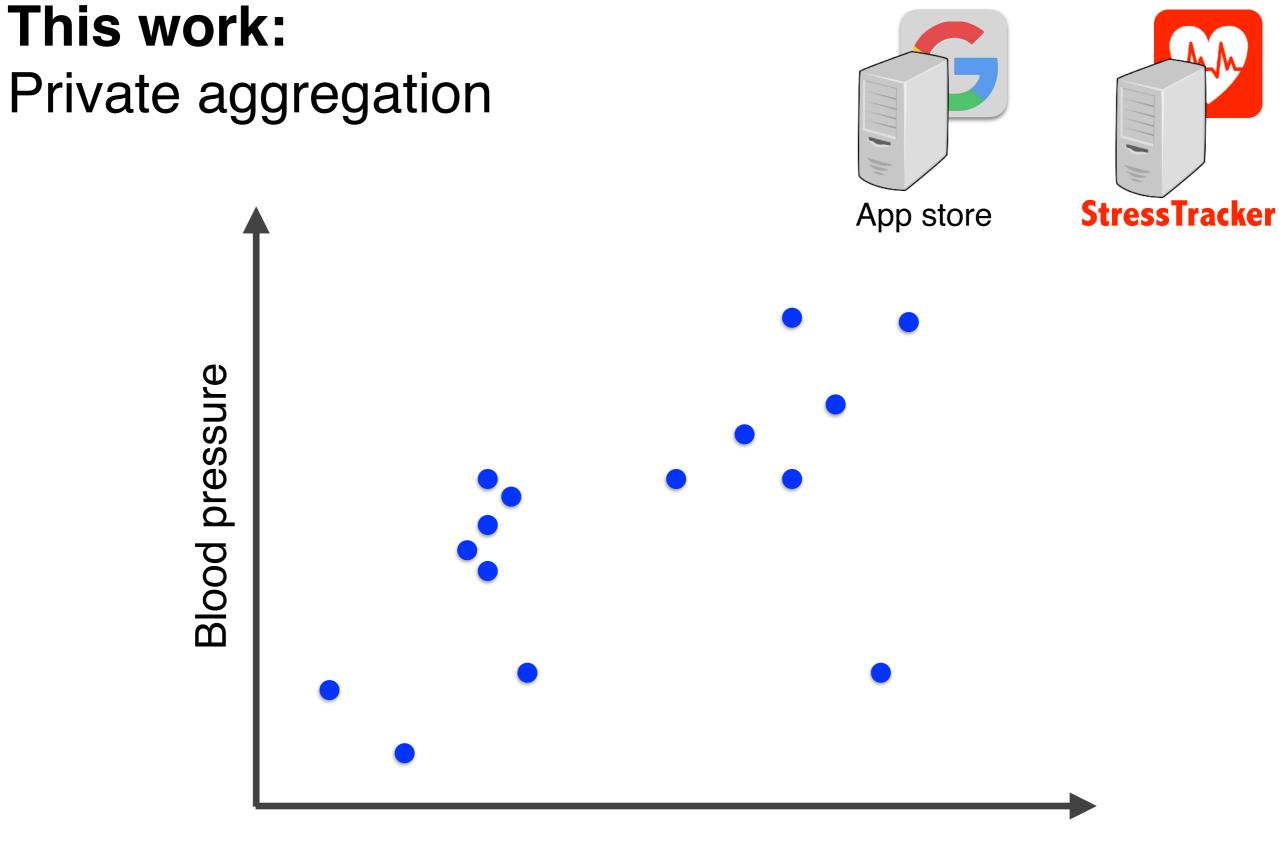


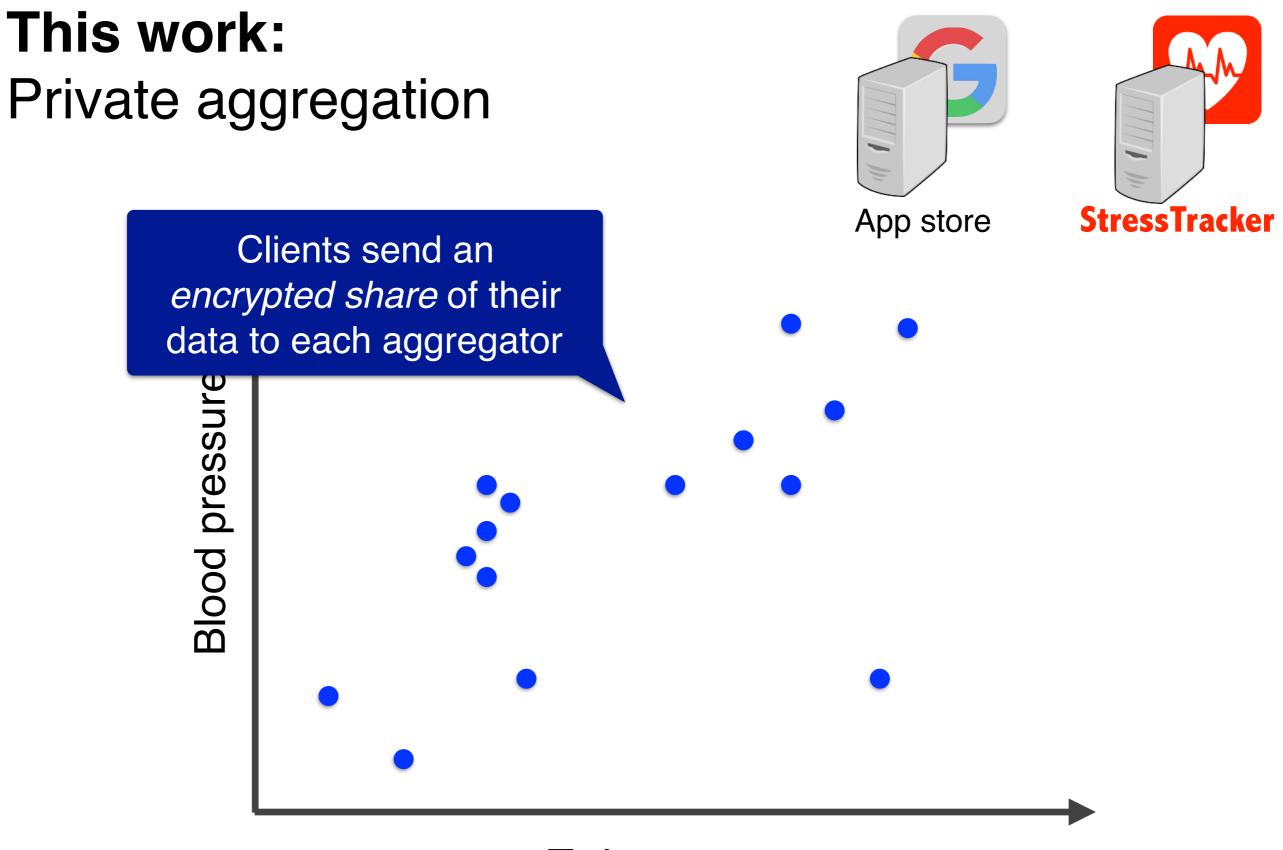
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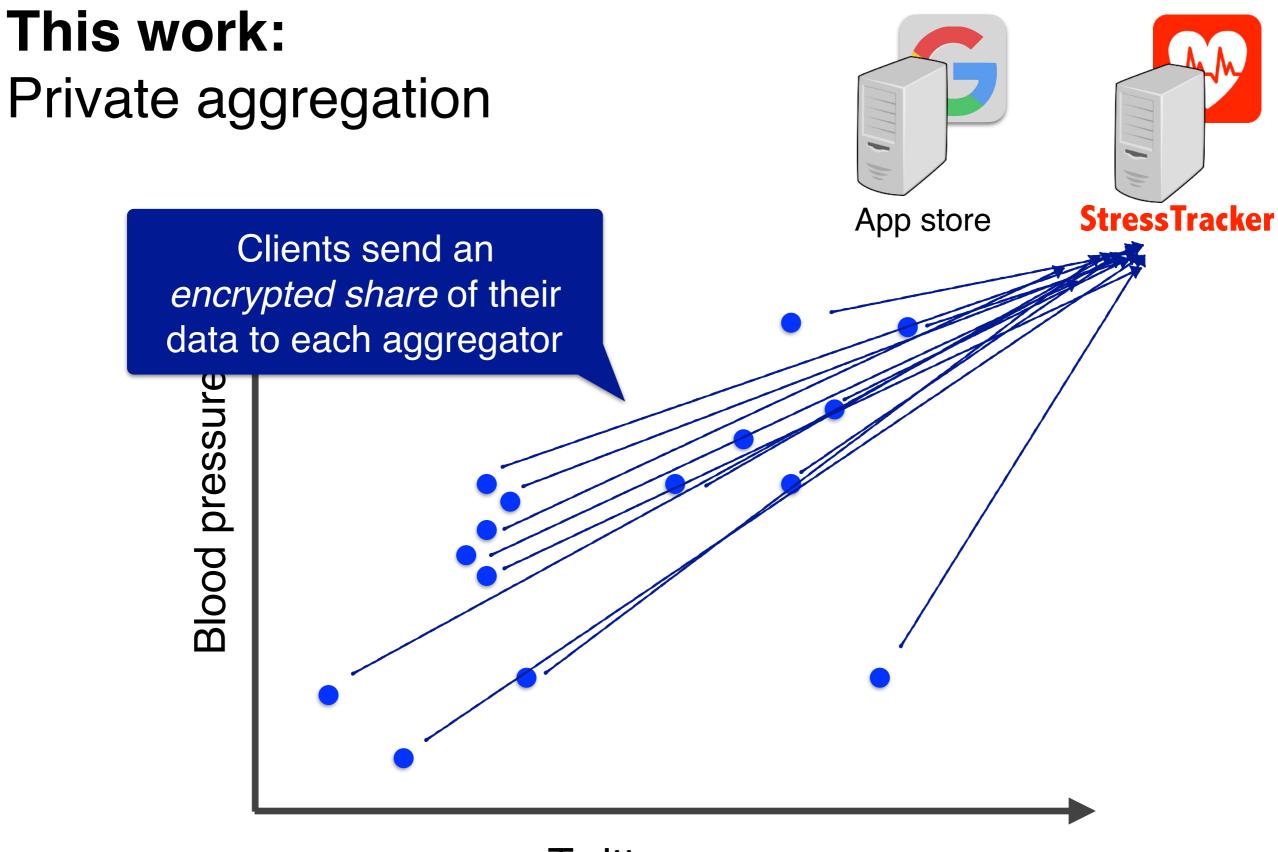


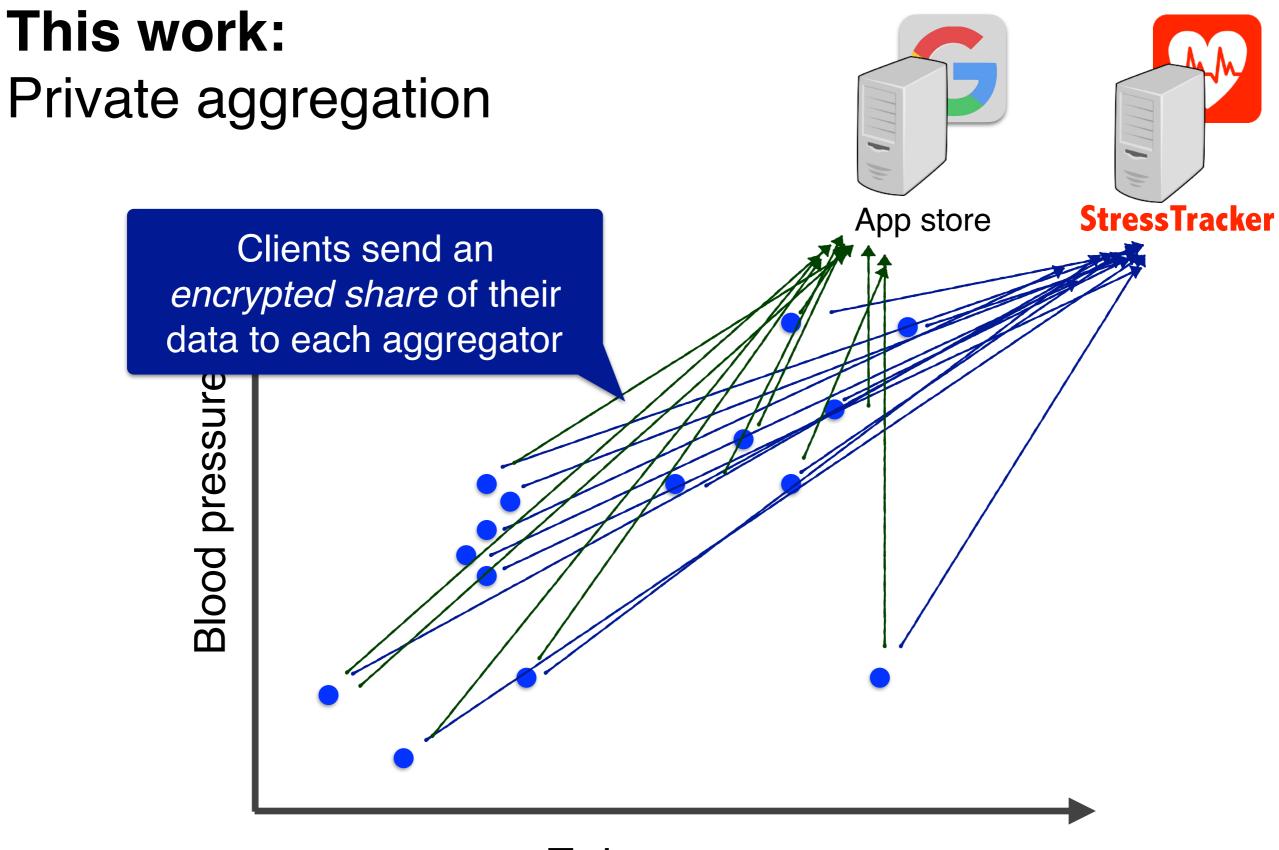
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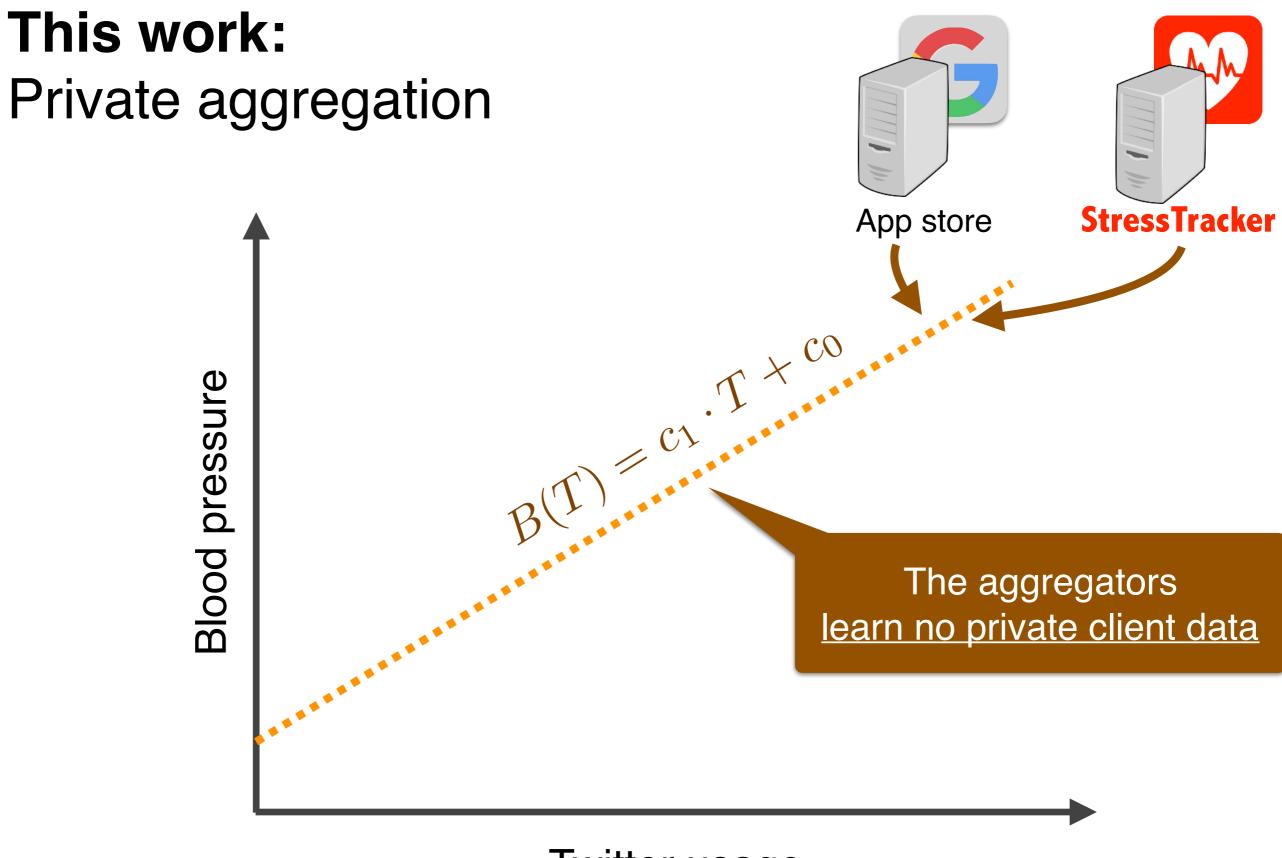






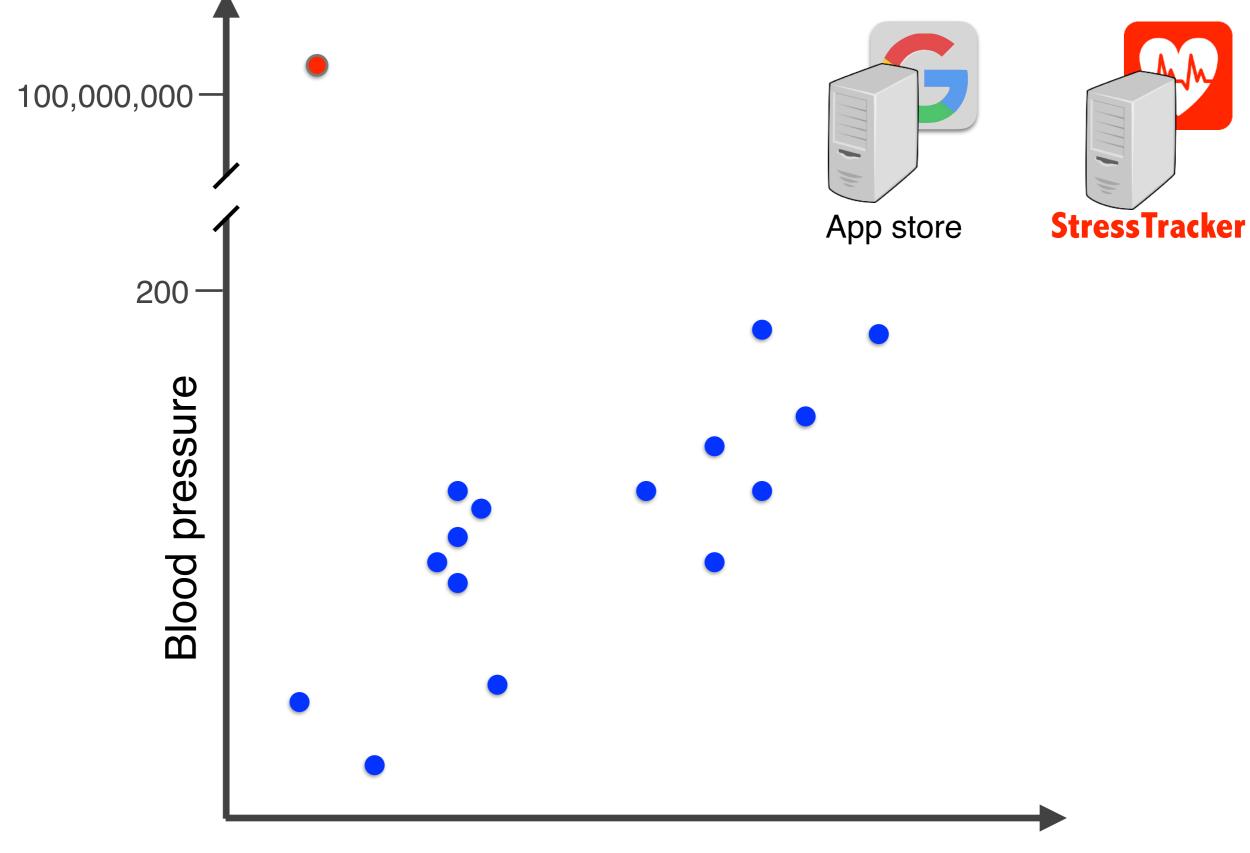


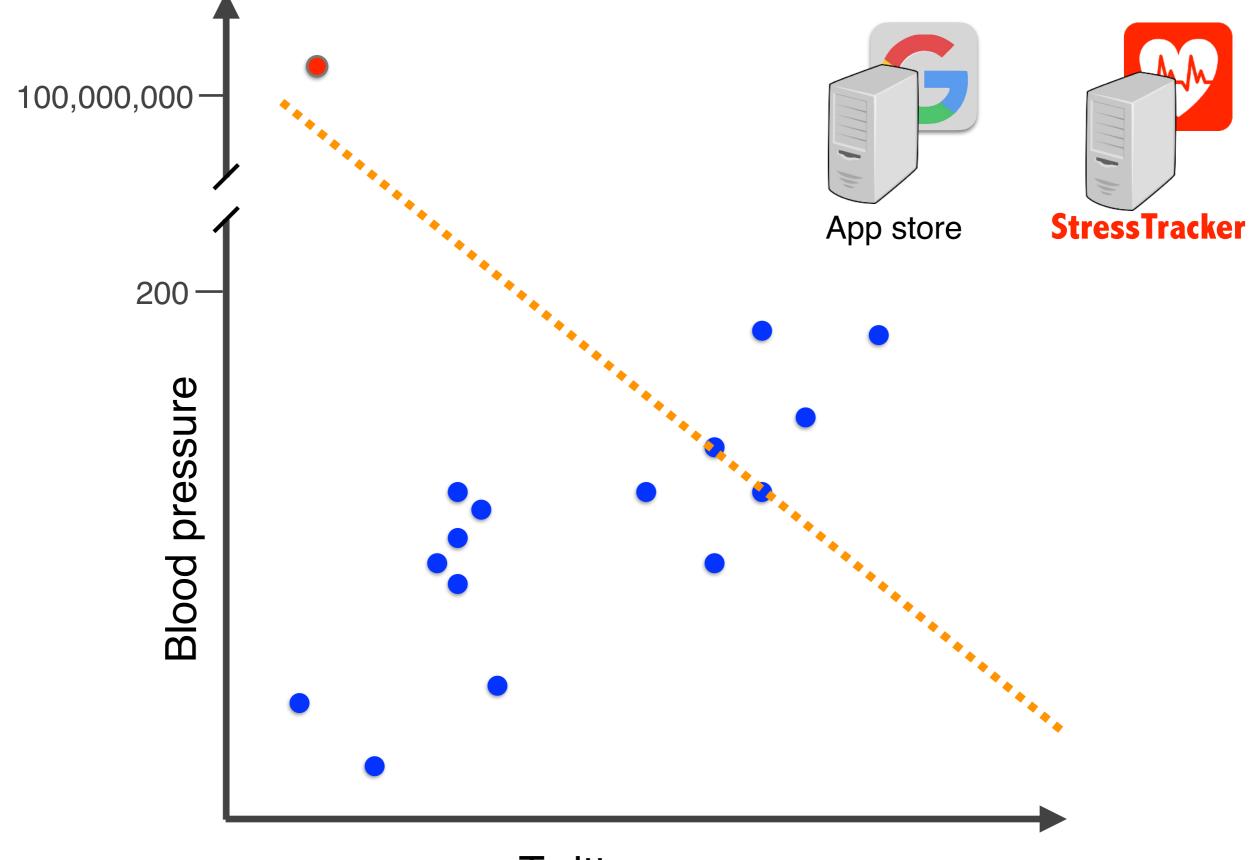






- **1. Exact correctness** If <u>all servers</u> are honest, servers learn $f(\cdot)$
- **2. Privacy** If <u>one server</u> is honest, servers learn only* $f(\cdot)$
- **3. Robustness** Malicious clients have bounded influence
- 4. EfficiencyNo public-key crypto (apart from TLS)1000s of submissions per second







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Prio is the first system to achieve all four.



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...and Prio supports a wide range of aggregation functions f(·)

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Contributions

1. Secret-shared non-interactive proofs (SNIPs)

- Client proves that its encoded submission is well-formed
- We do not need the power of traditional "heavy" crypto tools

2. Aggregatable encodings

Can compute sums privately \implies Can compute f(·) privately ...for many f's of interest

Contributions

1. Secret-shared non-interactive proofs (SNIPs)

- Client proves that its encoded submission is well-formed
- We do not need the power of traditional "heavy" crypto tools



See the paper

Related systems

- Additively homomorphic encryption
 P4P (2010), Private stream aggregation (2011), Grid aggregation (2011),
 PDDP (2012), SplitX (2013), PrivEx (2014), PrivCount (2016),
 Succinct sketches (2016), ...
- Multi-party computation [GMW87], [BGW88]
 FairPlay (2004), Brickell-Shmatikov (2006), FairplayMP (2008), SEPIA (2010), Private matrix factorization (2013), JustGarble (2013), ...
- Anonymous credentials/tokens VPriv (2009), PrivStats (2011), ANONIZE (2014), ...
- Randomized response [W65], [DMNS06], [D06] RAPPOR (2014, 2016), ...

Prio is the first system to achieve

exact correctness, privacy, robustness, efficiency.

Outline

- Background: The private aggregation problem
- A straw-man solution for private sums
- Providing robustness with SNIPs
- Evaluation
- Discussion: Real-world considerations

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Warm-up: Computing private sums

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- Every device i holds a value x_i
- We want to compute

 $f(\mathbf{X}_1, \ldots, \mathbf{X}_N) = \mathbf{X}_1 + \ldots + \mathbf{X}_N$

without learning any users' private value x_i.

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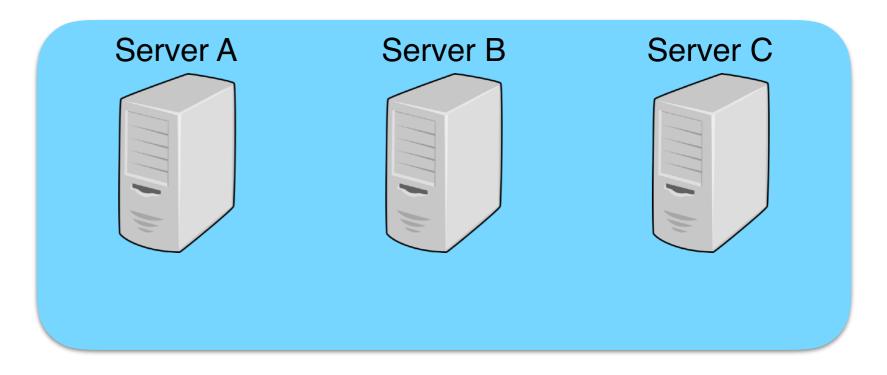
without learning any users' private value x_i.

Example: Privately measuring traffic congestion.

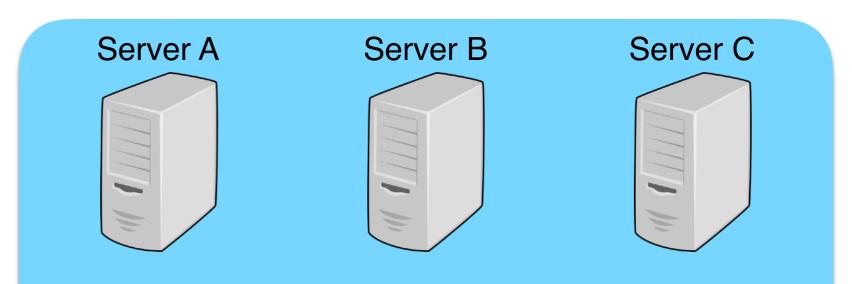


The sum $x_1 + \ldots + x_N$ yields the number of app users on the Bay Bridge.

[Chaum88], [BGW88], ... [KDK11] [DFKZ13] [PrivEx14] ...



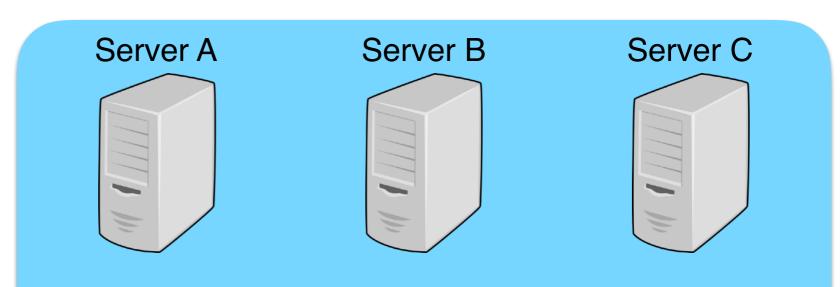
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Assume that the servers are non-colluding.

Equivalently: that at least one server is honest.

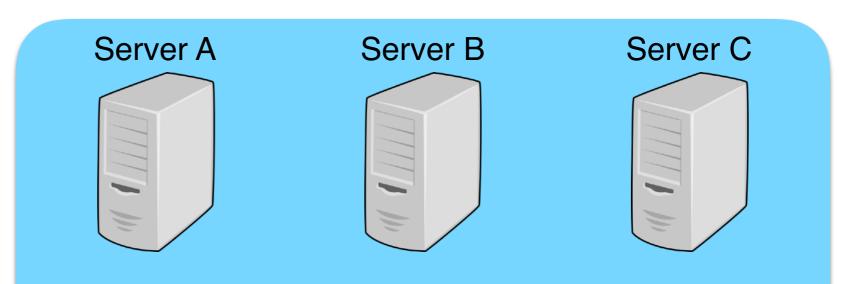
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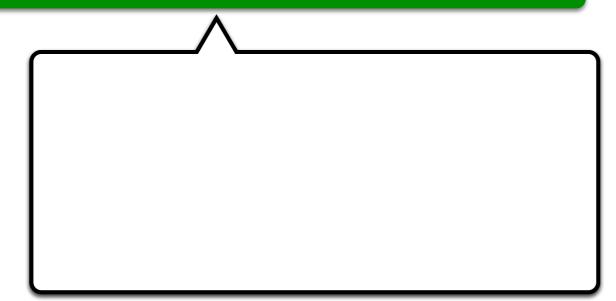


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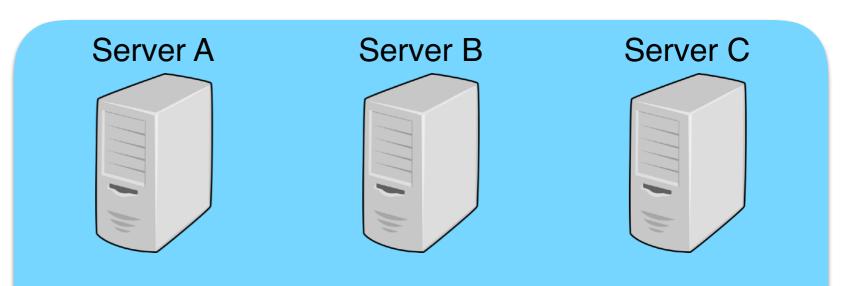


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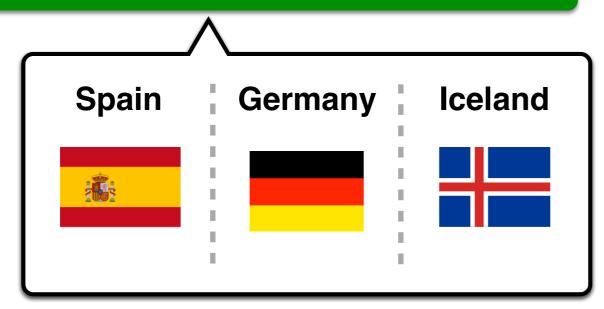


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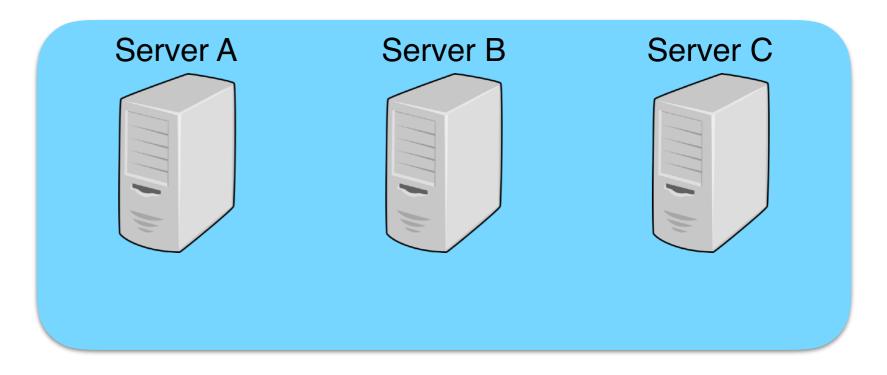


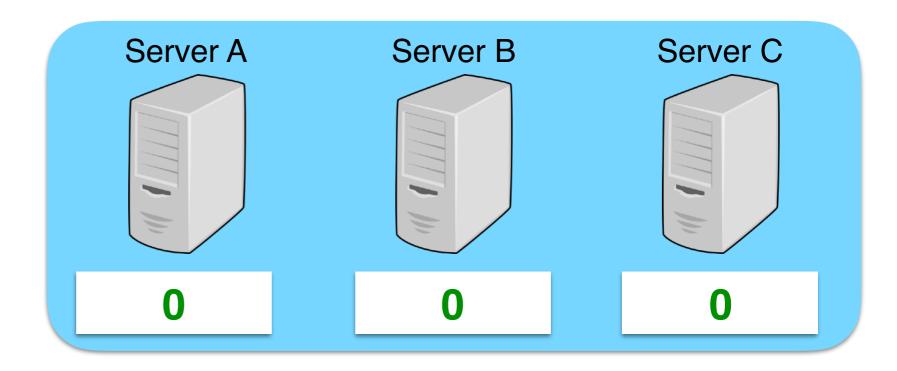
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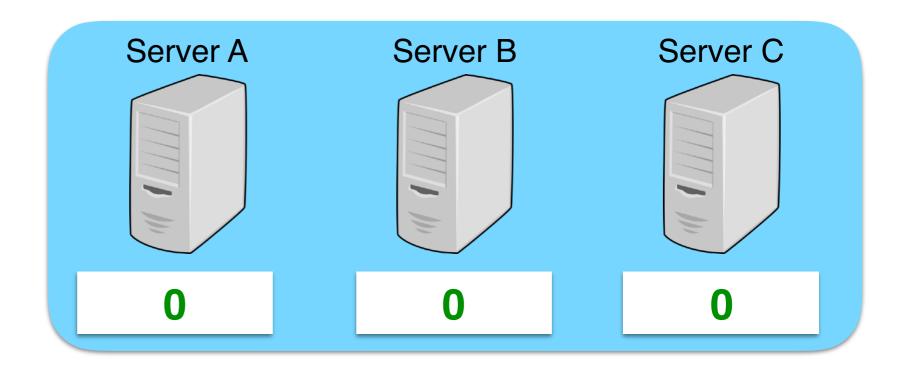


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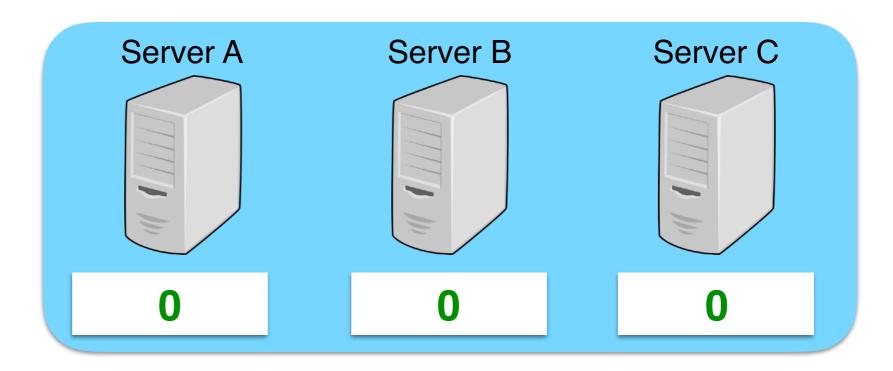
Secret sharing Pick three random "shares" that sum to 1. 1 = 15 + (-12) + (-2) (mod 31)

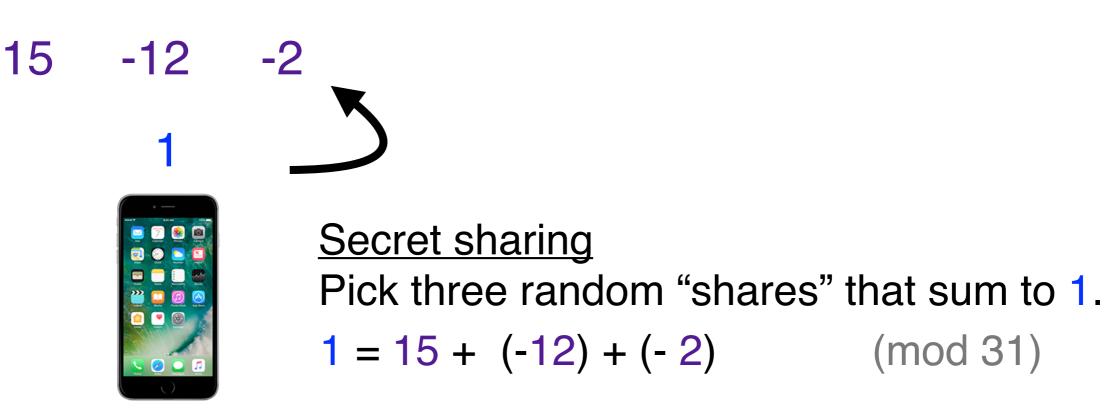
Need all three shares to recover the shared value.



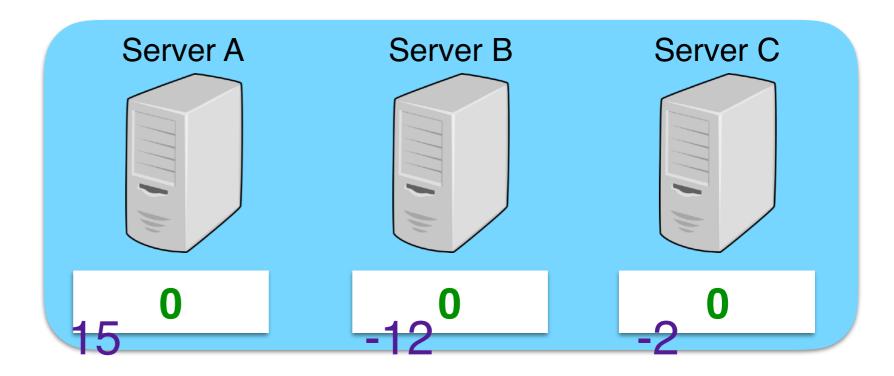
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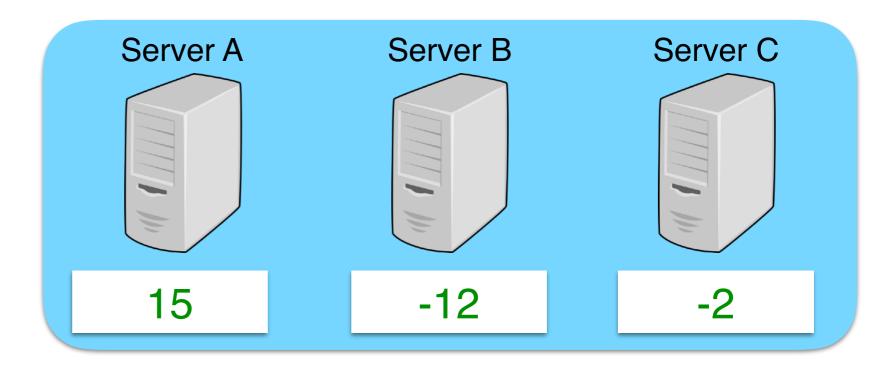




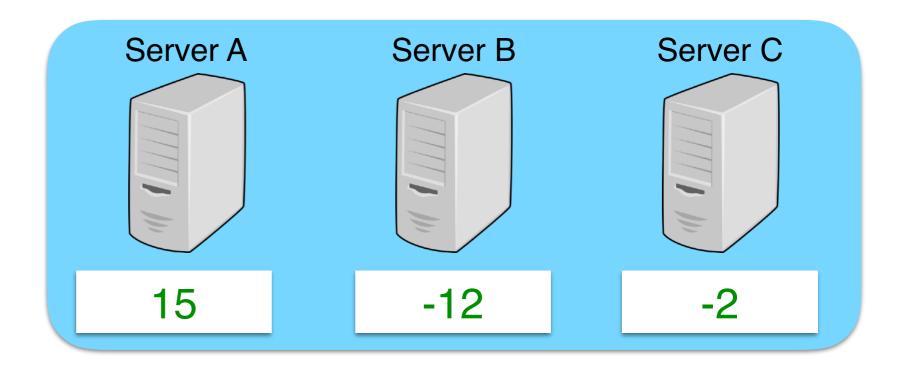
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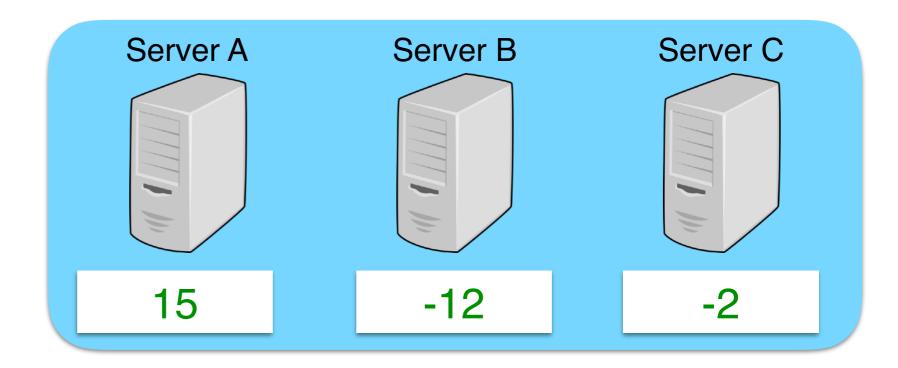








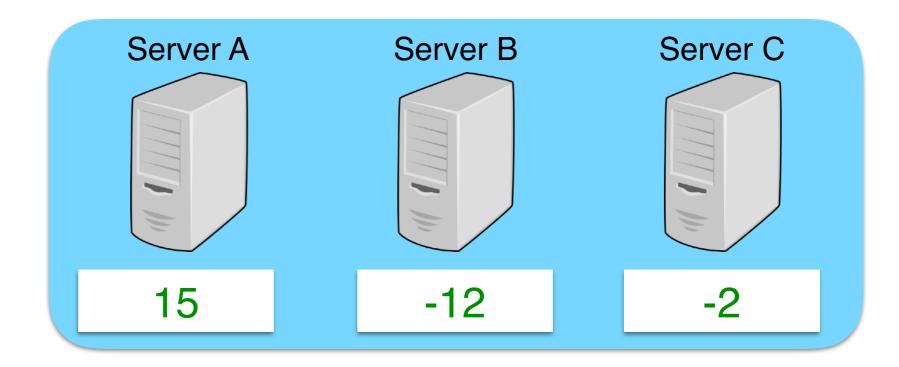


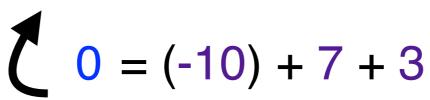


0 = (-10) + 7 + 3



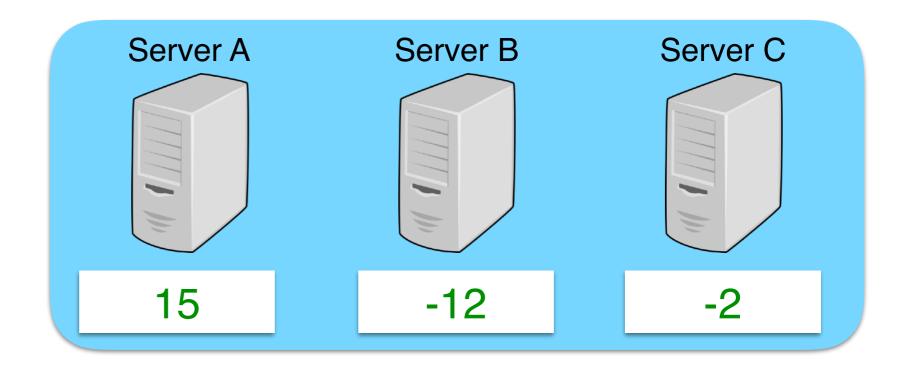






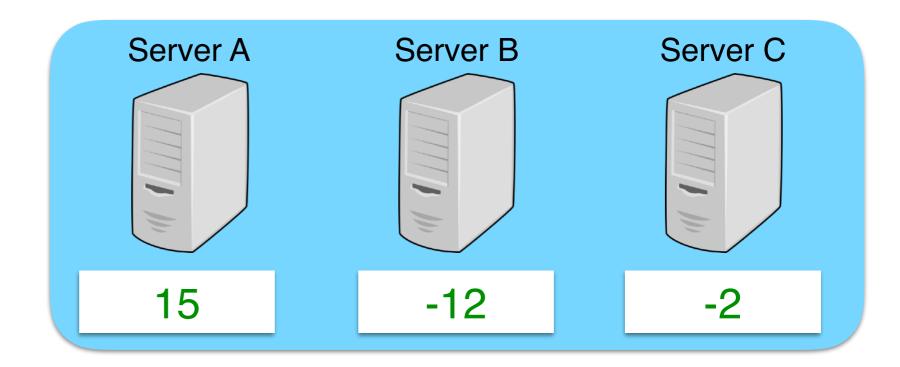




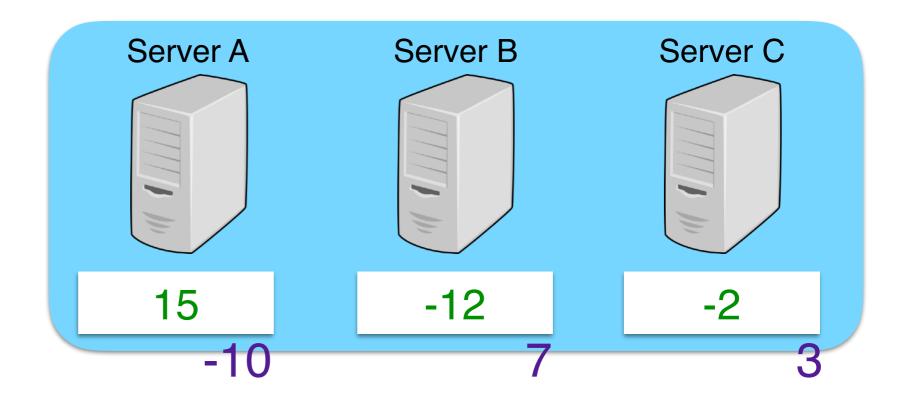


$$-10 \quad 7 \quad 3$$

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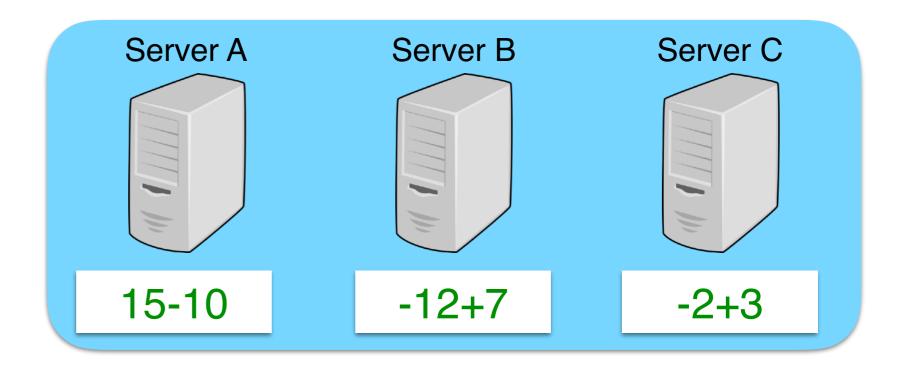












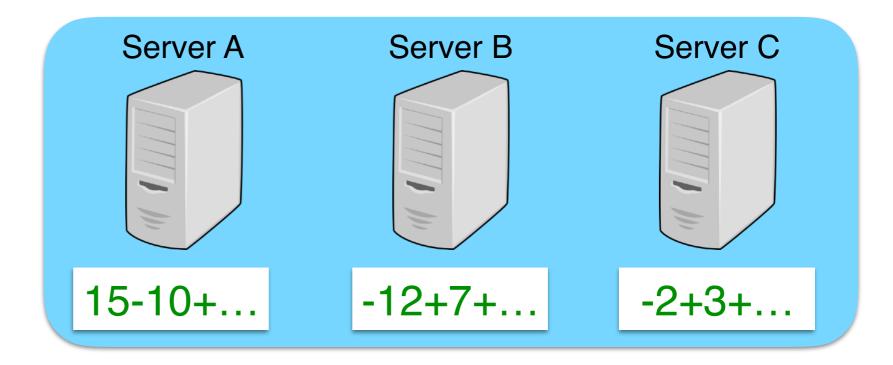


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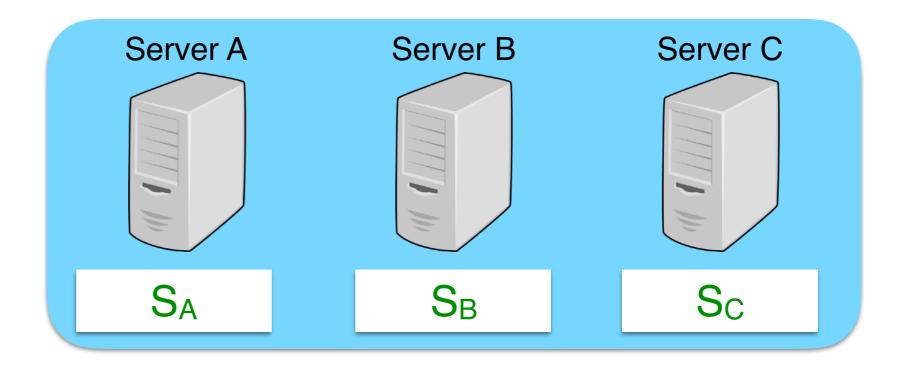


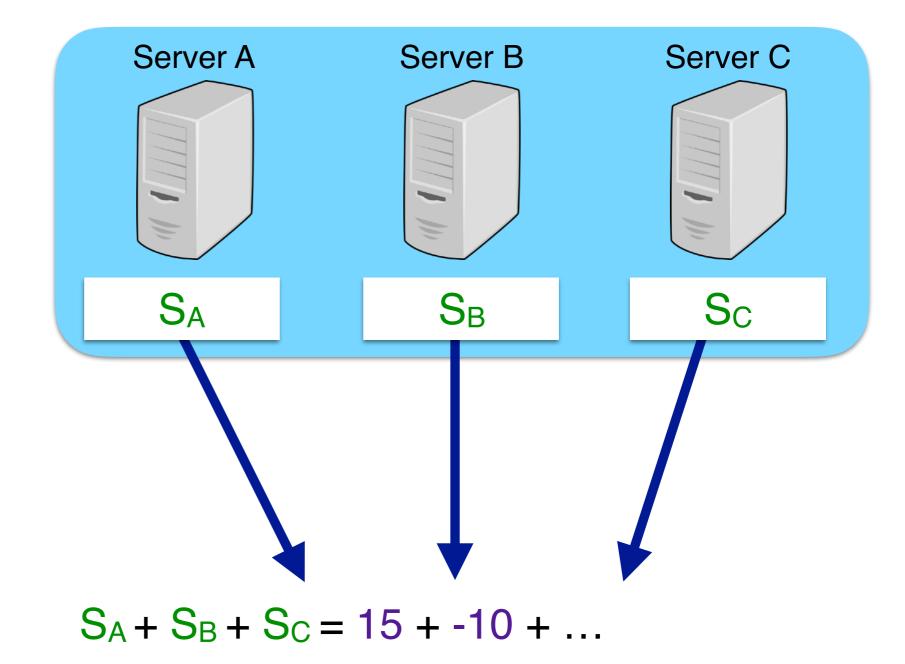


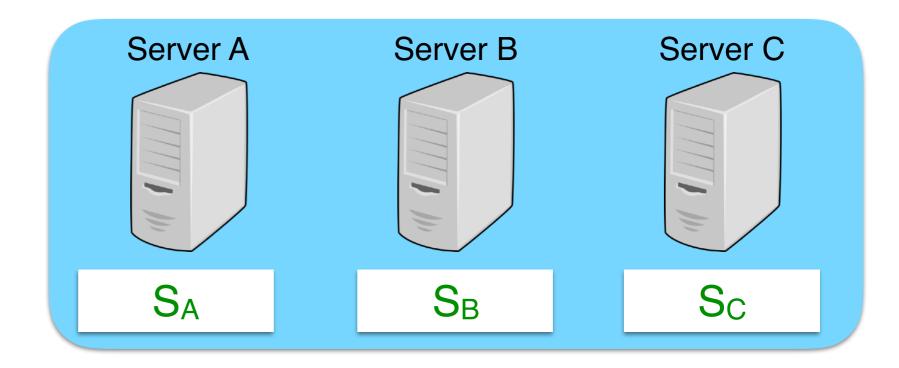




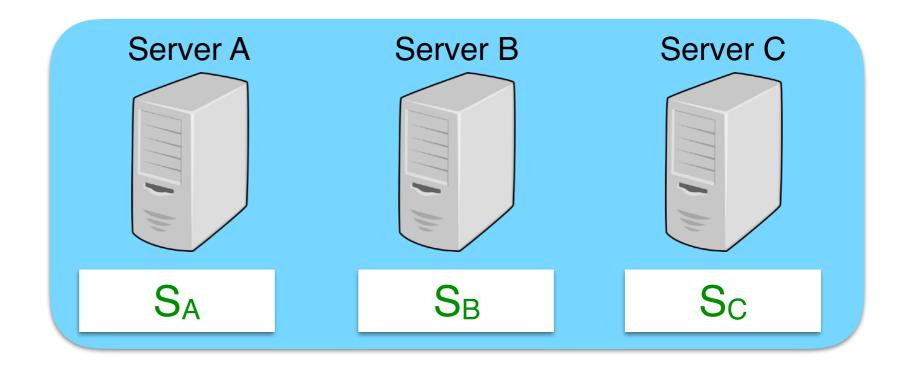






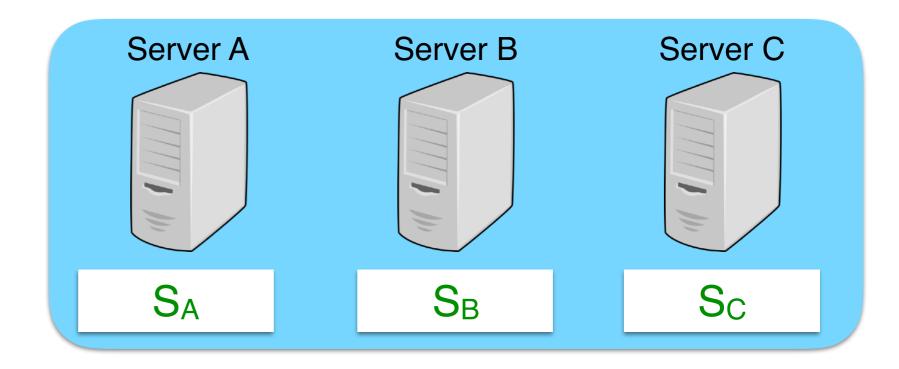


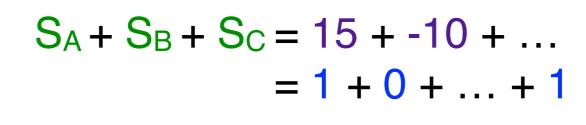
$$S_A + S_B + S_C = 15 + -10 + \dots$$



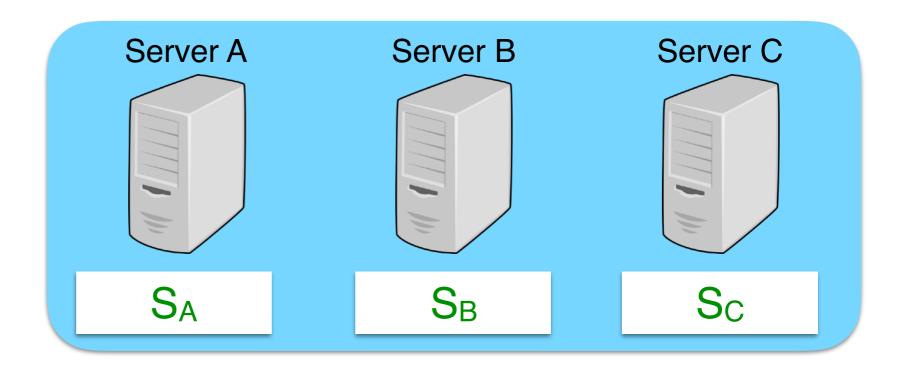
$$S_A + S_B + S_C = 15 + -10 + \dots$$

= 1 + 0 + \dots + 1





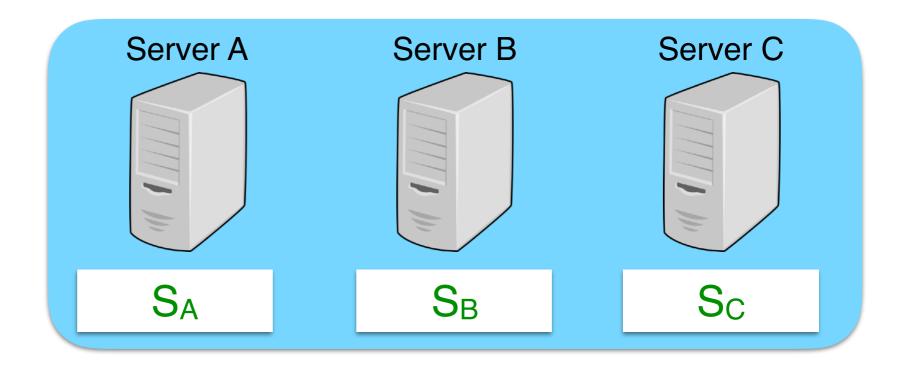
Servers learn the sum of client values and learn *nothing else*.





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 $S_A + S_B + S_C = 15 + -10 + \dots$ = 1 + 0 + \dots + 1

> Learn that three phones are on the Bay Bridgedon't know which three

Computing private sums

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Exact correctness: If everyone follows the protocol, servers compute the sum of all x_i s.

Privacy: Any proper subset of the servers learns nothing but the sum of the x_i s.

Efficiency: Follows by inspection.

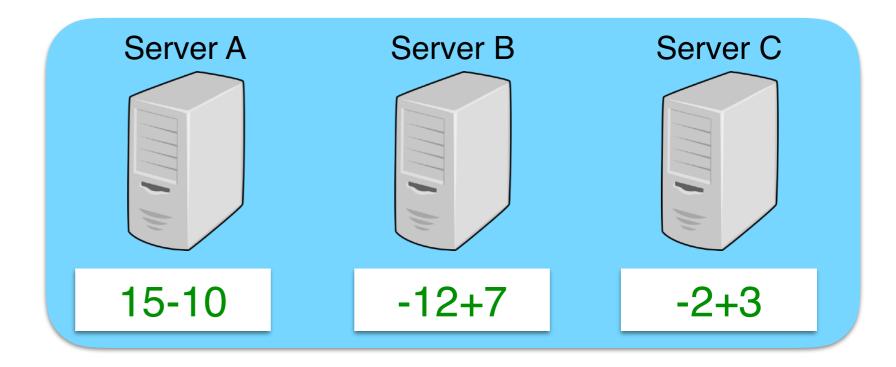
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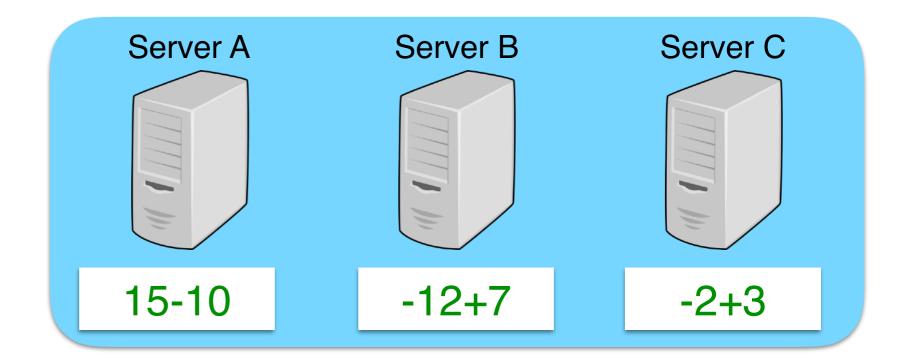




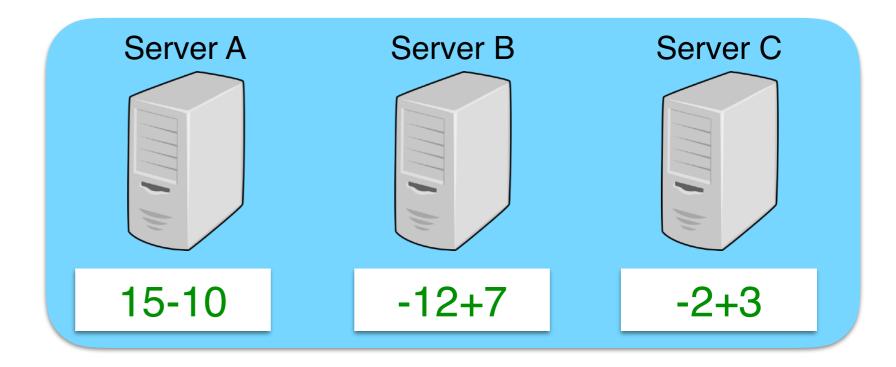










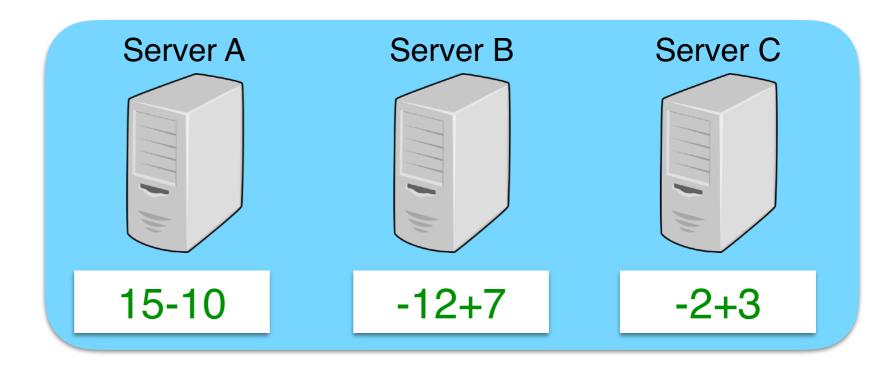








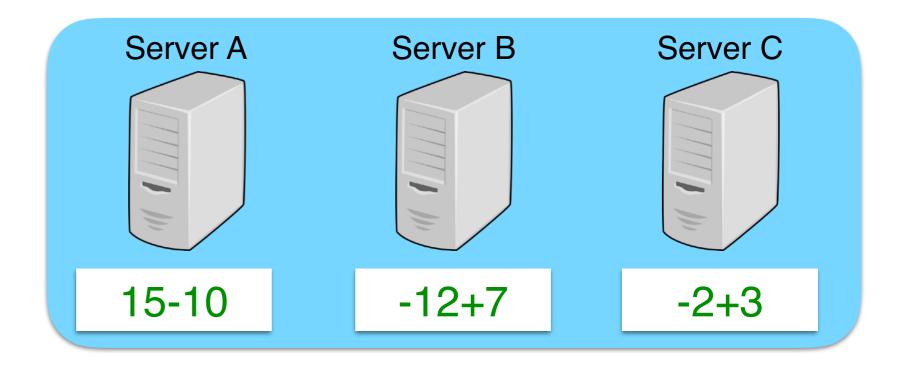










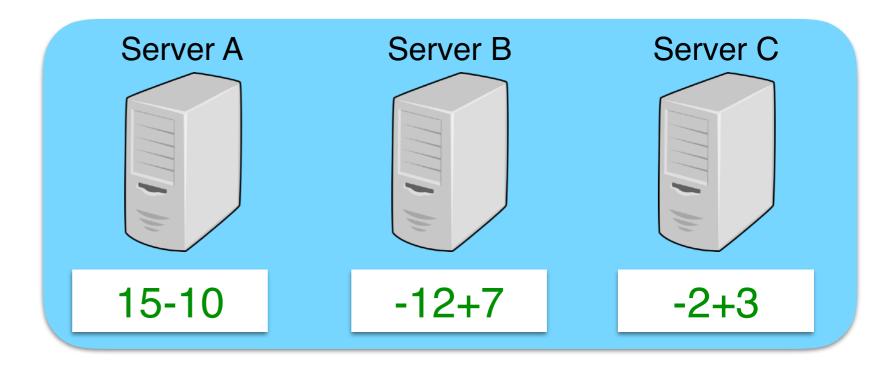


An evil client needn't follow the rules!

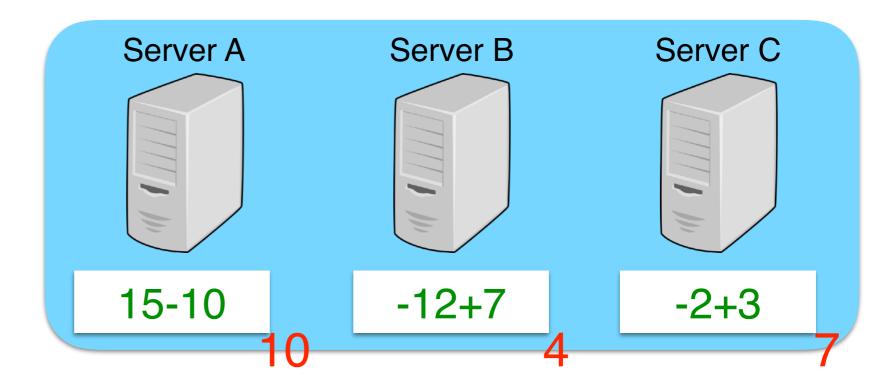
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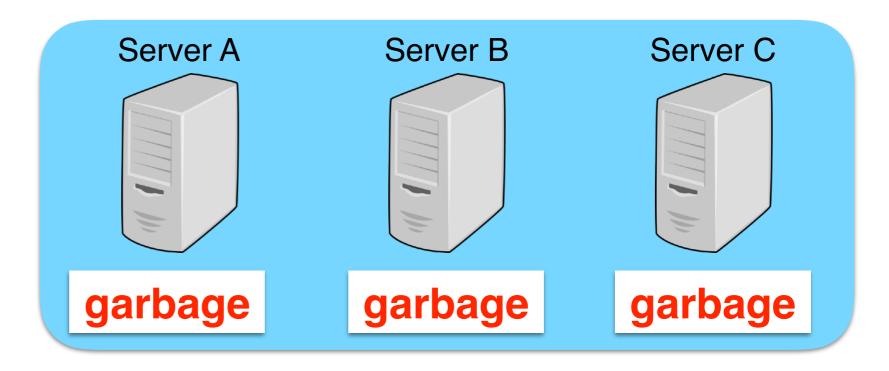








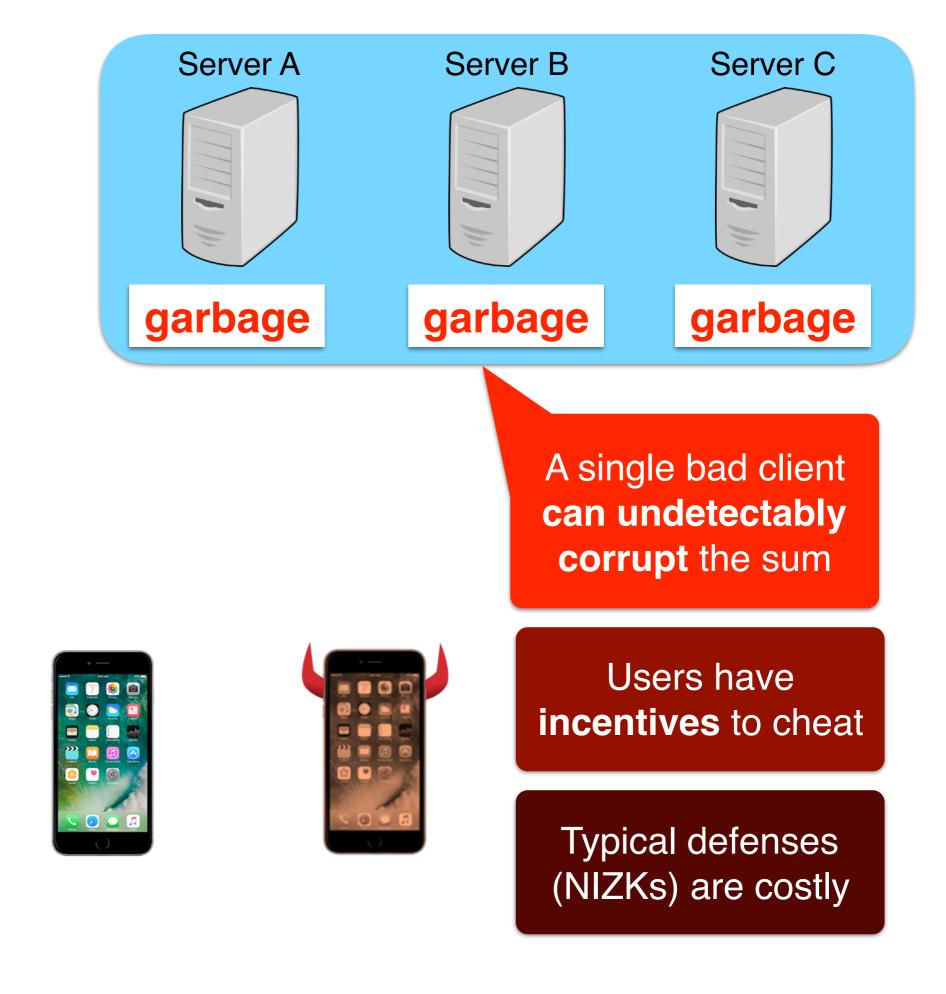












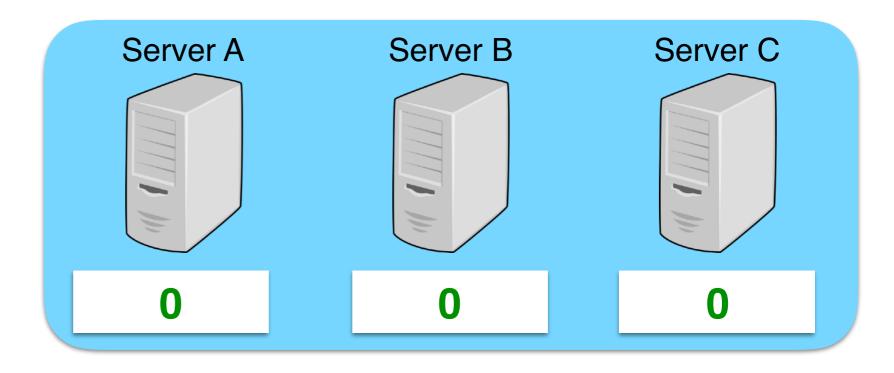


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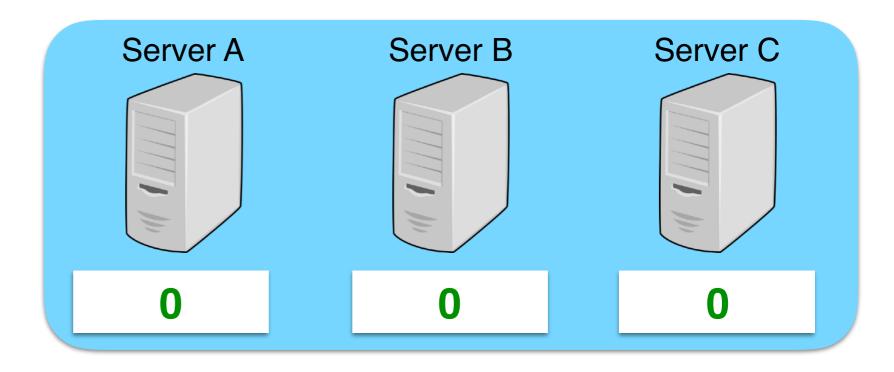
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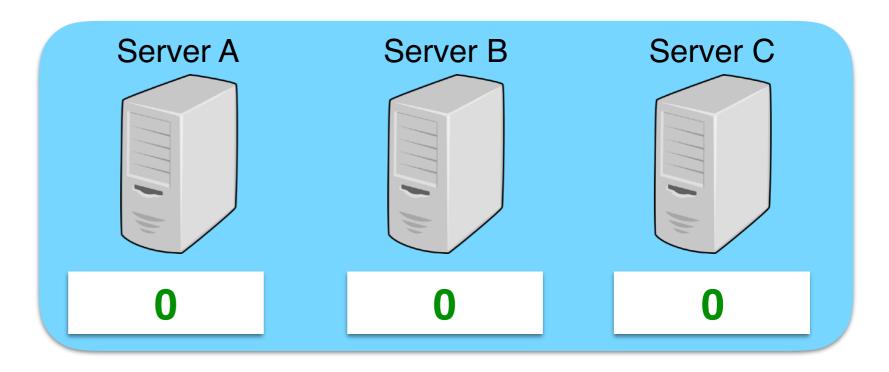


x = 1

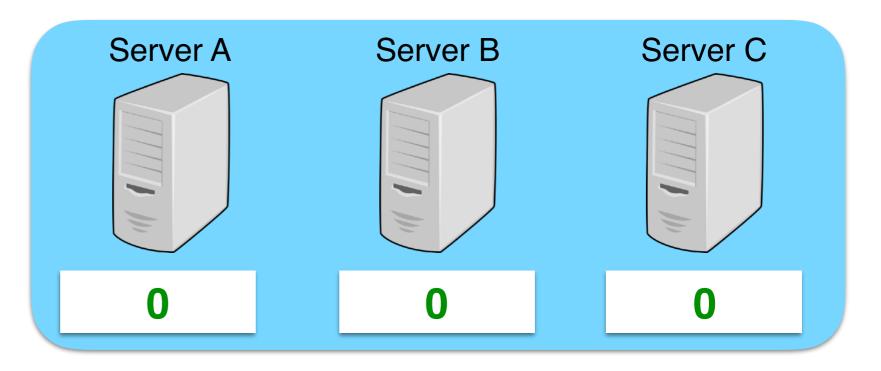


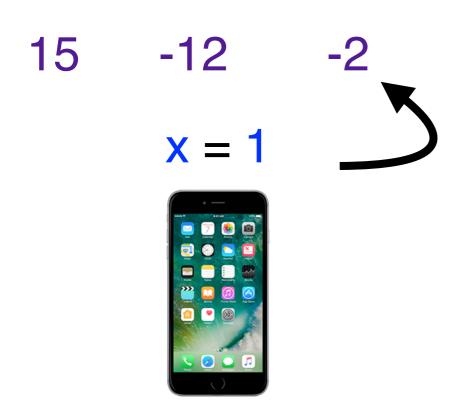


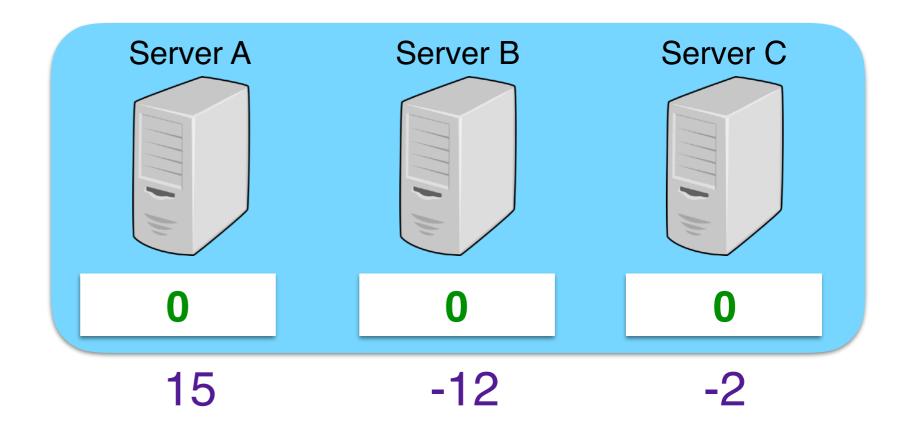




15 + (-12) + (-2) = 1x = 1



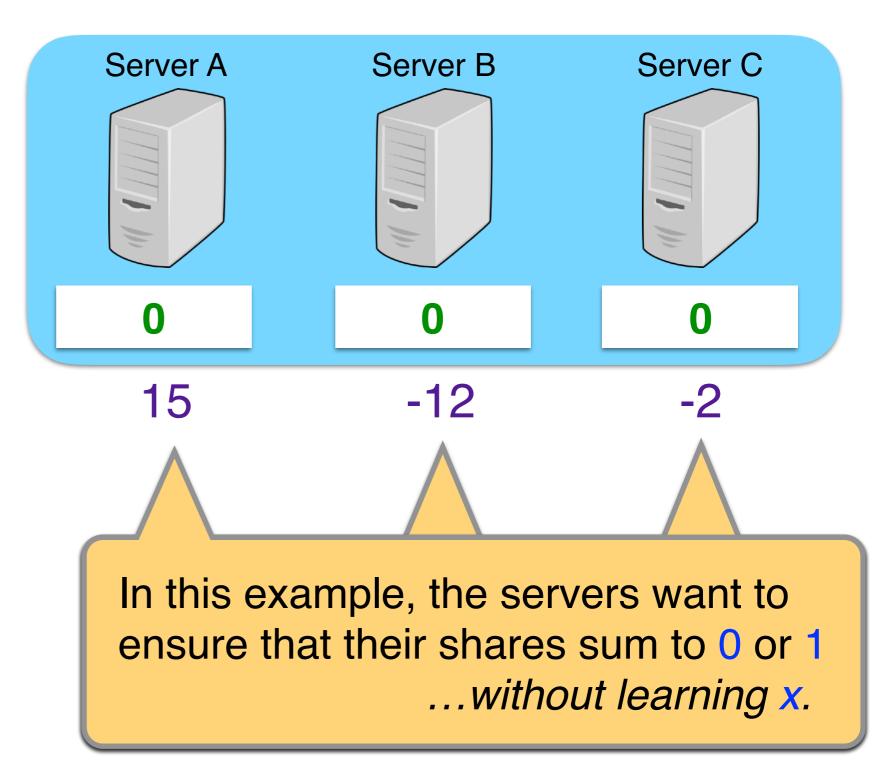


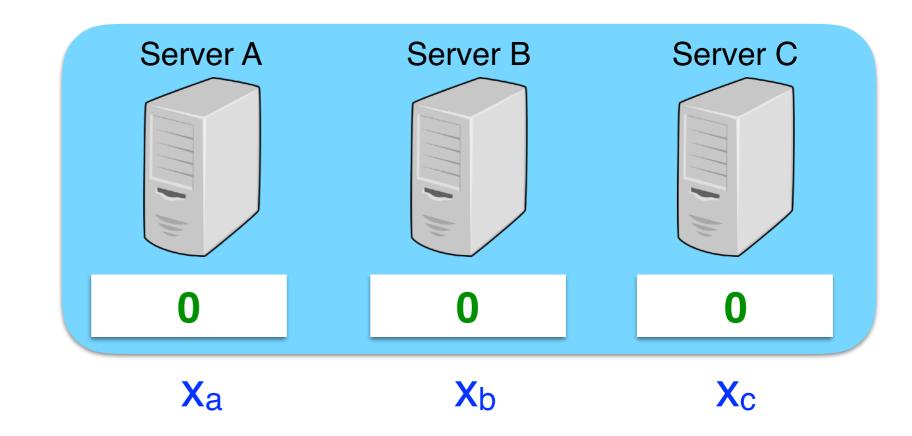


x = **1**







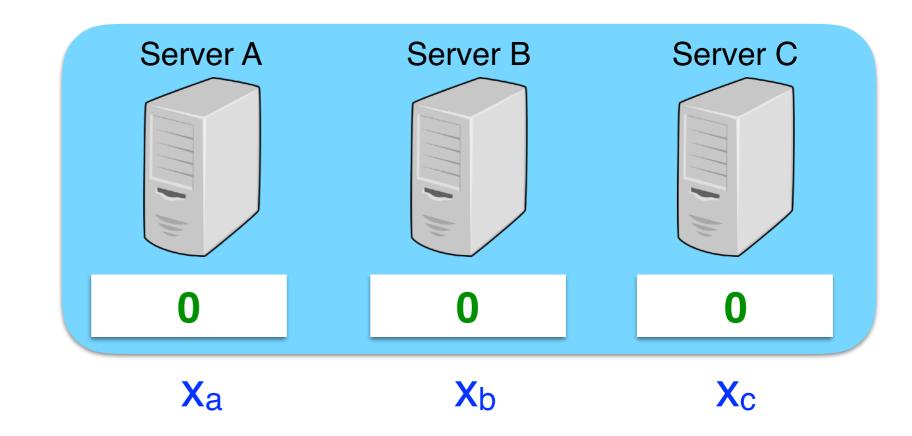


x = 1



More generally, servers

- hold shares of the client's private value x
- hold an <u>arbitrary</u> public predicate Valid(·)
 expressed as an arithmetic circuit
- want to test if "Valid(x)" holds, without leaking x



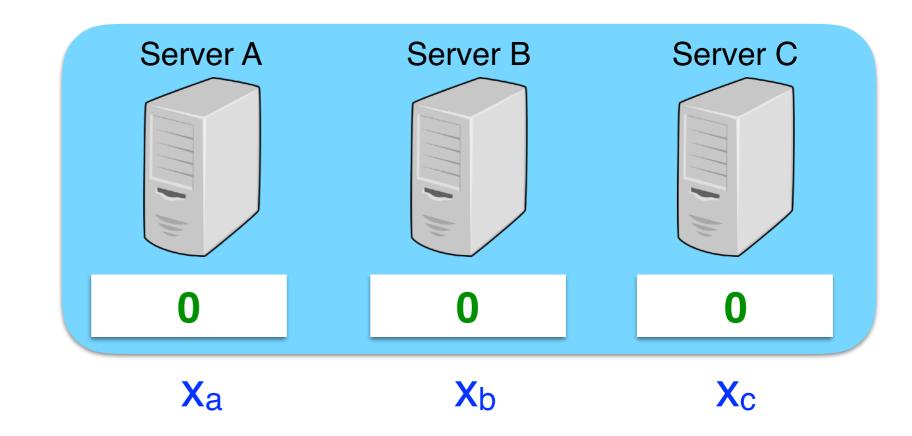
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For our running example: Valid(x) = " $x \in \{0,1\}$ "

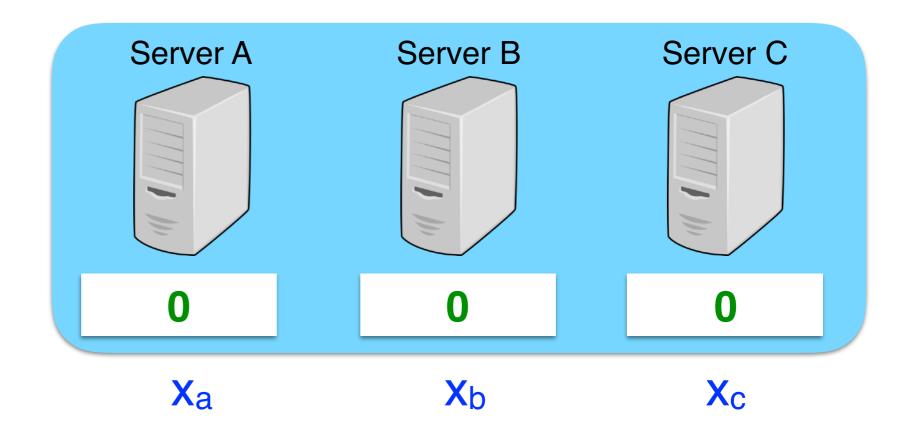


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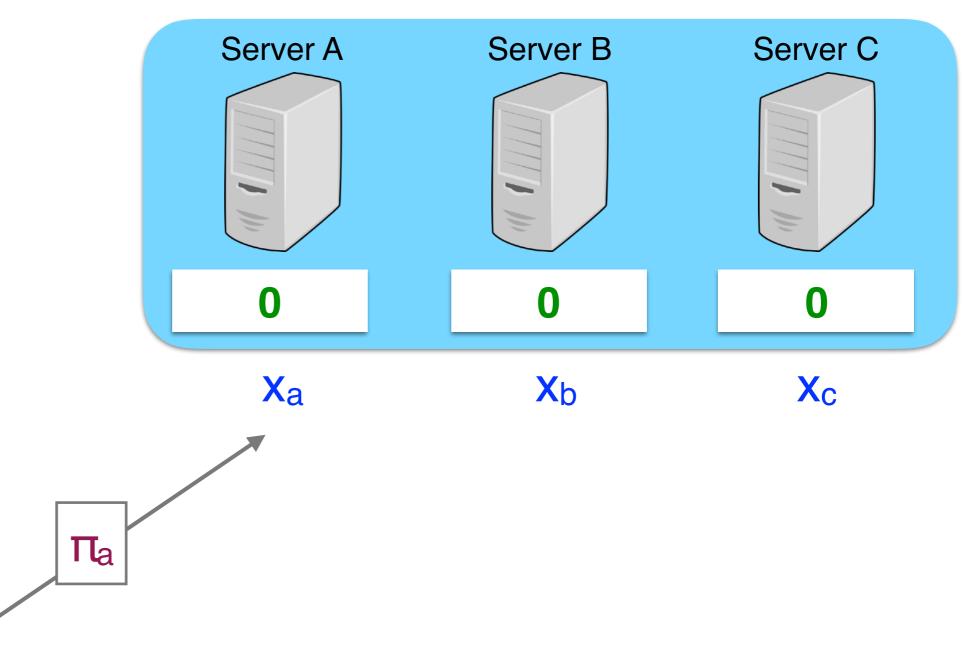


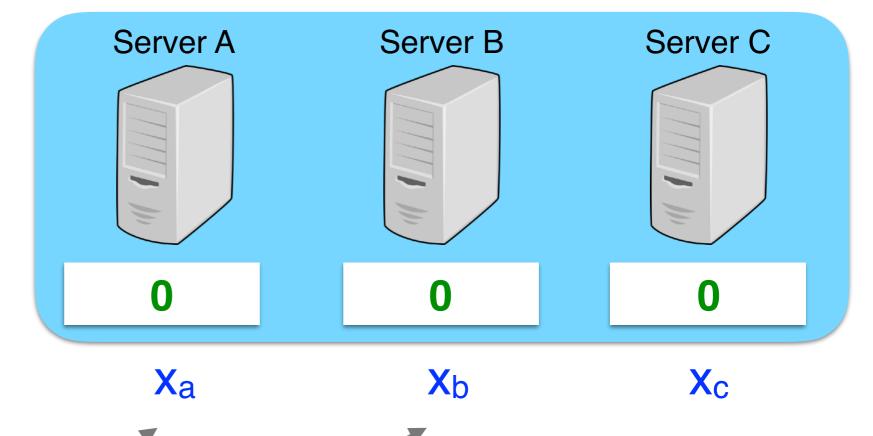


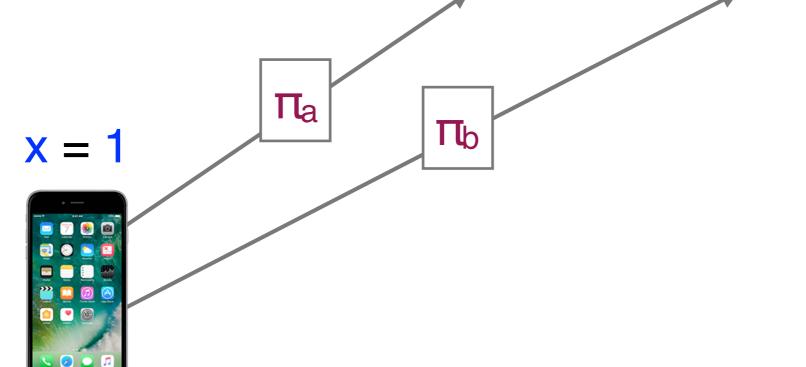
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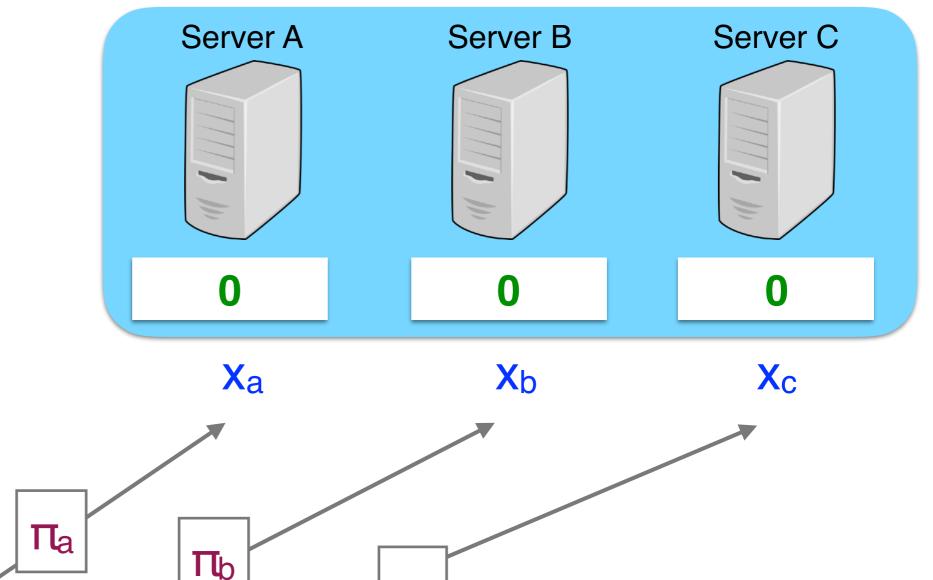
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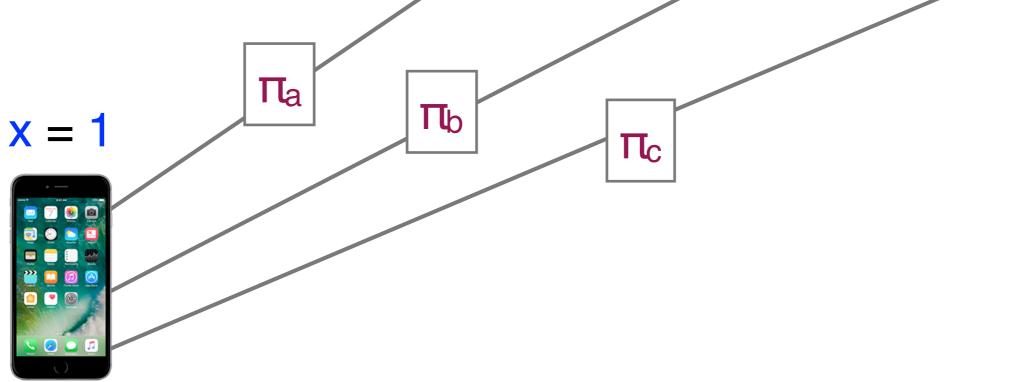
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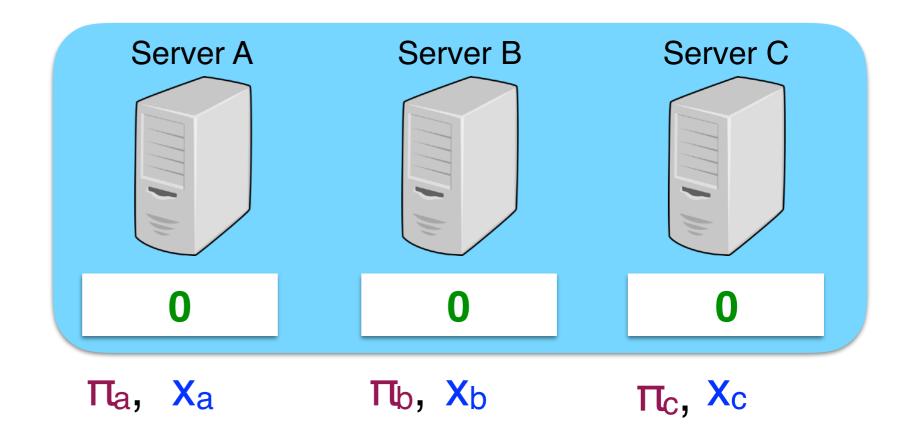


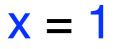




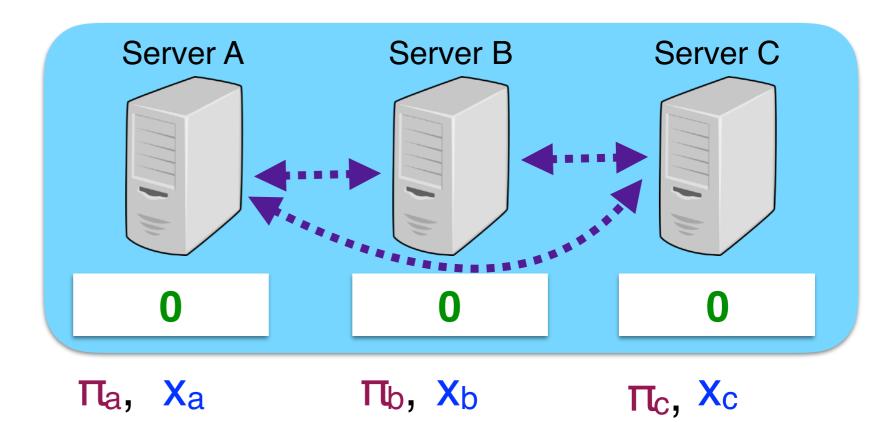




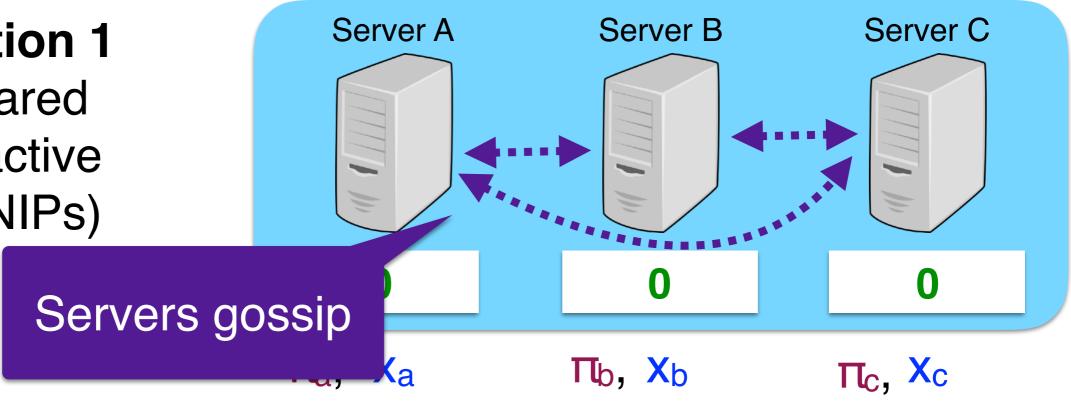






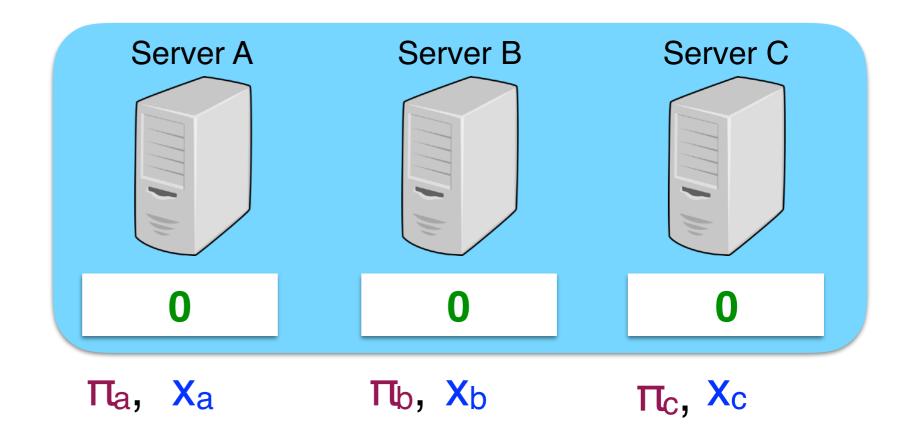


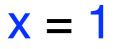




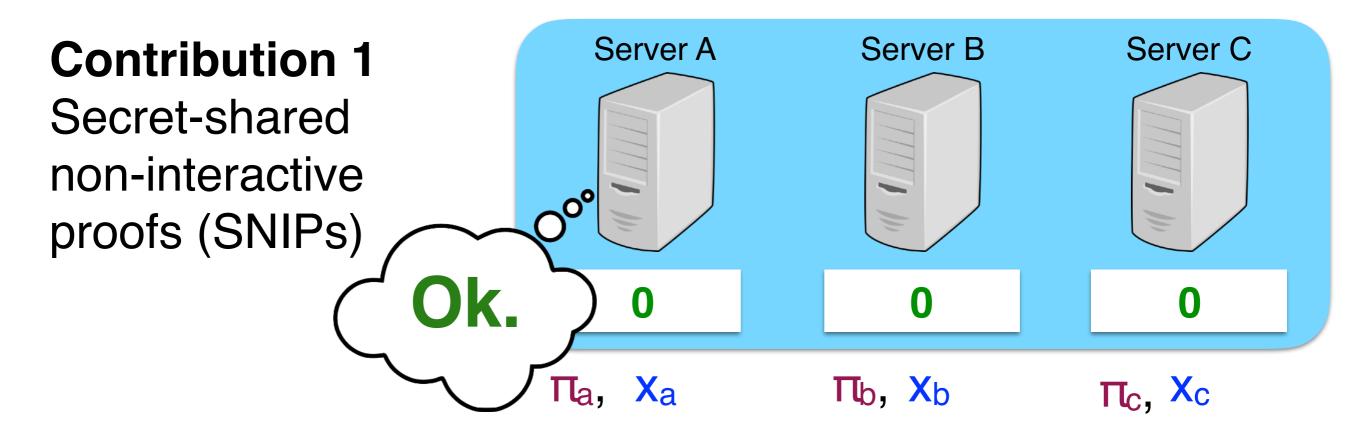




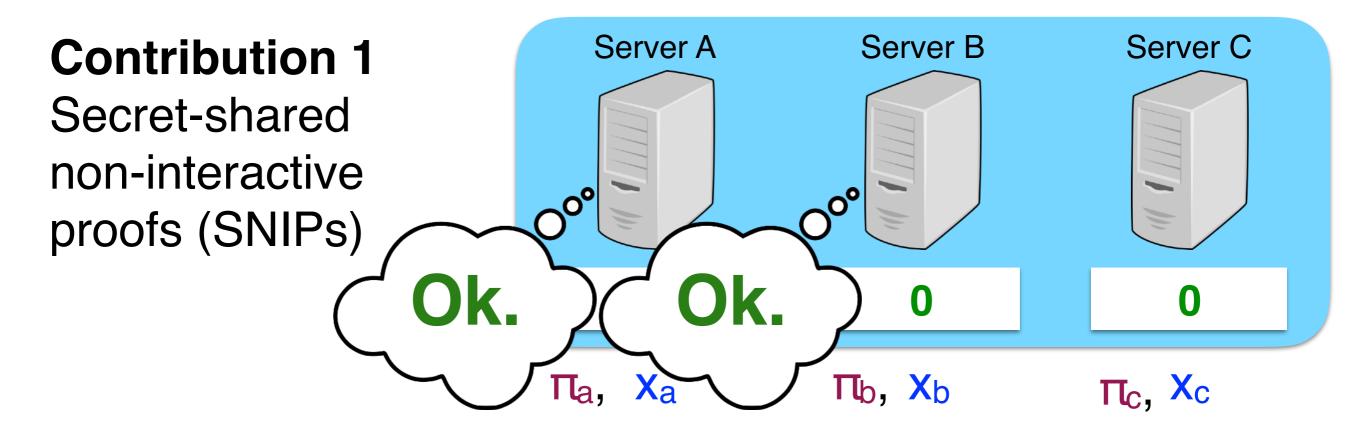




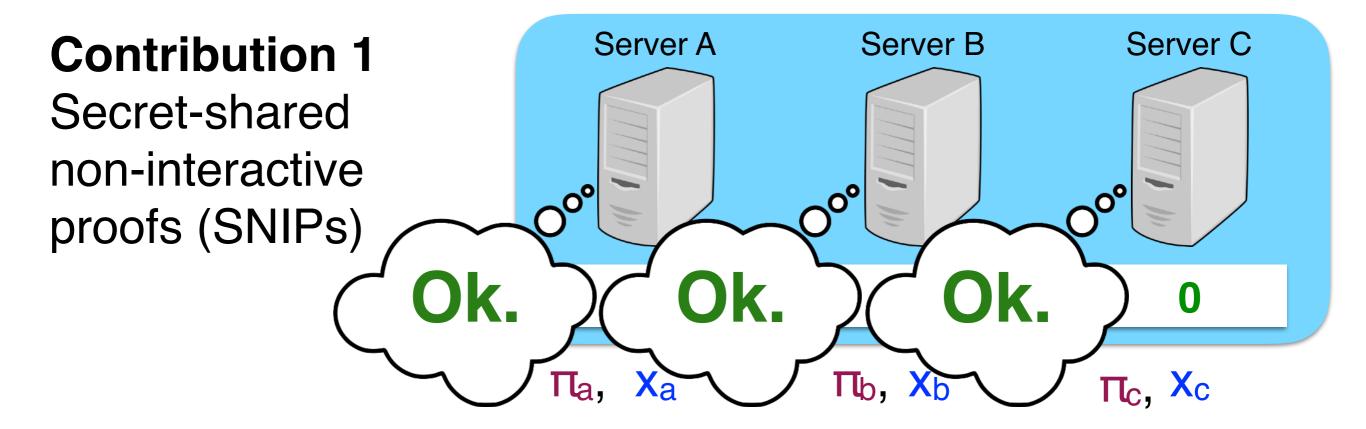




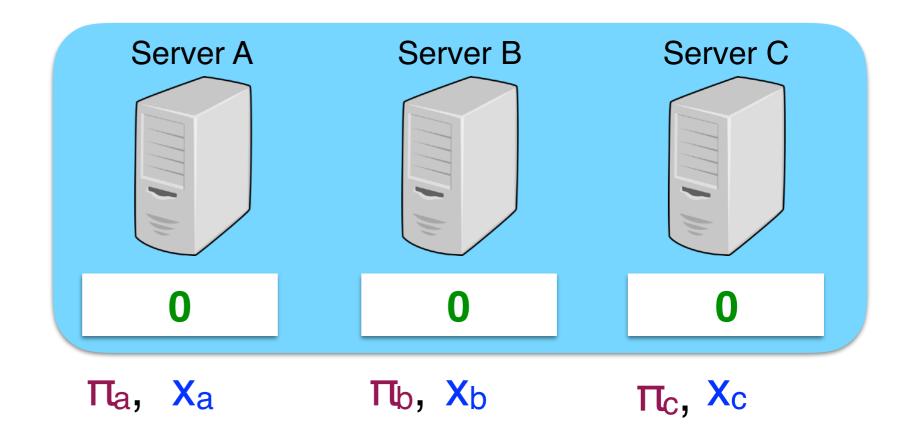


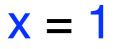




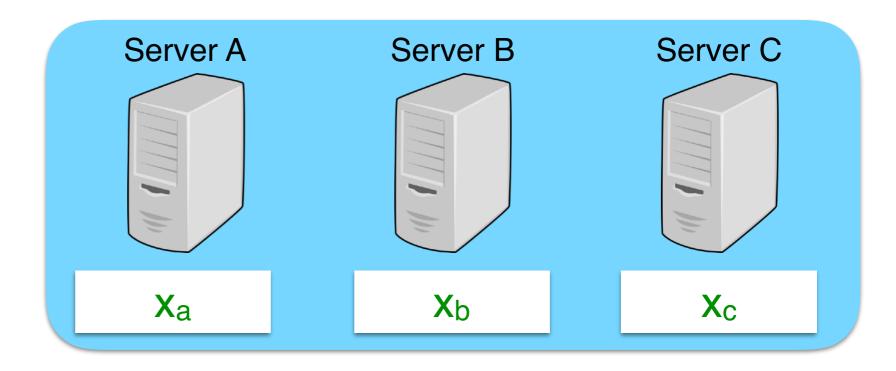




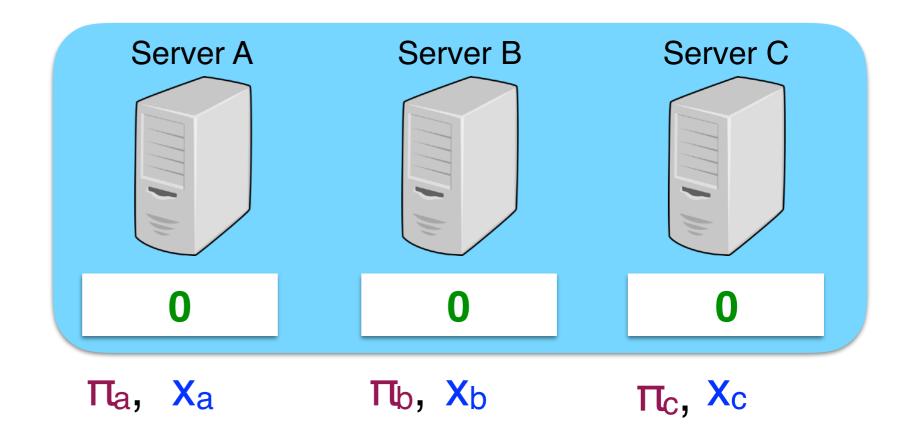


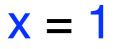




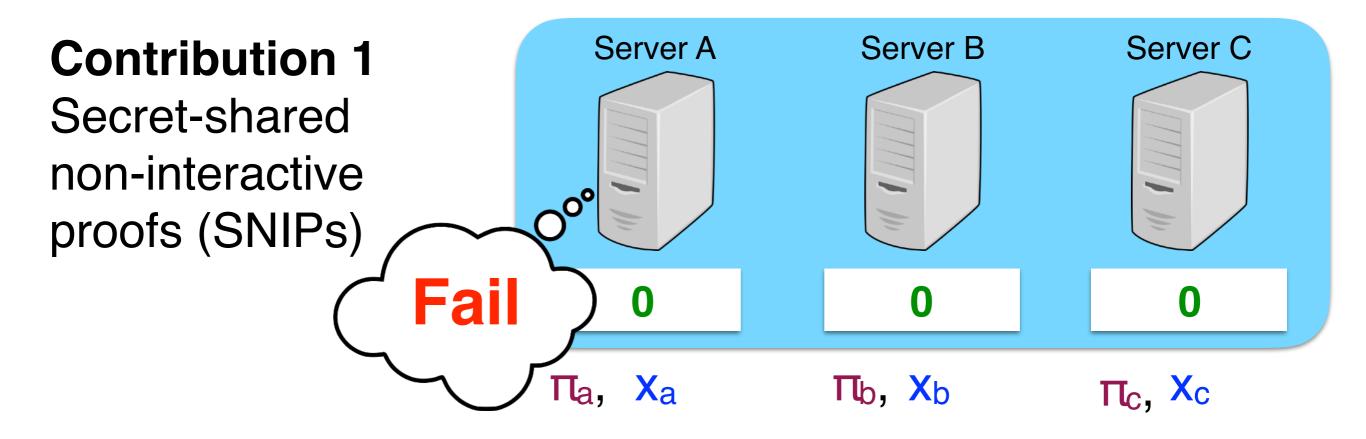




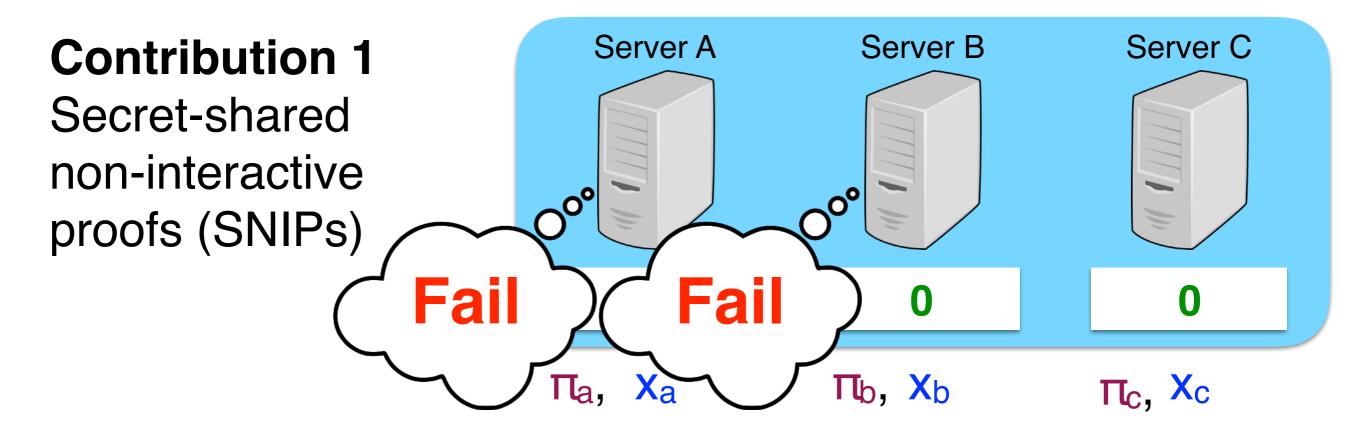




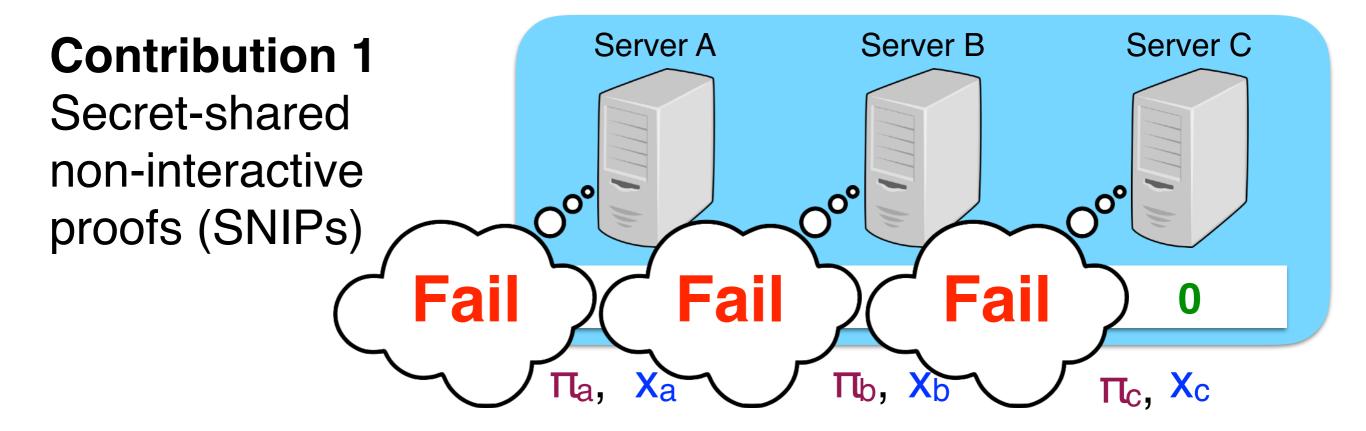




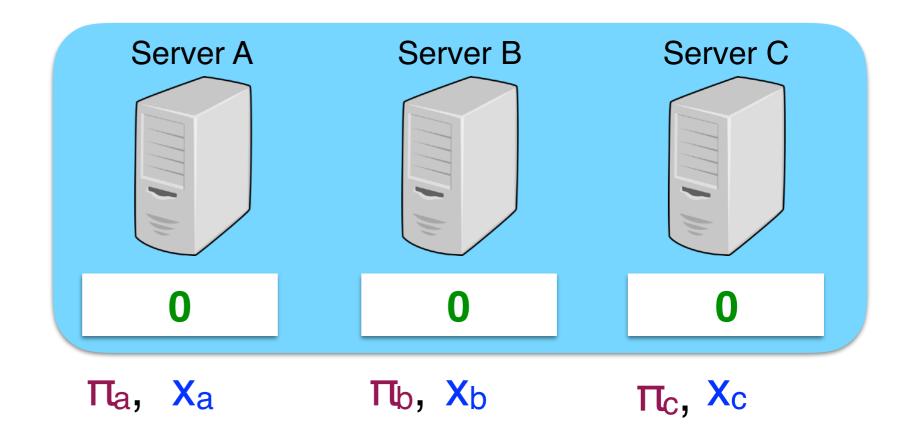


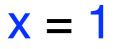




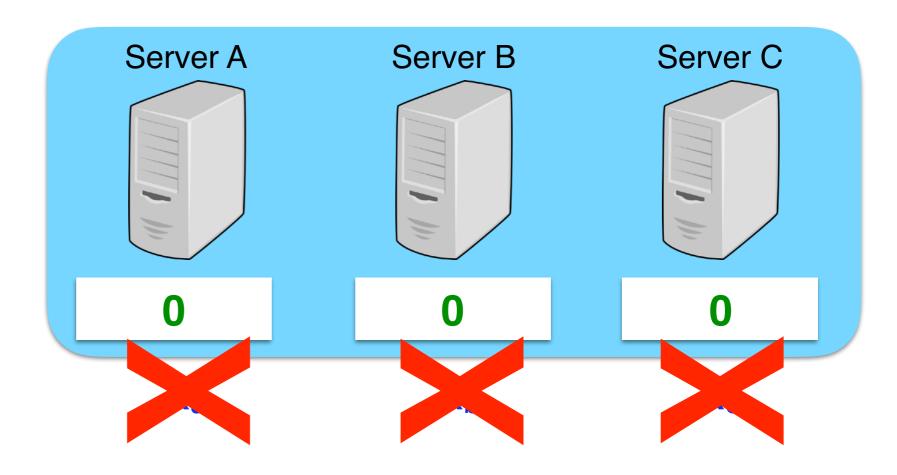








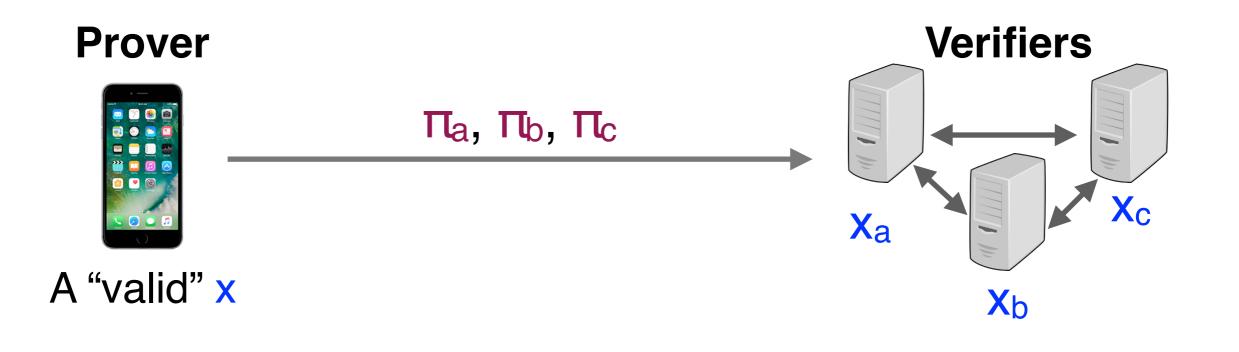


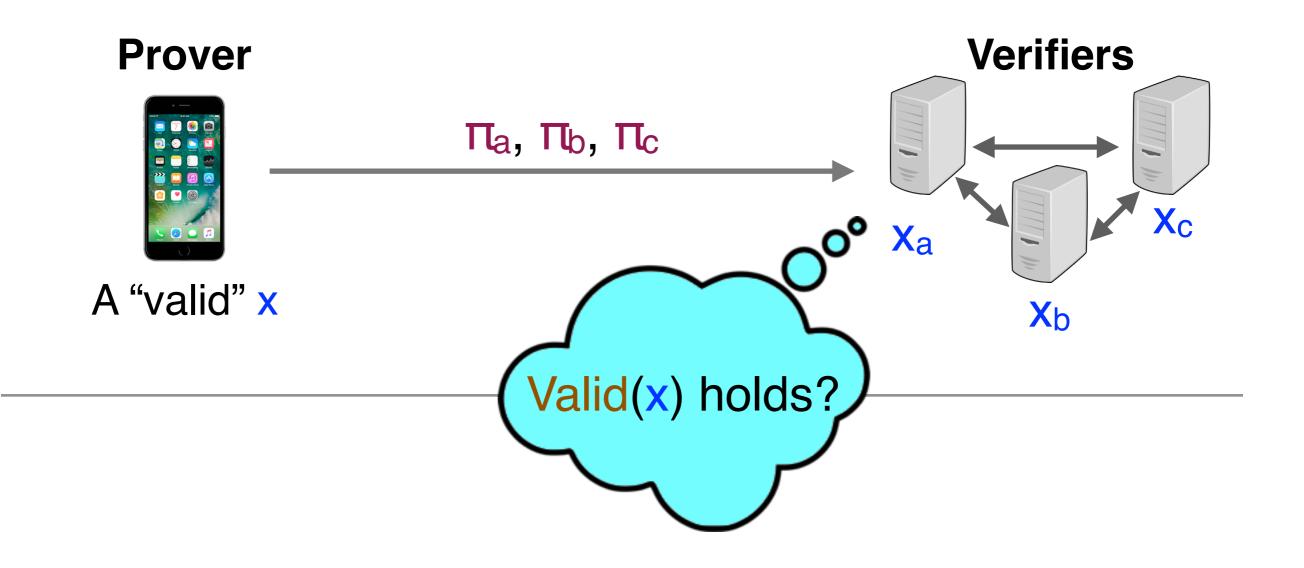


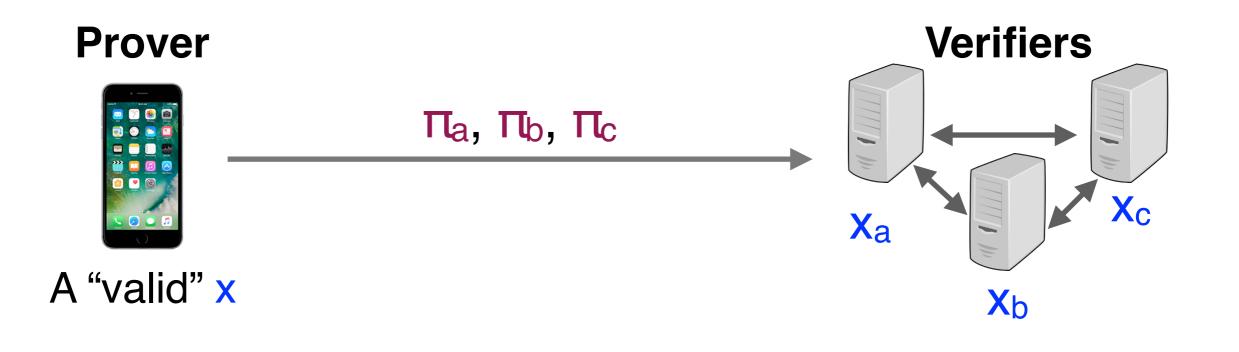


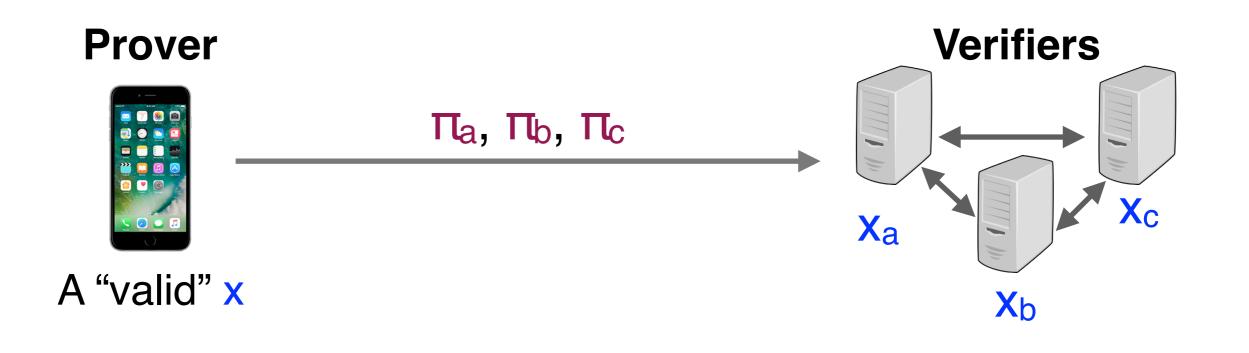


- Prio servers detect and reject malformed client submissions
- In this example, each client can influence the aggregate statistic by +/- 1, at most









Completeness.Honest prover convinces honest verifiers.Soundness.Dishonest prover rarely convinces
honest verifiers.Zero knowledge.Any proper subset of the verifiers learns
nothing about x, except that x is valid.

Traditional techniques

- Non-interactive proofs in ROM [FS86], [BFM88], [BDMP91], [CP92], [CS97], [M00], ...
- zkSNARKs and KOE-based proofs [G10], [L12], [GGPR13], [BCGTV13], [PGHR13], ...
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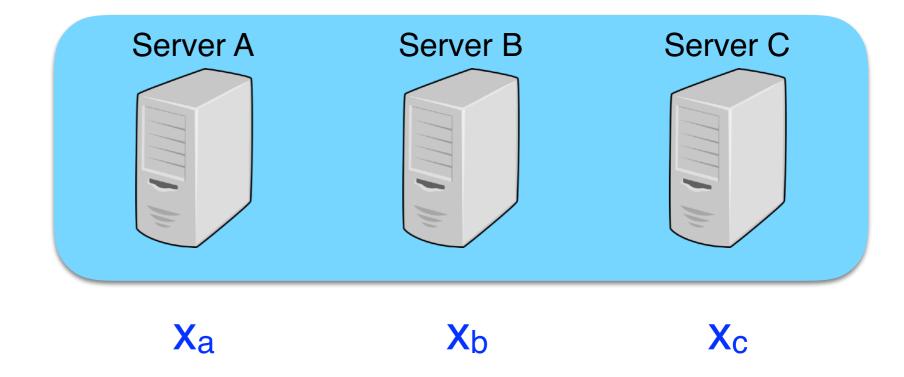
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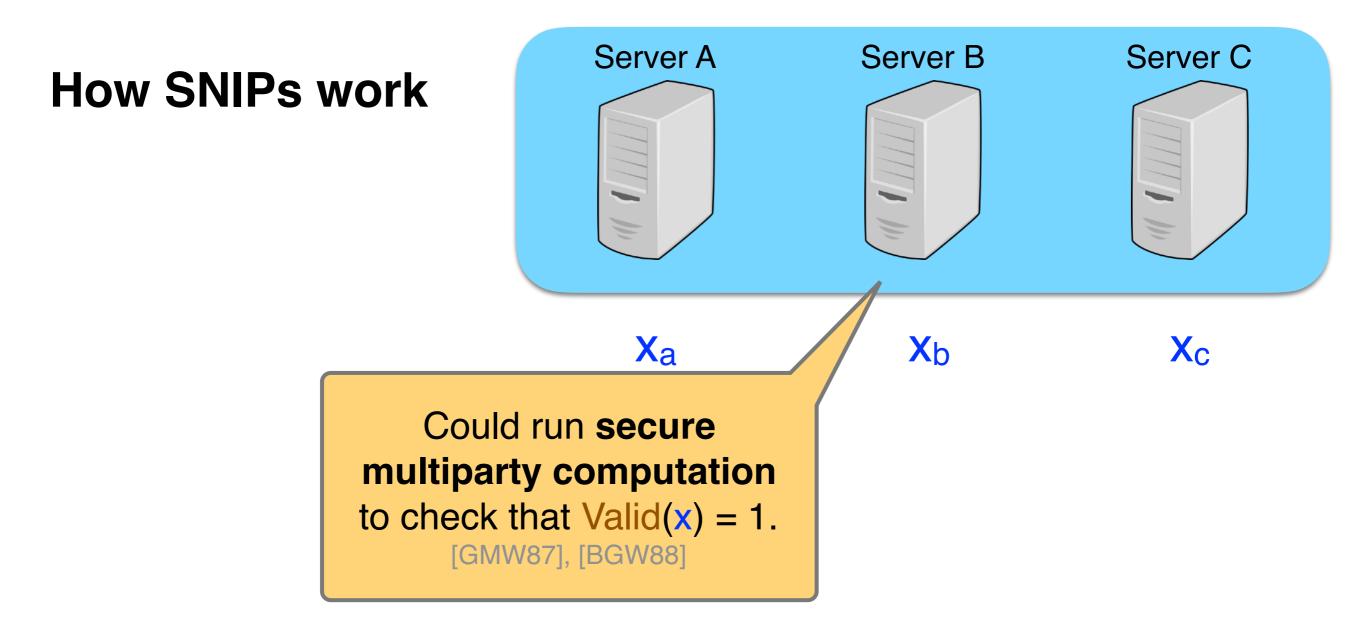
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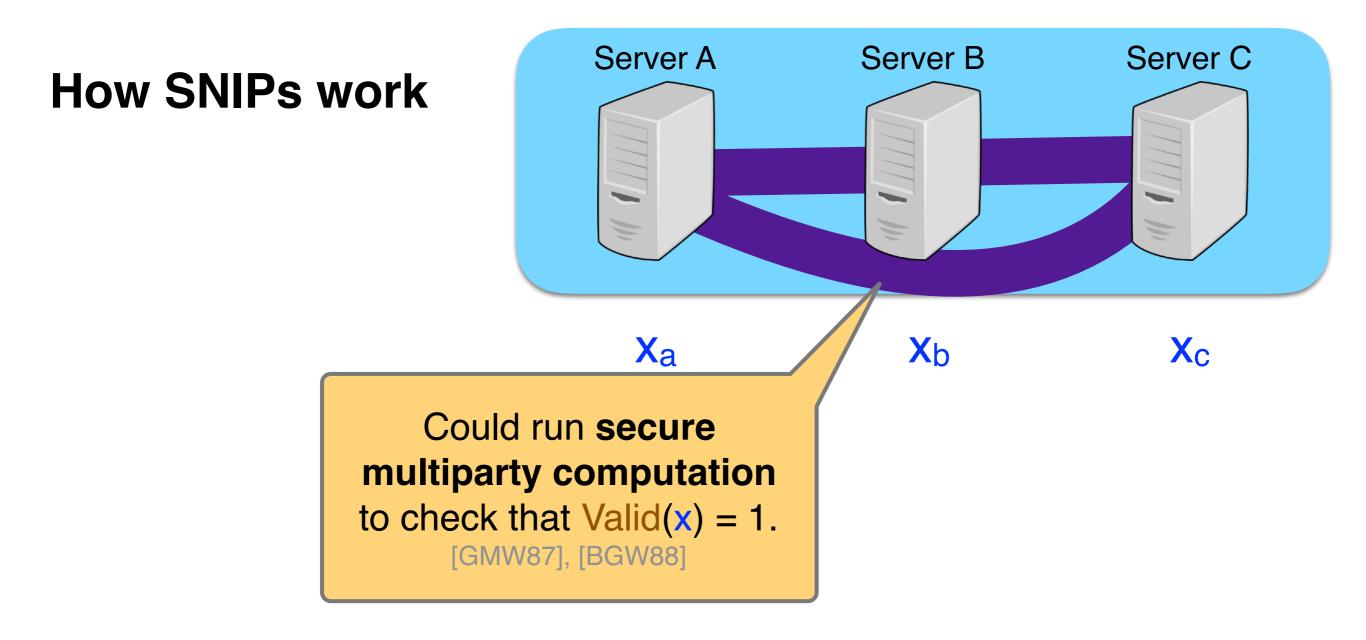
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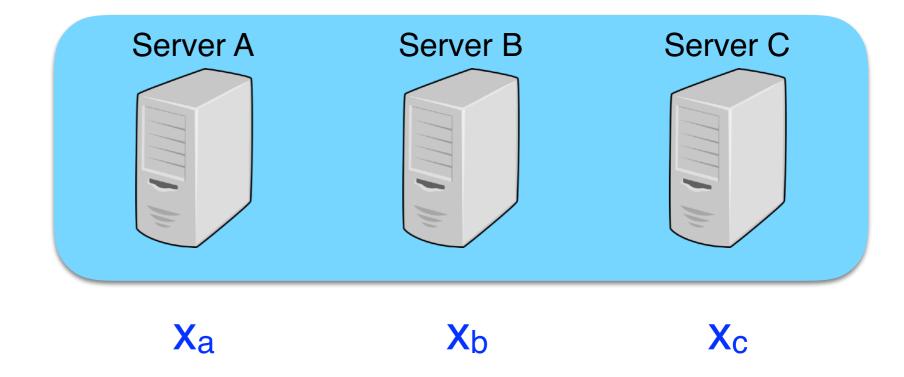
How SNIPs work







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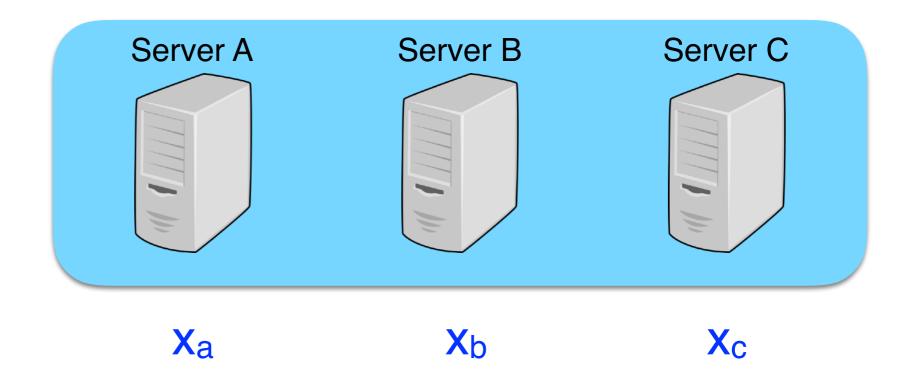


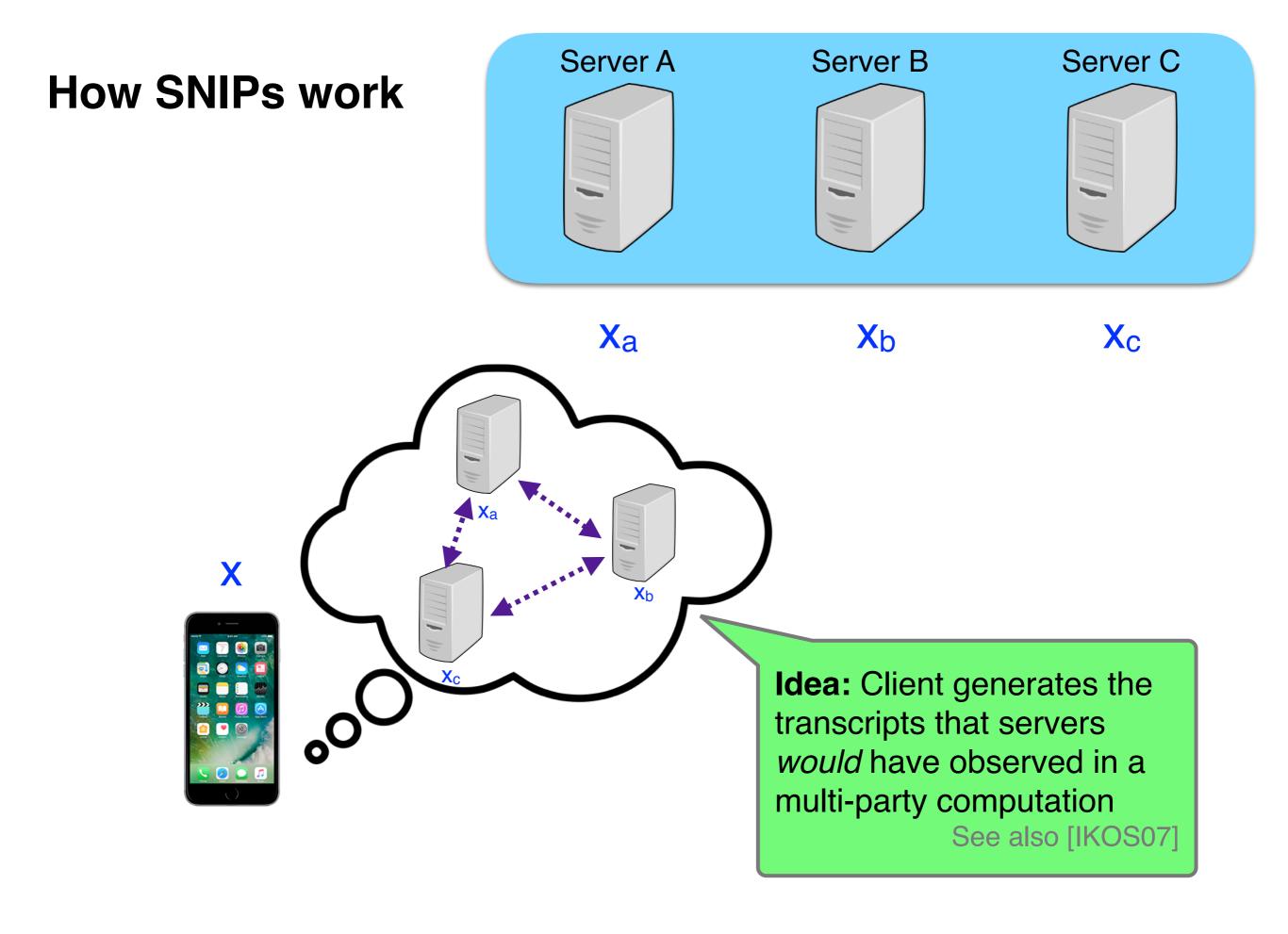
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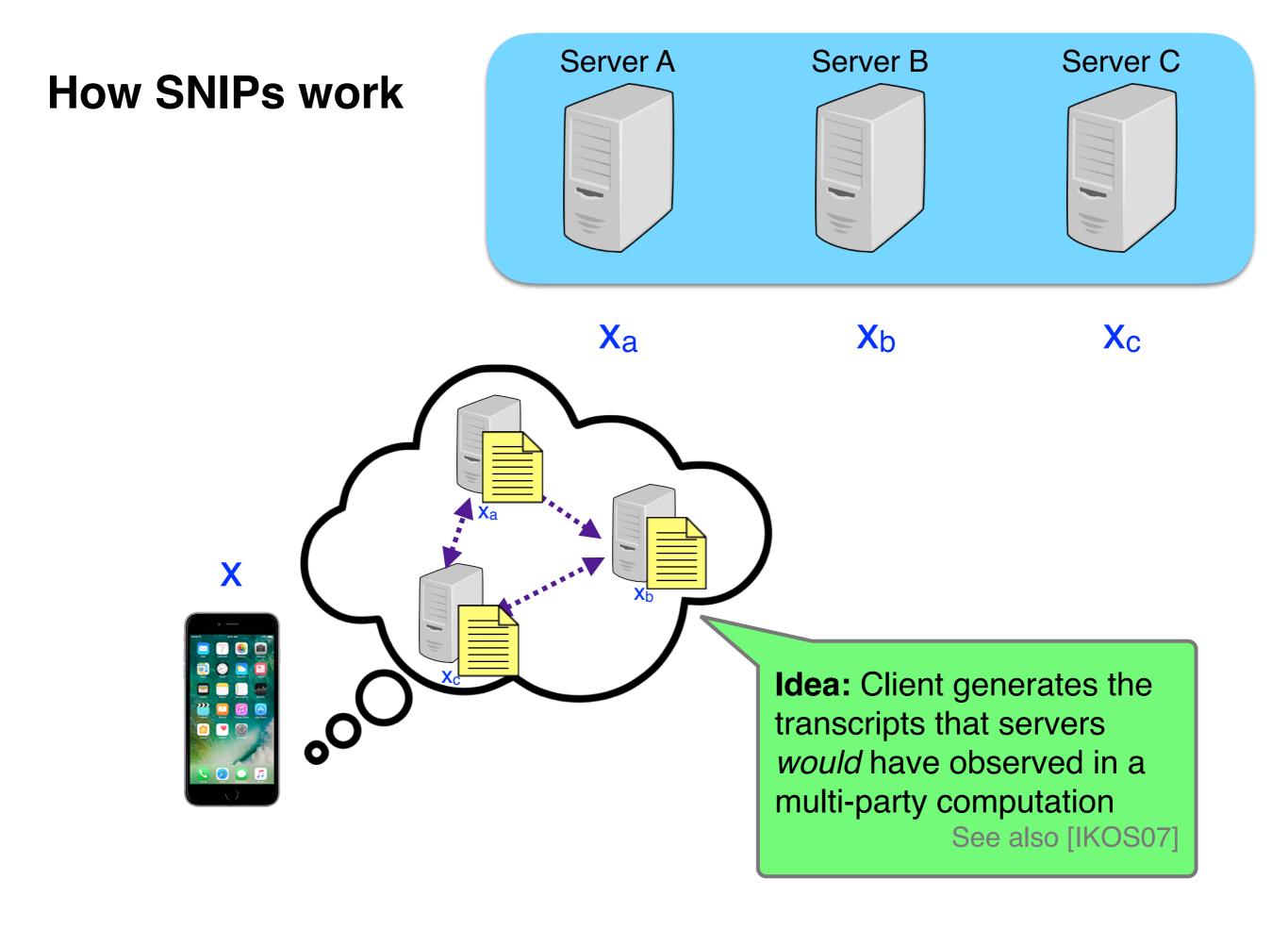


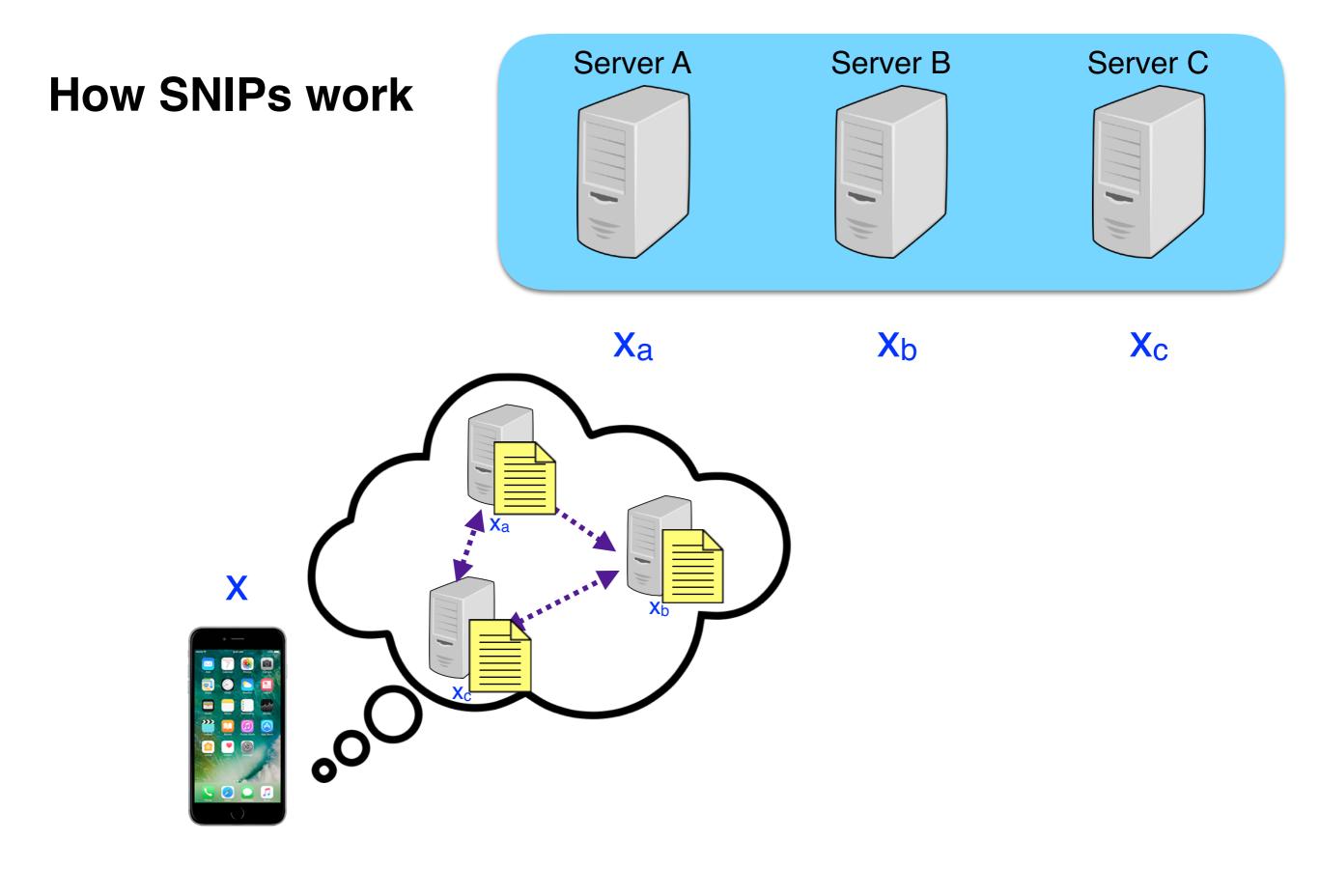
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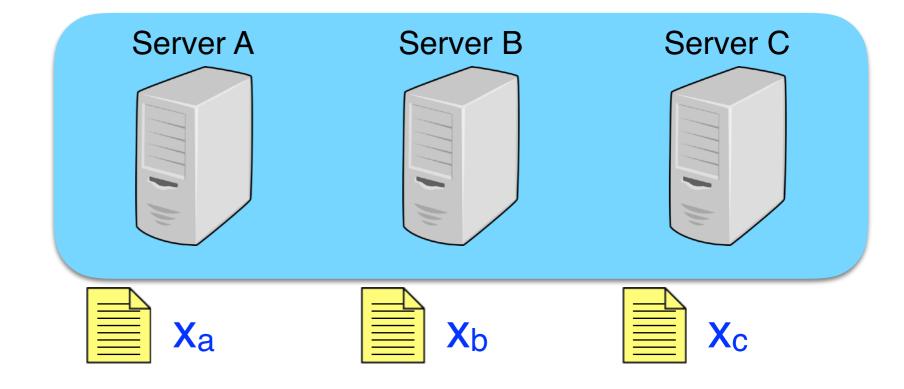
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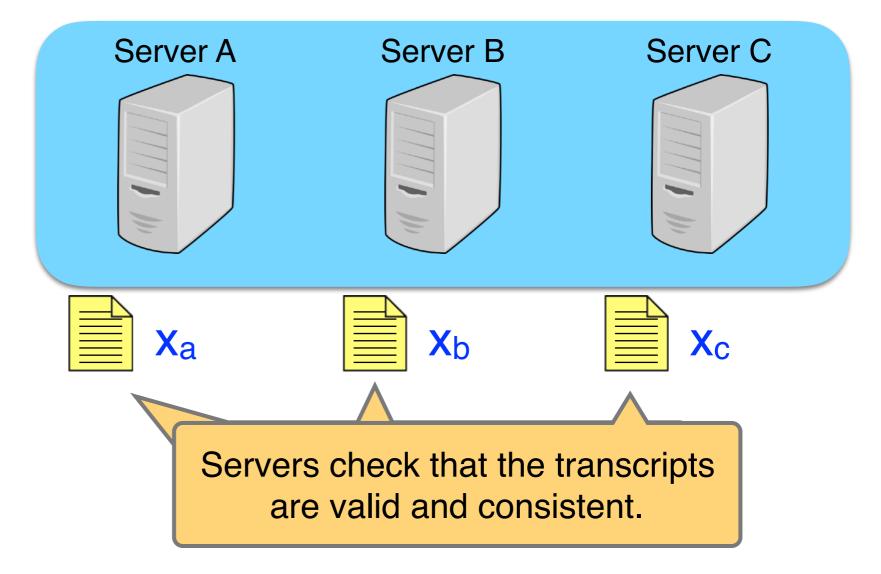






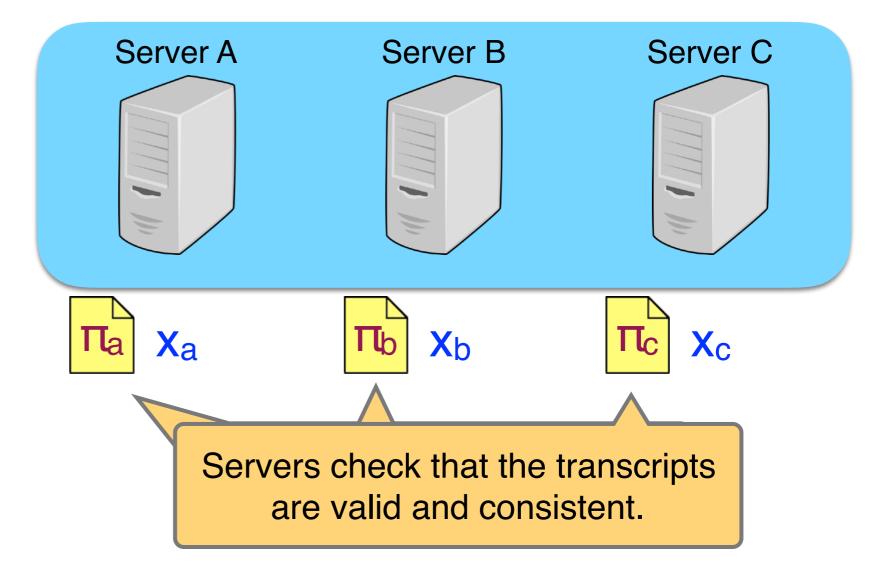






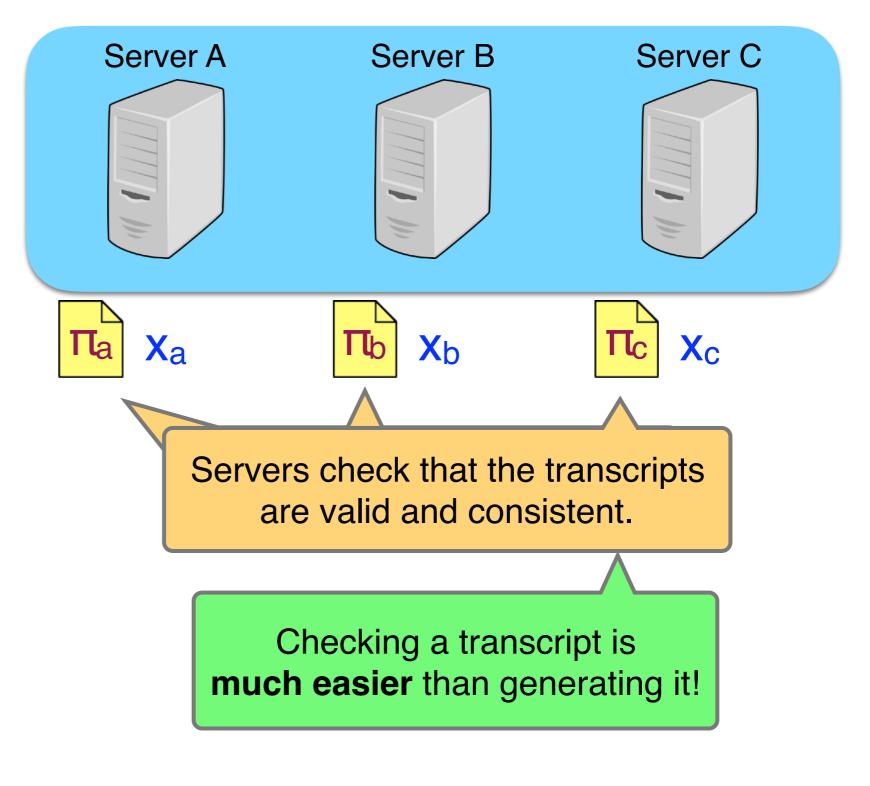
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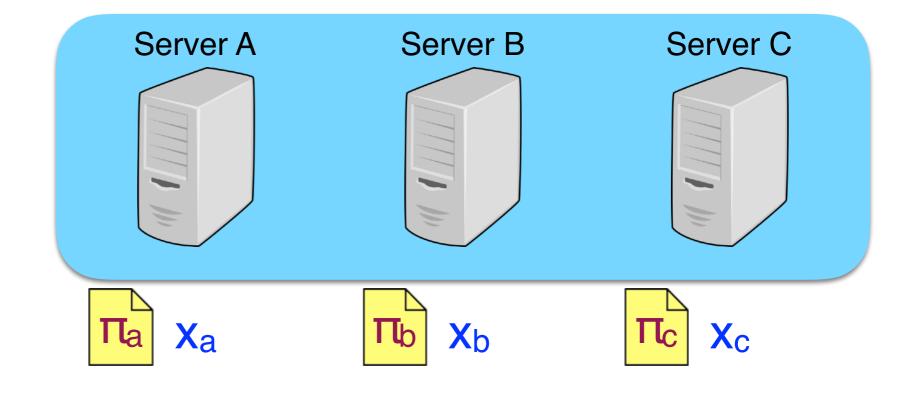
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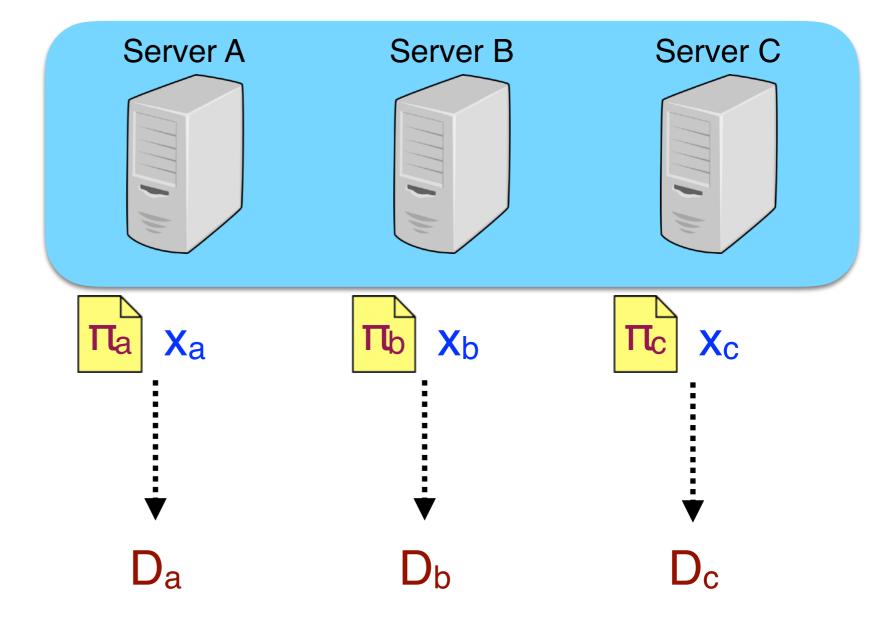


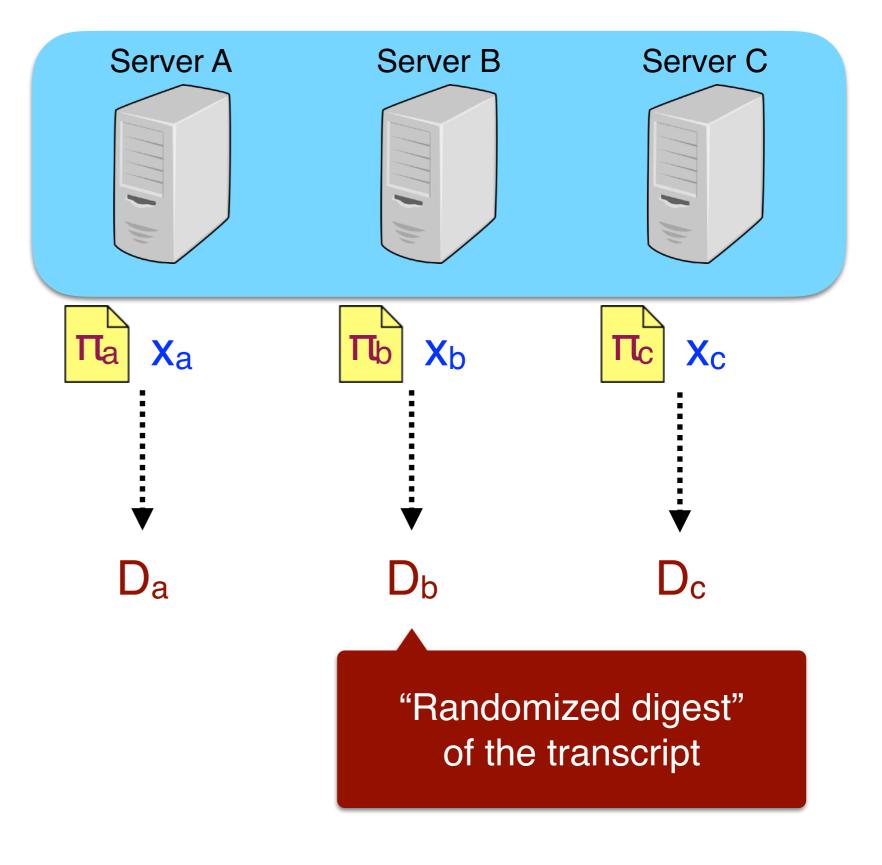


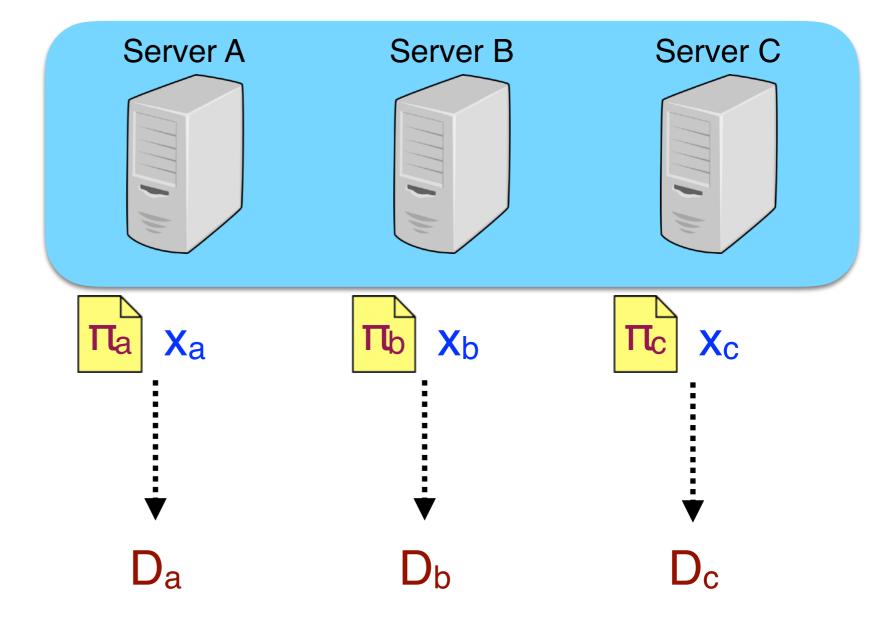
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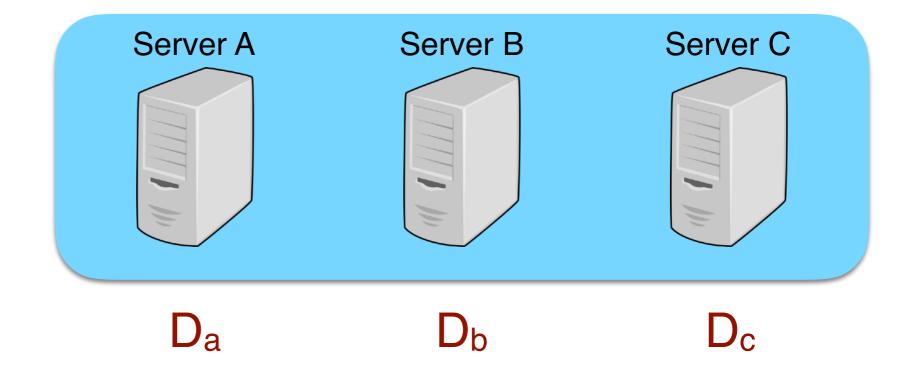


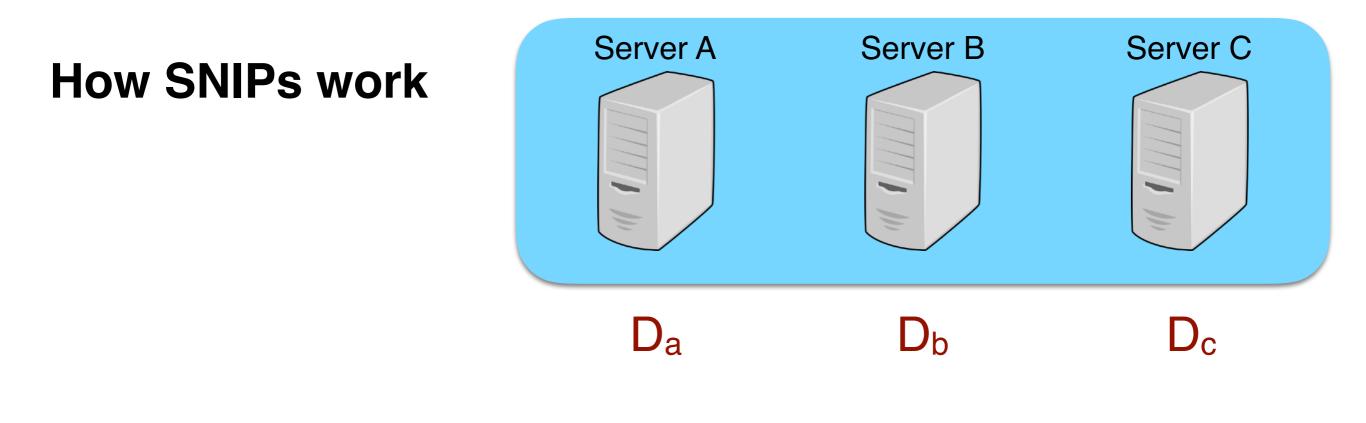




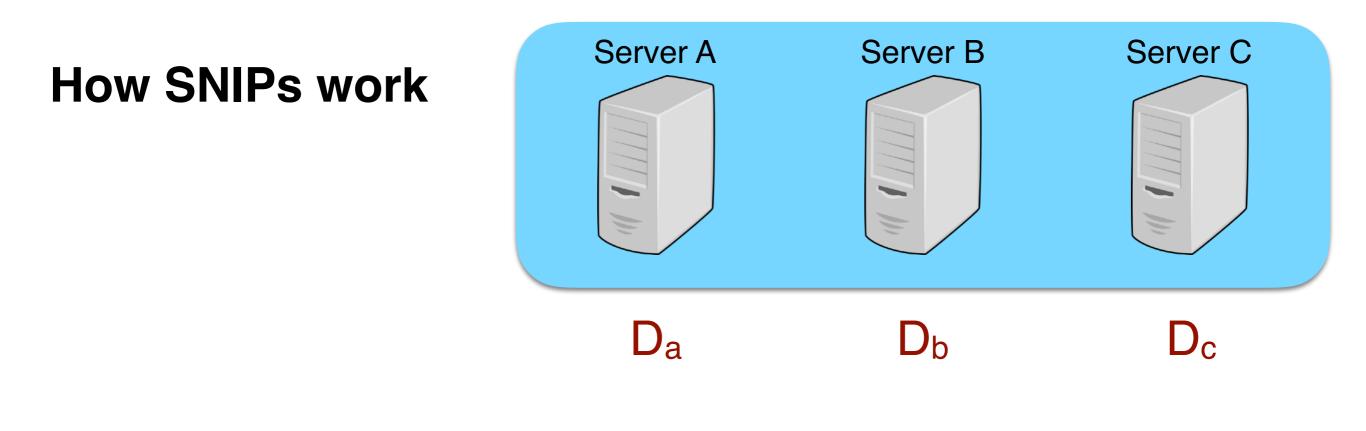








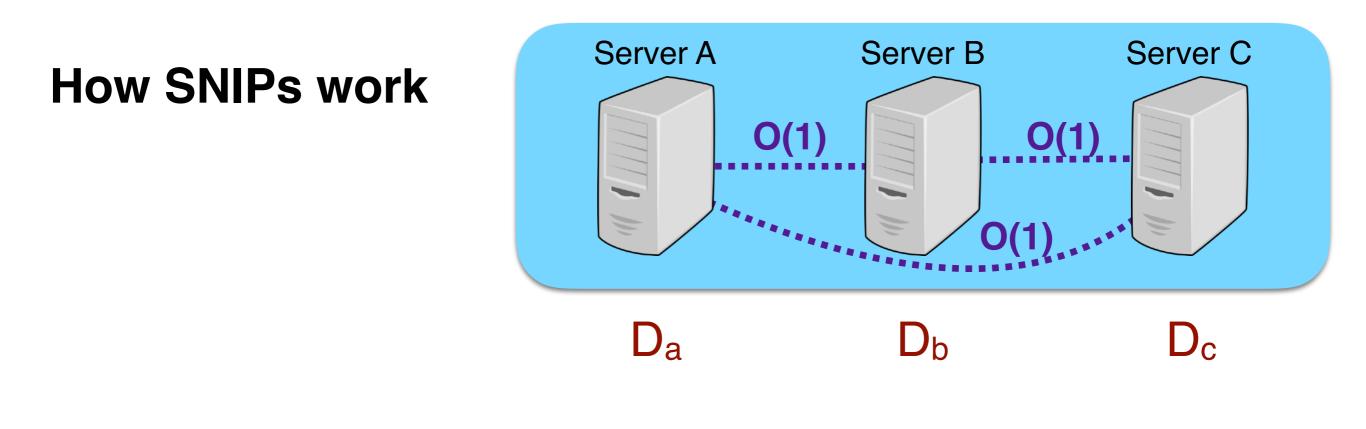




- If x is valid, $D_a + D_b + D_c = 0$
- If x is invalid, $D_a + D_b + D_c \neq 0$ with high probability

Servers run lightweight multi-party computation to check that $D_a + D_b + D_c = 0$

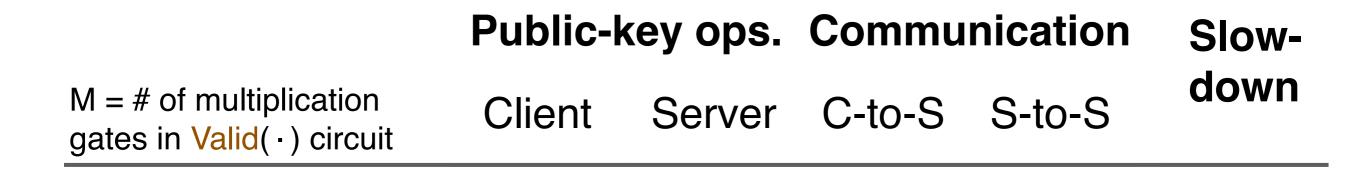
If so, servers accept x is valid.

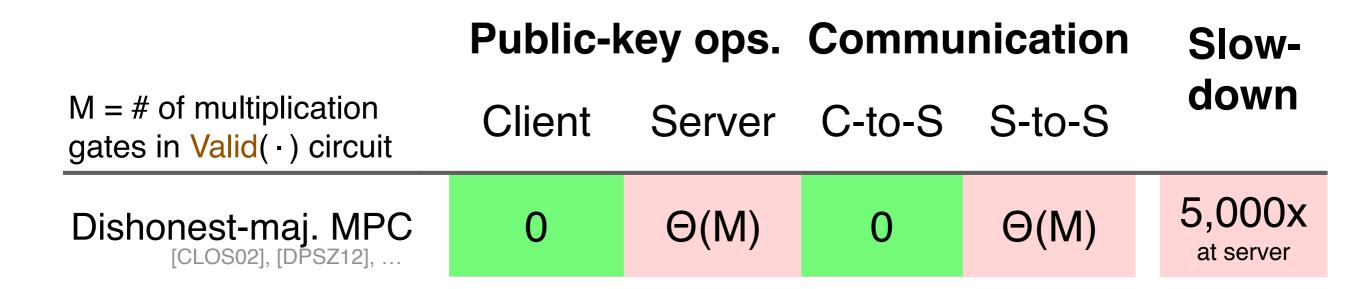


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$M = #$ of multiplication gates in Valid(\cdot) circuit	Client	Server	C-to-S	S-to-S	down
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For specific Valid() circuits, it is possible to eliminate this cost [BGI16]

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From sums to more complex aggregates

If you can compute private sums, you can compute many other interesting aggregates

[PrivStats11], [KDK11], [DFKZ13], [PrivEx14], [MDD16], ...

- Average
- Variance
- Standard deviation
- Most popular (approx)
- "Heavy hitters" (approx)
- Min and max (approx)
- Quality of arbitrary regression model (R²)
- Least-squares regression
- Stochastic gradient descent [Bonawitz et al. 2016]

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- A straw-man solution for private sums
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E.g., for privately measuring telemetry data.

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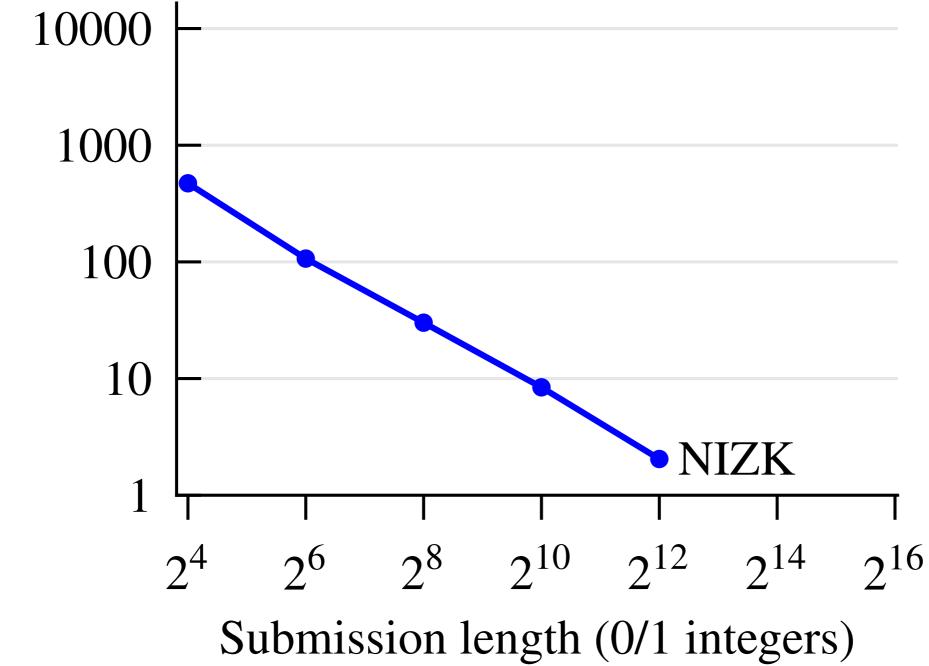


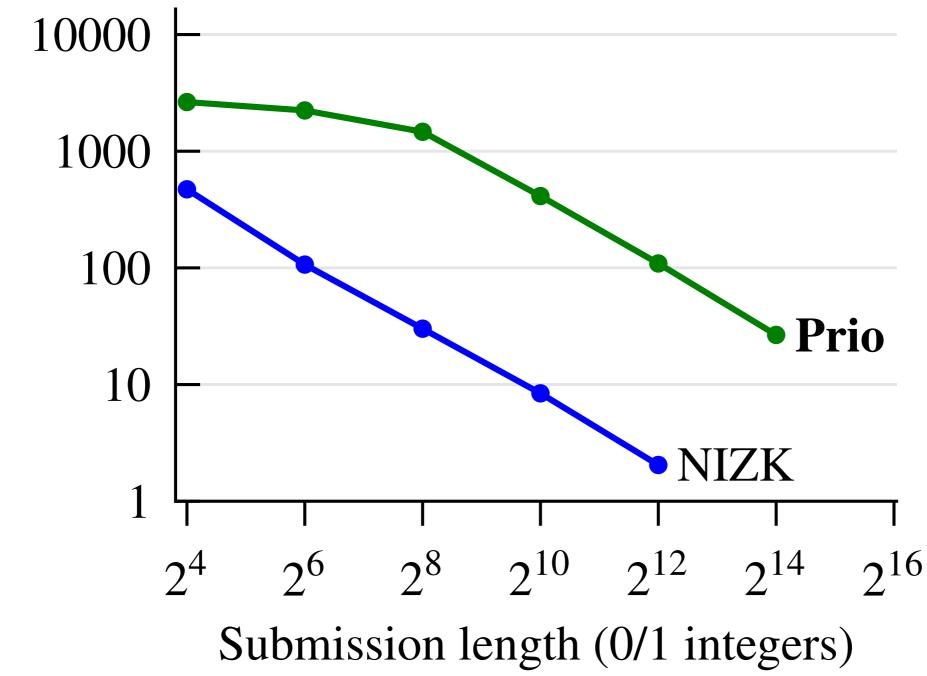
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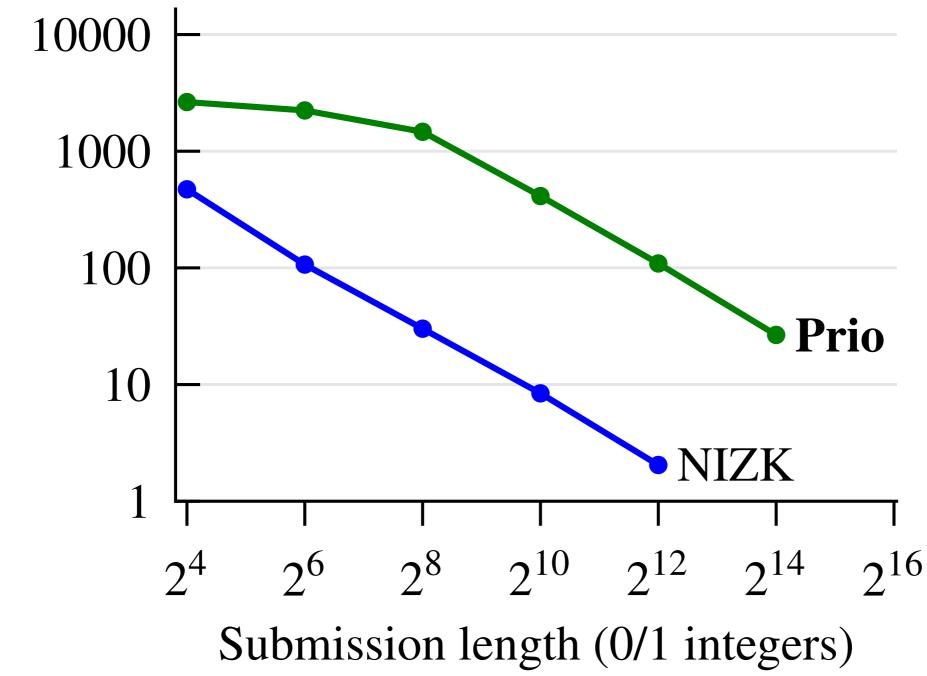
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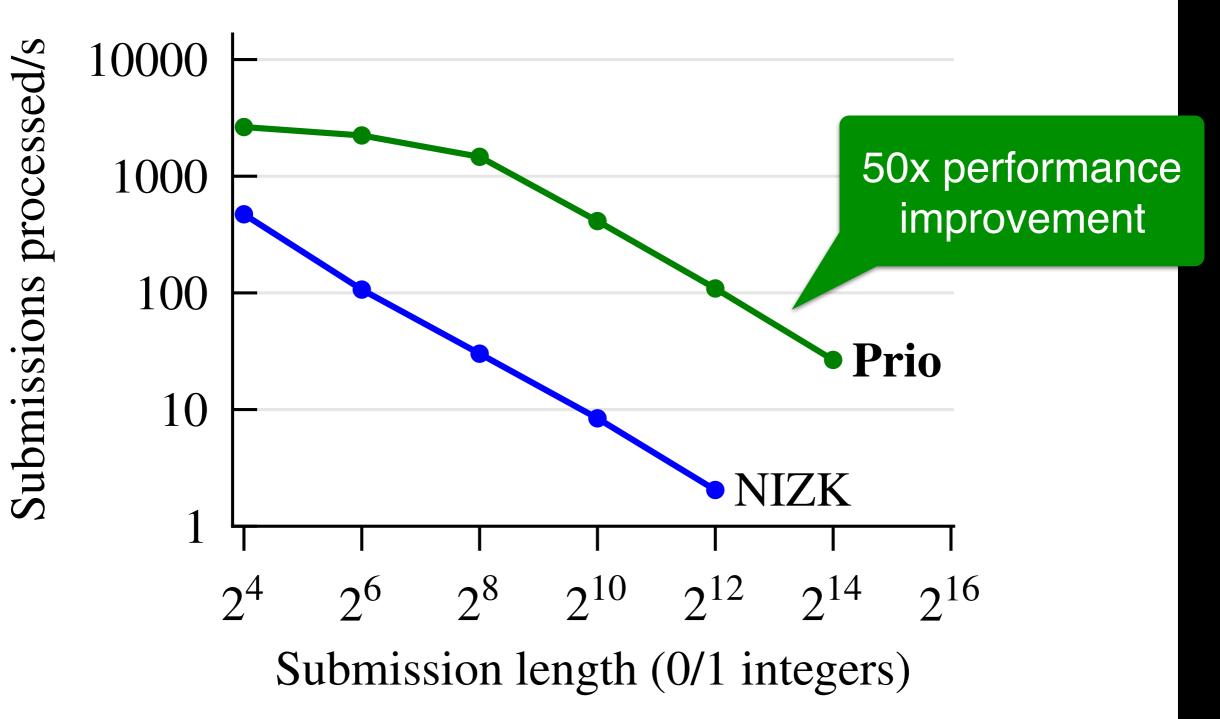
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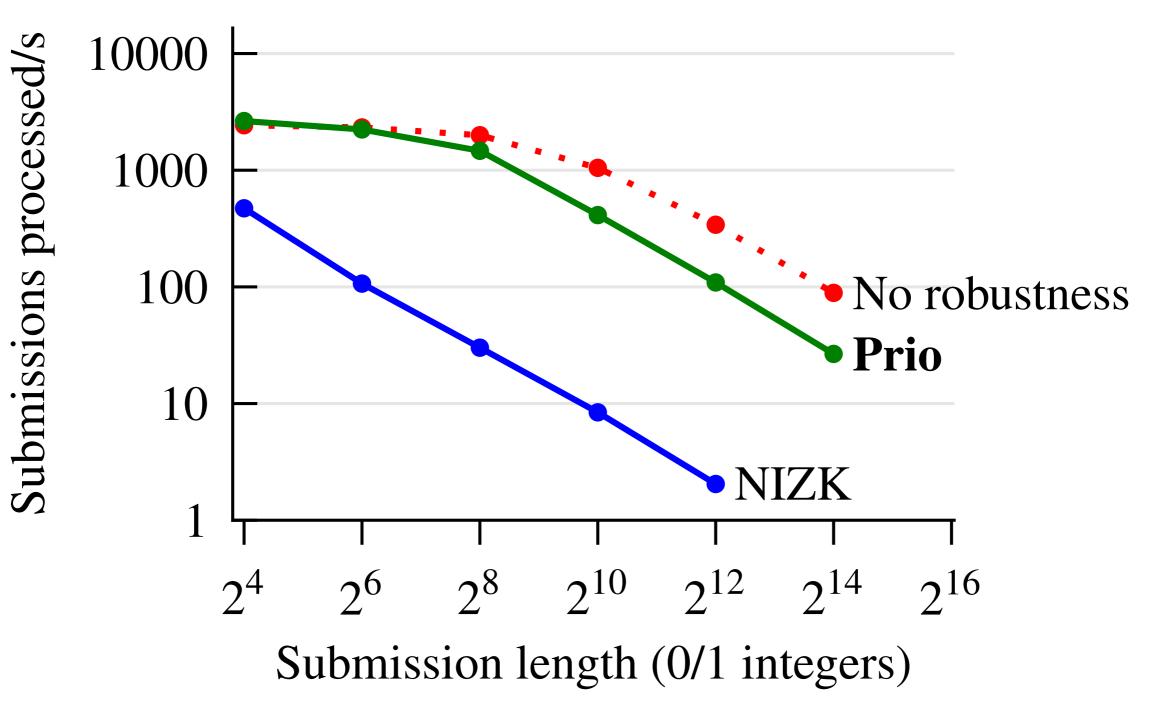


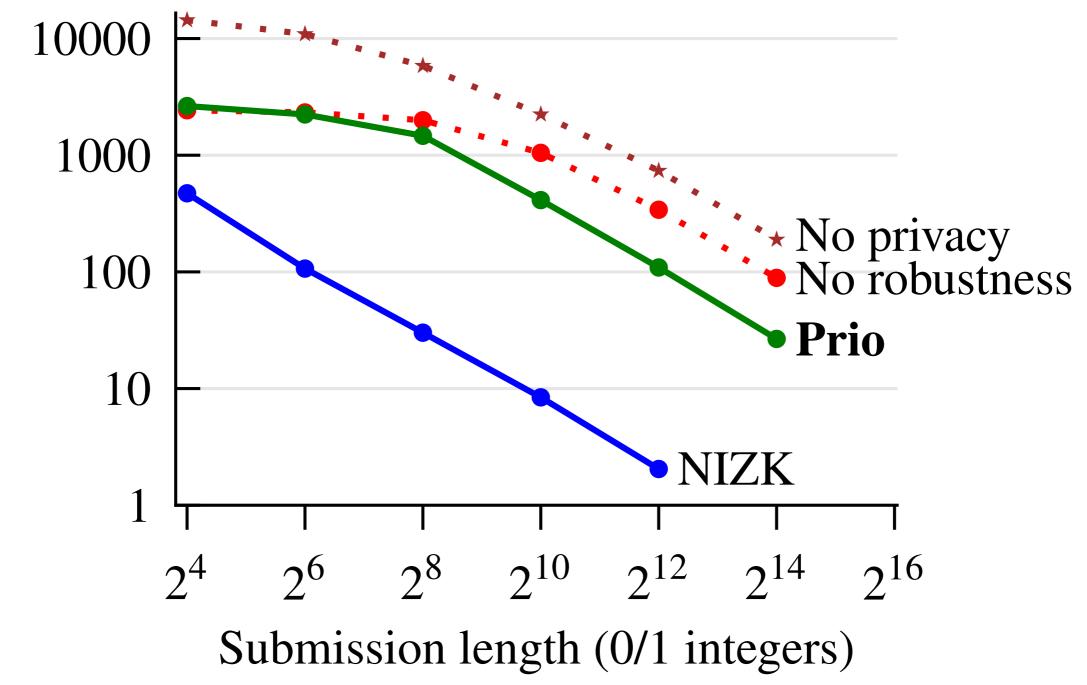


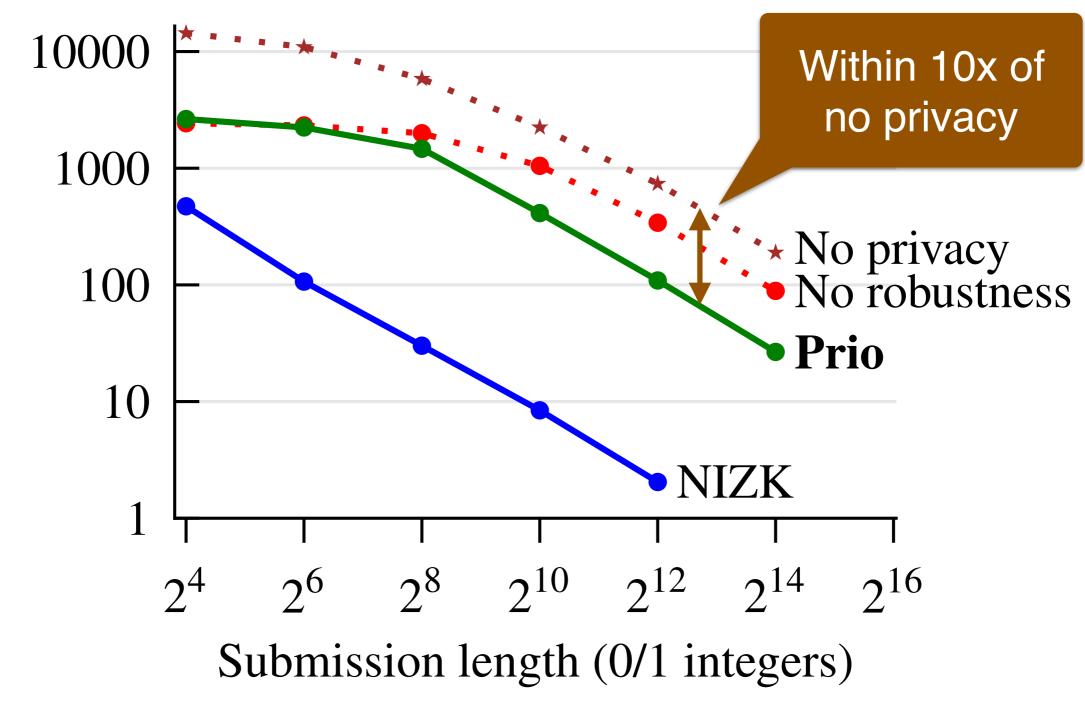












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- Server resources are cheap, client resources are not
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- Need some defense against faulty/disruptive clients
- Privately collecting popular URLs is the interesting application – Existing solutions are good, but not great

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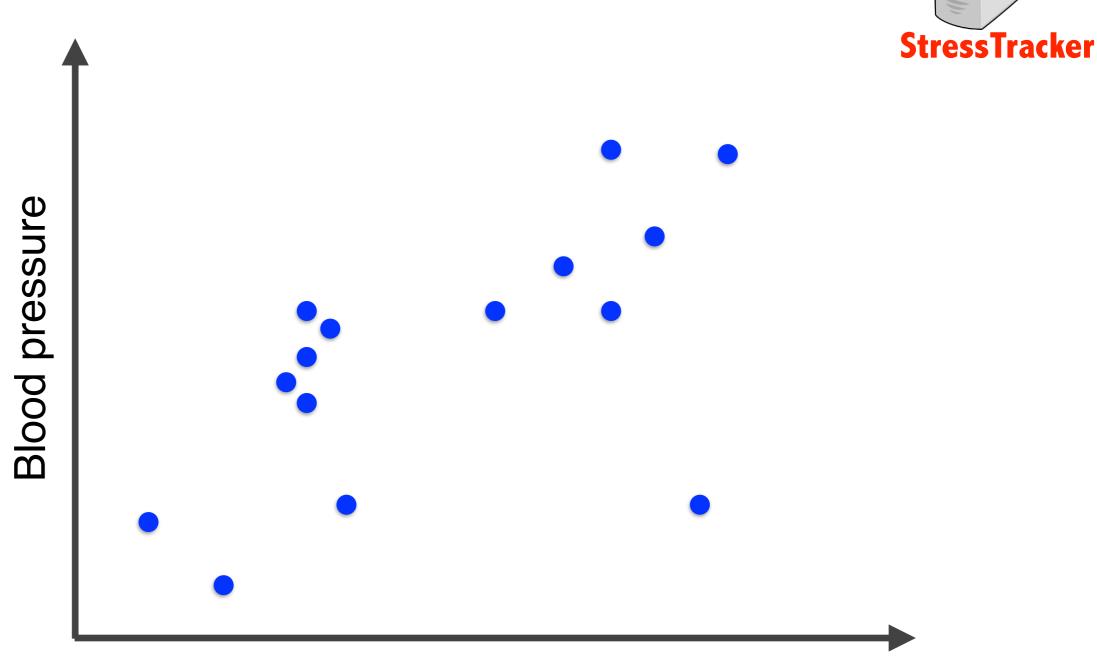
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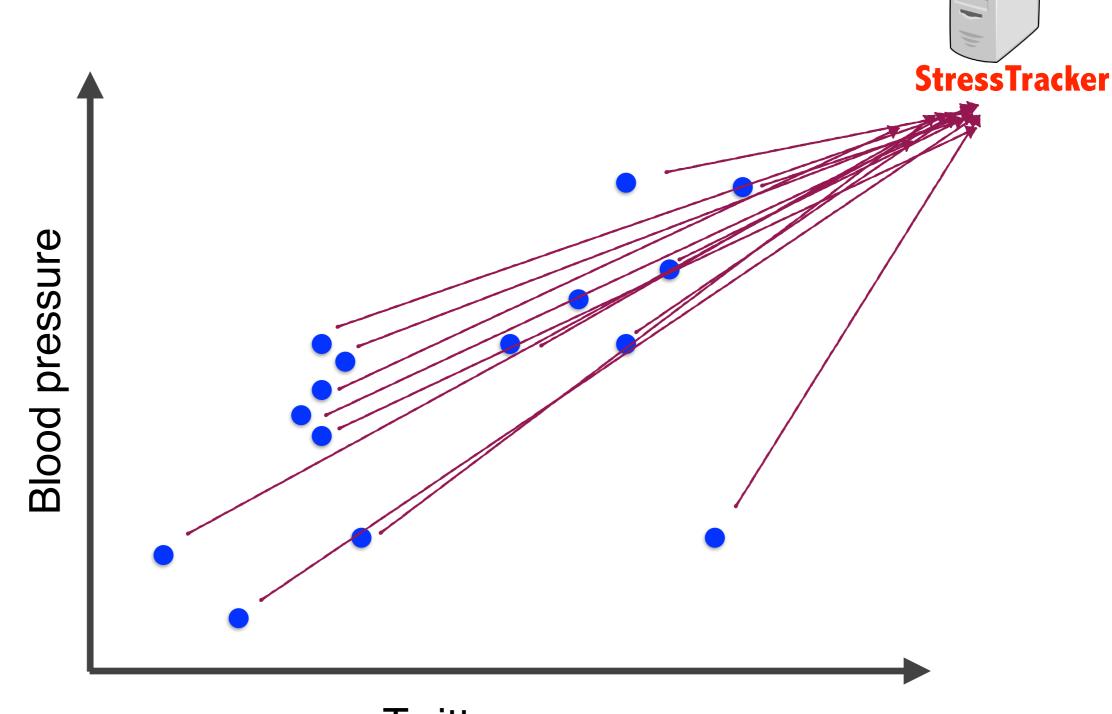
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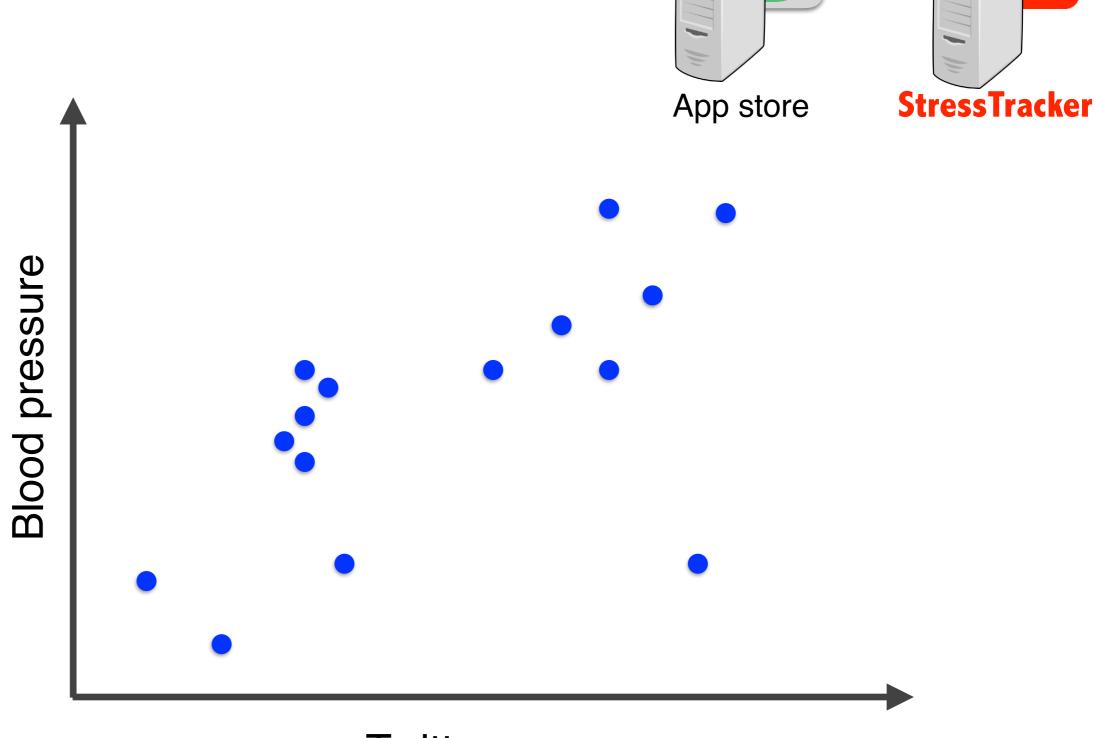
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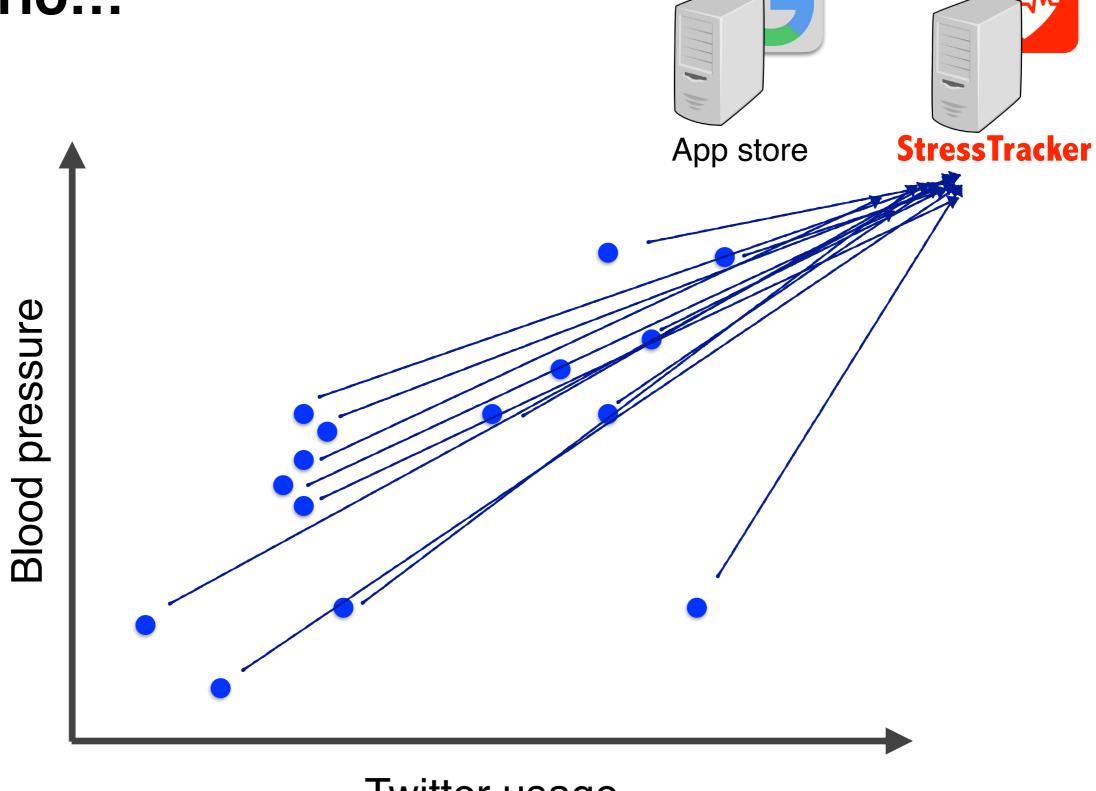
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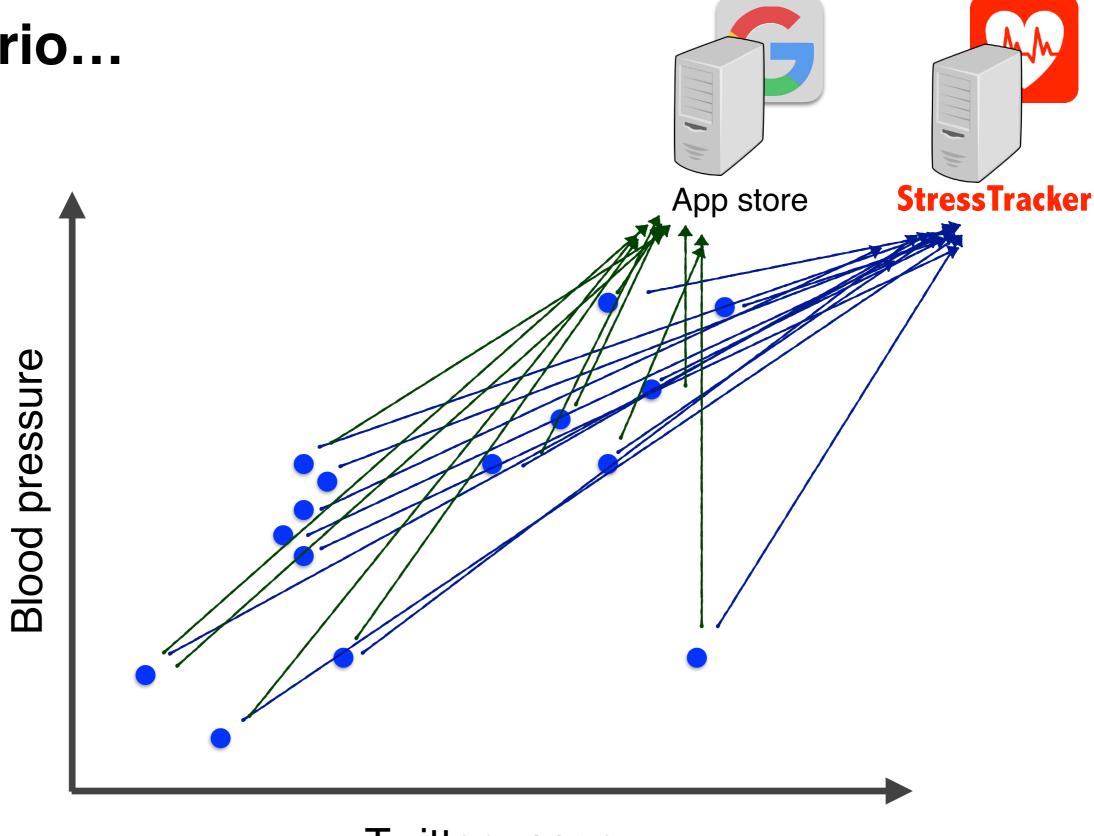
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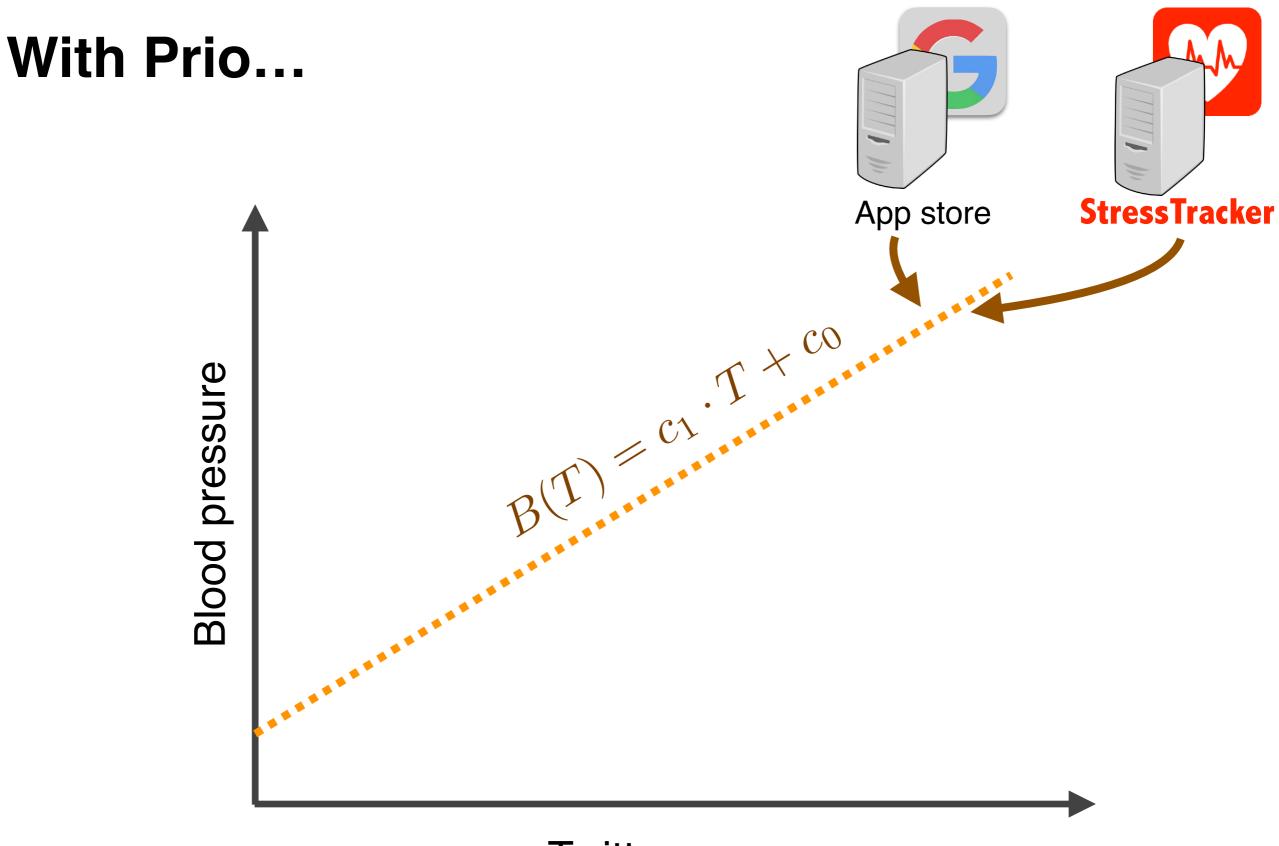


With Prio...



With Prio...





Conclusions

- Wholesale collection of sensitive user data puts our security at risk.
- Prio is the first system for aggregation that provides:
 - exact correctness,
 - privacy,
 - robustness, and
 - efficiency.
- To do so, Prio uses SNIPs and aggregatable encodings.
- These techniques together bring private aggregation closer to practical.

Thank you!

Henry Corrigan-Gibbs henrycg@cs.stanford.edu

https://crypto.stanford.edu/prio/