



Utilizing Large-Scale Randomized Response at Google: RAPPOR and its lessons

Úlfar Erlingsson, Vasyli Pihur, Aleksandra Korolova,
Steven Holte, **Ananth Raghunathan**, Giulia Fanti,
Ilya Mironov, Andy Chu

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RAPPOR Motivation: Hijacking of Chrome Settings

Find the Chrome homepages/search-engines used by clients
... with privacy for each user

I.e., find popularity %'s of
Yahoo! Search, Bing, ...

Also: detect unusually high %'s for
sites installing unwanted software

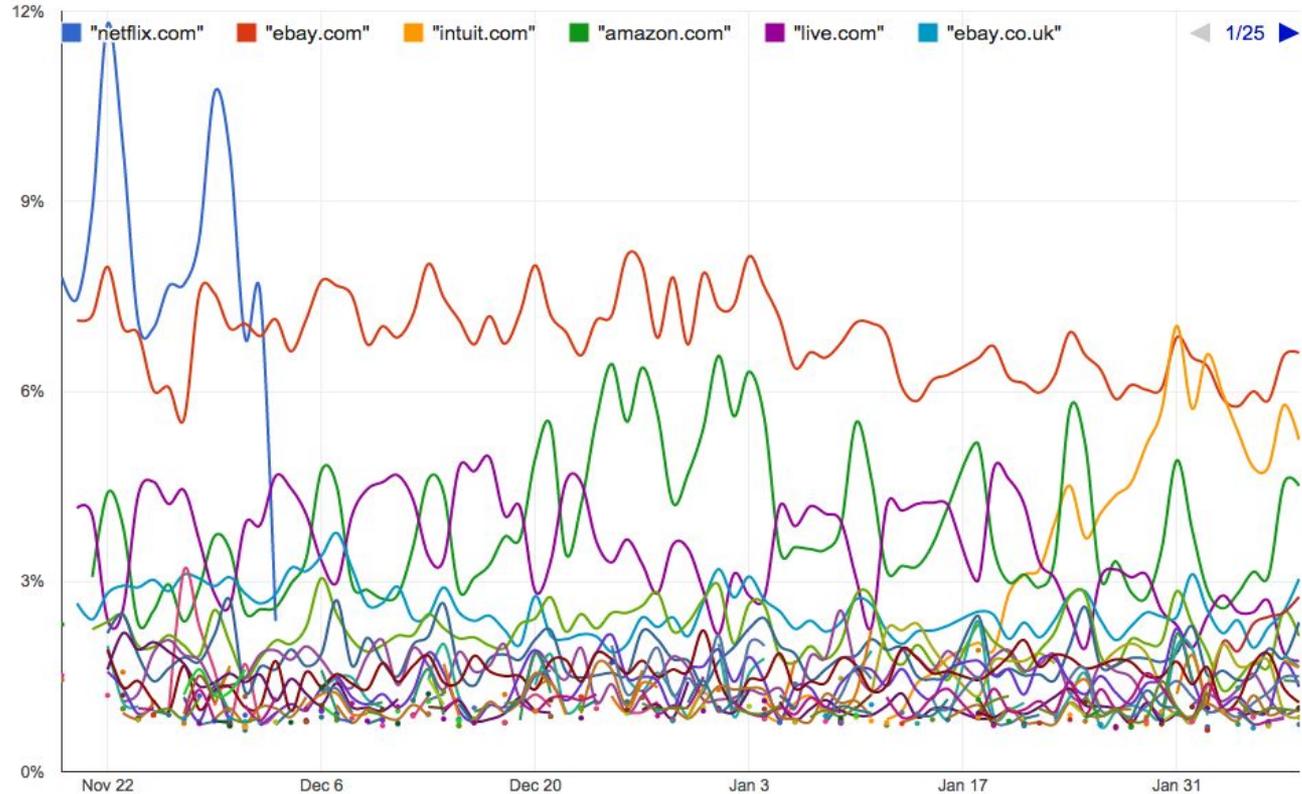
RAPPOR can find them, without
seeing any user's homepage!



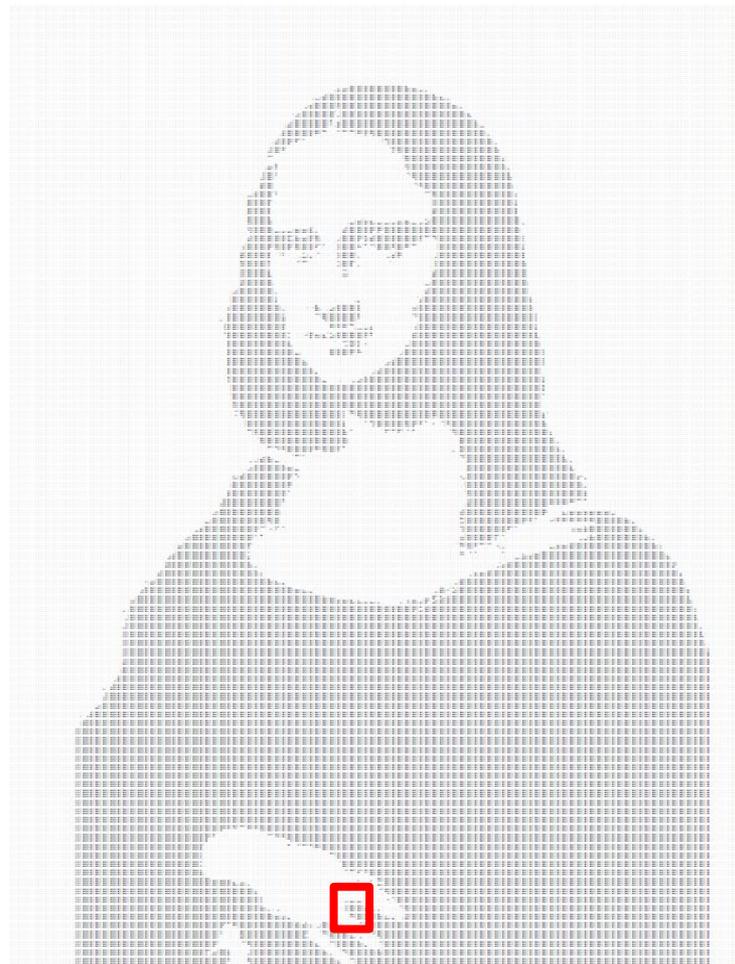
Who on the Web is still using Silverlight?

*Estimated by
RAPTOR*

netflix
ebay
intuit
amazon
live



Metaphor for RAPPOR



Microdata: An individual's report

Each bit is flipped with probability 25%



```
.....M.....MM.M.....MMM.M..
.....MM...MMMM...
...M..MM.MM..MMM.M.MM.M...M..MM..
.MM.....MMM.....MMMMMMMMMM...M...MM
.M...M.....MM..MMMMMMMM...M...
M.....M..MM.MMMMMMMMMMMMMMMMMM...M
.....M.....M.M.M.MMMMMM...MMMMM...
...M.....M.MM.M.MM..M..M..MM.MMMMM
M...M.M.....M.M..M..MMM.MMMMM.MMMM
.MMM.M.....M.M.M.....MMMMMMMMMM.M
```

Big picture remains!



Best practice for learning statistics about users/clients

- **Collect** user data (perhaps with unique id for each user)
- **Scrub** IP addresses, timestamps, etc., from user data

- **Keep central database** of scrubbed data (e.g., for 2 weeks)
 - Keep only aggregates for older data
- **Report aggregates of data over a threshold** (e.g., 10 users)

Can be the best approach (e.g., for opt-in, low-sensitivity data)

RAPPOR: Learn user statistics with much stronger privacy

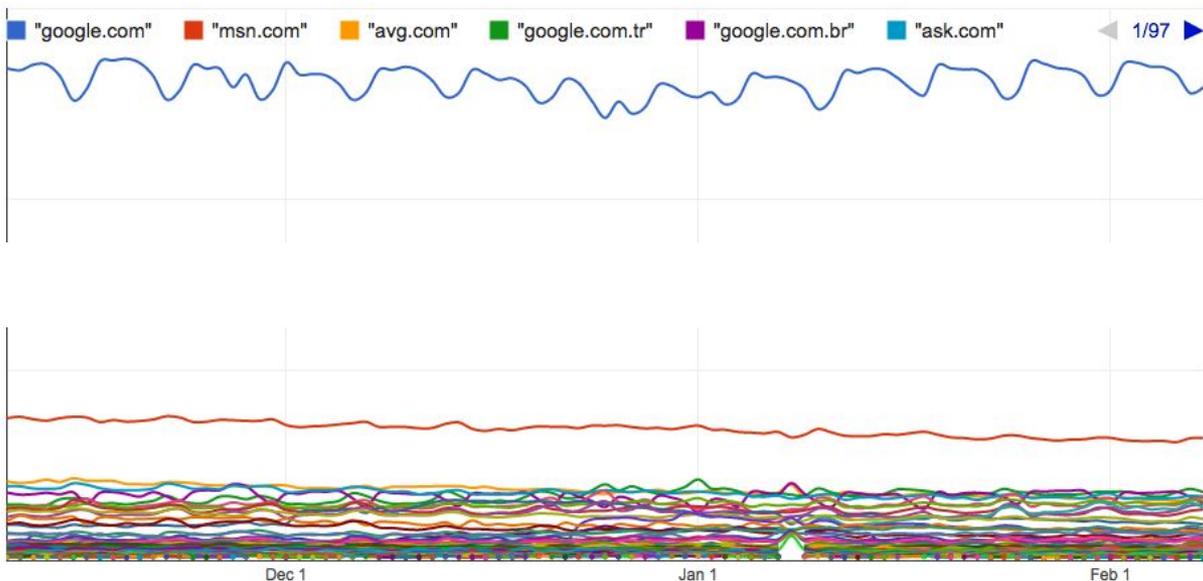
- **Rigorous and meaningful privacy guarantees** for each user
- **No central database** (hackable, subpoenaable) of user data
- User's privacy **doesn't depend on a trusted third party**
- **No privacy externalities** (e.g., from trackable user IDs)

Well-suited to sensitive user data, such as URLs from users

Dashboard at [redacted]

Chrome homepages (over 90 days)

Estimated proportions



google

msn

avg

google tr

google br

Gold Standard of Security

Same key aspects in software construction & computer security

In programming

Specification

=

In security

Security policy

Implementation

=

Enforcement mechanism

Correctness

=

Assurance

Methodology*

=

Security model

* e.g., **functional vs. declarative vs. imperative programming**

Gold Standard of Privacy

Same key aspects in software construction & computer security

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=

=

=

In privacy

Privacy policy

Enforcement mechanism

Assurance

Privacy model*

* e.g., **HIPAA vs. usage control vs. local- or database-differential privacy**

Takeaways from this talk

1. **Randomized response**

Learning categorical data and aggregating Bloom filters

2. **RAPPOR's 2-level randomized response**

Longitudinal differential privacy and anonymity

3. Lessons learnt from the large-scale deployment of a randomized-response privacy mechanism

4. Follow-up works

1. Randomized Response: Collecting a sensitive Boolean

Developed in 1960's for sensitive surveys

“Are you now, or have you ever been, a member of the communist party?”

- a. Flip a coin, **in private**
- b. If coin comes up heads, respond “Yes”
- c. If coin comes up tails, tell the truth

Estimate true “Yes” ratio with: “Yes”% - 50%

1. Randomized Response: Collecting a sensitive Boolean

Developed in 1960's for sensitive surveys

“Are you now, or have you ever been, a member of the communist party?”

- a. Flip a coin, **in private**
- b. If coin comes up heads,
--- flip another coin to select randomly “Yes” or “No”
- c. If coin comes up tails, tell the truth

Satisfies differential privacy property (with two coins)

Still easy to estimate true “Yes” ratio

Randomized response on categorical Boolean values

- If number of categories is small, can do an independent randomized response for each category
 - Bit-by-bit array of randomized responses

0	1	0	1	1	1	0	0	0	0	0	1	0	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

- Example: The categories may refer to salary ranges
 - Users do a “yes/no” randomized response for each range

0	1	0	1	1	1	0	0	0	0	0	1	0	1	0	0	1	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

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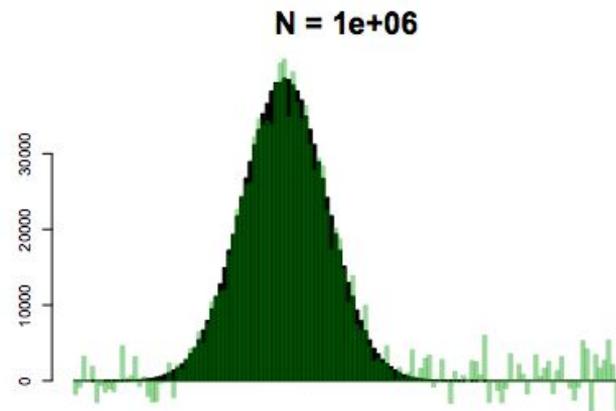
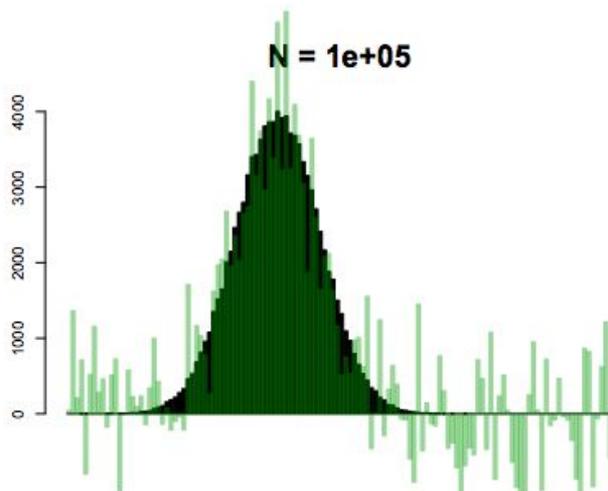
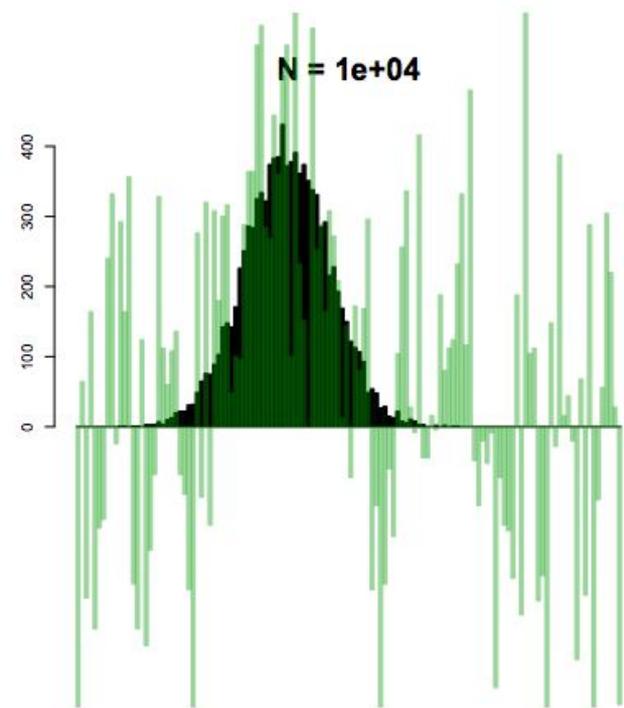
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---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

**This user's salary lies in this range.
The “Yes” coin came up heads, so bit is “1”.**

Learning the shape of the Salaries distribution

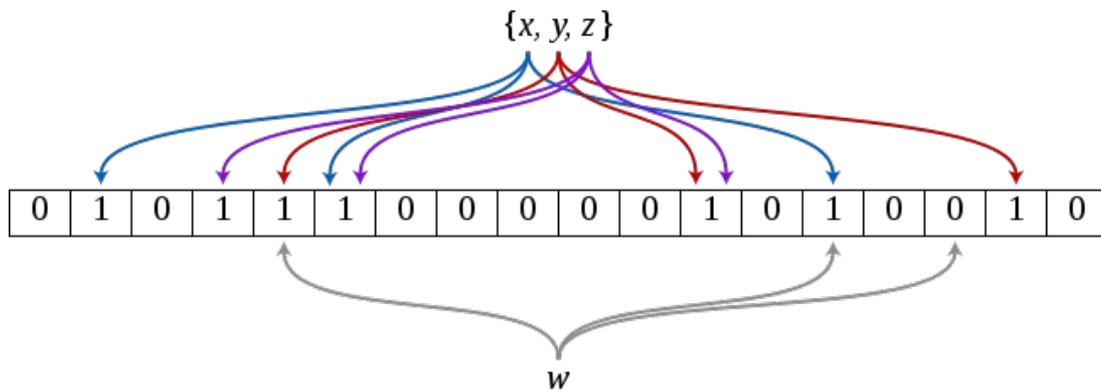


Users flip a “yes” coin for just one bit;
“no” coins for others

No prior knowledge of the shape of the distribution.

Bloom filters to handle large sets of categories

- Compressed representation of a large set



- To minimize collisions/false positives, use multiple cohorts
 - Randomly assign clients to one of m cohorts
 - Each cohort uses different Bloom-filter hash functions

2. RAPPOR two-level randomization and differential privacy

- Problem to ask the communist question repeatedly
 - Average of coin flips eventually reveals the true answer
- **Memoization** is the trick: Reuse the same answer
- But memoized random bits can hurt anonymity
 - Repeated bit sequence forms a unique tracking ID
- **Randomization of memoized response** is the answer!
 - Flip coins on a value, and memoize
 - Then report coin flips on the memoized data

RAPPOR algorithm

1. Hash a value v into Bloom filter B using h hash functions
2. Memoize a **Permanent Randomized Response** B'

$$B'_i = \begin{cases} 1, & \text{with probability } \frac{1}{2}f \\ 0, & \text{with probability } \frac{1}{2}f \\ B_i, & \text{with probability } 1 - f \end{cases}$$

3. Report an **Instantaneous Randomized Response** S

$$P(S_i = 1) = \begin{cases} q, & \text{if } B'_i = 1. \\ p, & \text{if } B'_i = 0. \end{cases}$$

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$f = 1/2$
for example

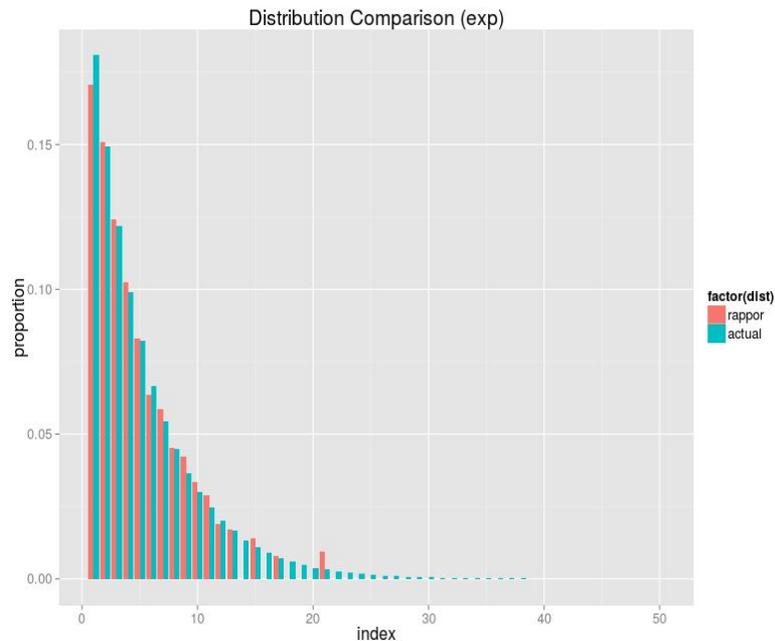
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$q = 3/4$ and $p = 1/2$
for example

OSS project

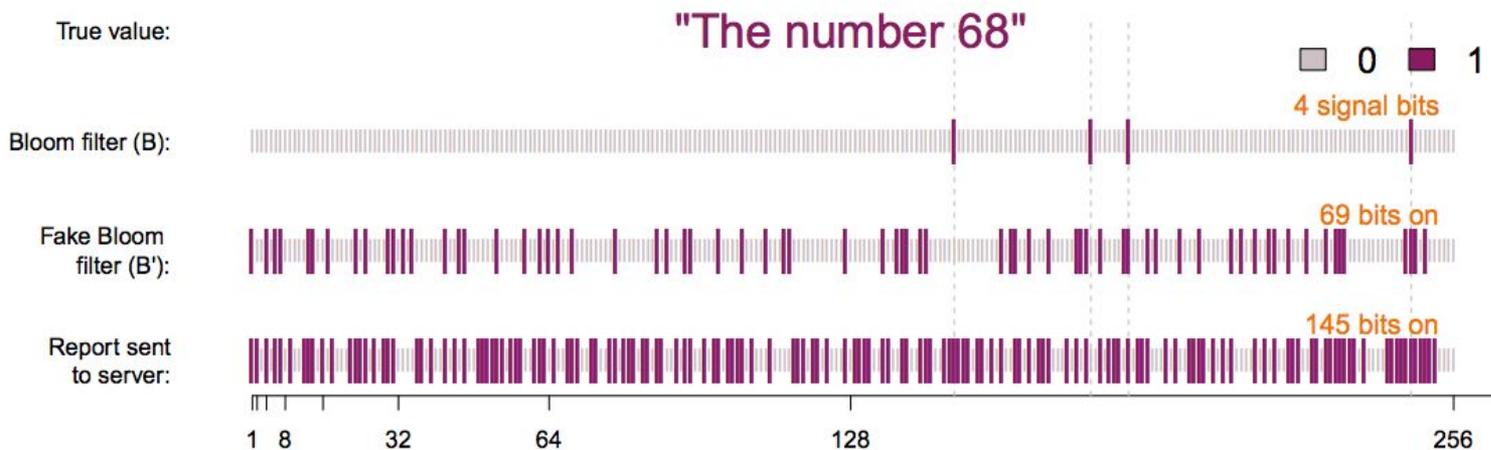
- Contents of <https://github.com/google/rappor>
 - Demo that you can run with a couple shell commands
 - Client library
 - Analysis tools and simulation
 - Documentation
 - Analysis service
 - Clients code in a few languages



Lessons Learnt

Design for simple explainability

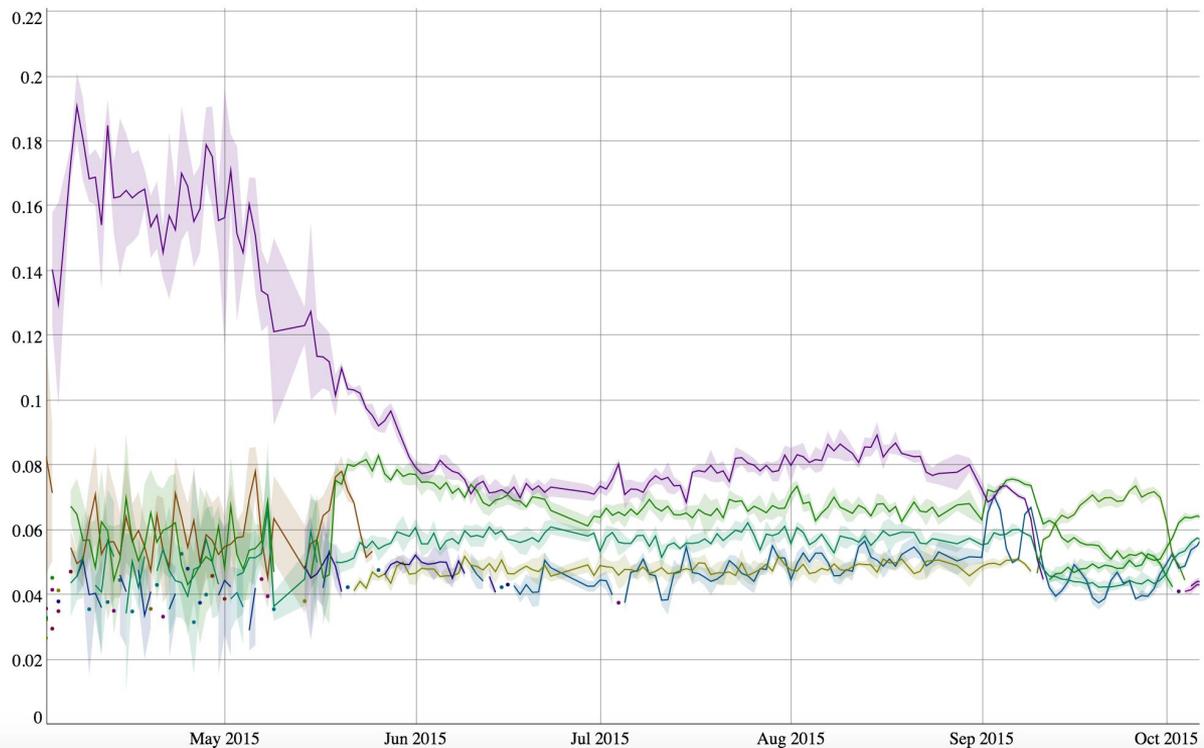
Critical to get comfort / acceptance from **everybody**
... (also need reasonable ϵ , and may want user opt-in)



There will be growing pains

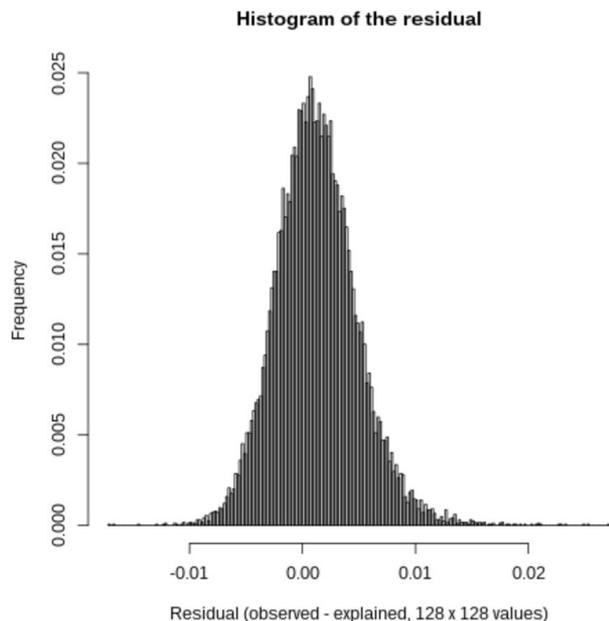
- Transitioning from a research prototype to a real product
- Scalability
- Versioning

Communicate Uncertainty

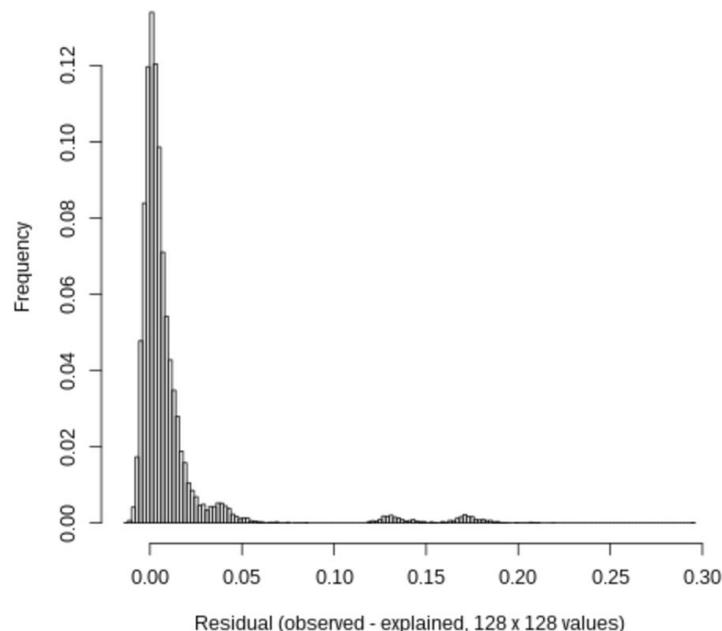


Candidates? – Enable diagnostics on collected data

No missing candidates



Three missing candidates



Know thy Enemies and Friends

If **raw data** is being collected:

- privacy people & technology are a hindrance to utility
 - hard to avoid the slippery slope
- ... bodes ill for (pure) database-differential privacy

If **statistical/privacy-protected data** is collected:

- privacy people become essential to utility
 - big step onto the slippery slope
- ... good reason to add noise early

Keep your friends close ...

- Partner closely with the users, and monitor their use
 - `tools/metrics/rappor/rappor.xml` - `chromium/src`
- Avoid users treating your technology as a black box
 - they'll be disappointed & affect user privacy w/o utility
- Set and manage expectations
 - e.g., local differential privacy can only see peaky tops

The world depends on trust; we can't do without it

- Google provides data for Chrome and RAPPOR!
- The ϵ for RAPPOR's are just worst-case fallbacks
 - ... do much better, unless Google explicitly chooses evil
- But, without trust, those ϵ only allow seeing peaky tops
- Need to work on better basis for combining trust with privacy
 - E.g., via technical and contractual separation of concerns
 - Backed by verifiable enforcement teeth

Follow-up Works

- Giulia Fanti, Vasyl Pihur, Úlfar Erlingsson, “Building a RAPPOR with the Unknown: Privacy-Preserving Learning of Associations and Data Dictionaries”, PoPETS 2016
 - Two-way contingency tables and recovering missing candidates
- Bassily, Smith, “Local, Private, Efficient Protocols for Succinct Histograms,” STOC 2015
- Kairouz, Bonawitz, Ramage, “Discrete Distribution Estimation under Local Privacy”, <https://arxiv.org/abs/1602.07387>
- Qin et al., “Heavy Hitter Estimation over Set-Valued Data with Local Differential Privacy”, CCS 2016

Follow-up Works

- Abadi, Chu, Goodfellow, McMahan, Mironov, Talwar, Zhang. “Deep learning with differential privacy.” ACM CCS 2016.
- Papernot, Abadi, Erlingsson, Goodfellow, Talwar. “Semi-supervised Knowledge Transfer for Deep Learning from Private Training Data.” ICLR 2017.

Conclusions

RAPPOR – locally differentially-private mechanism for reporting of categorical and string data

- First Internet-scale deployment of differential privacy
- Explainable
- Conservative
- Open-sourced
- Challenging
- ... just the beginning

Thank you!

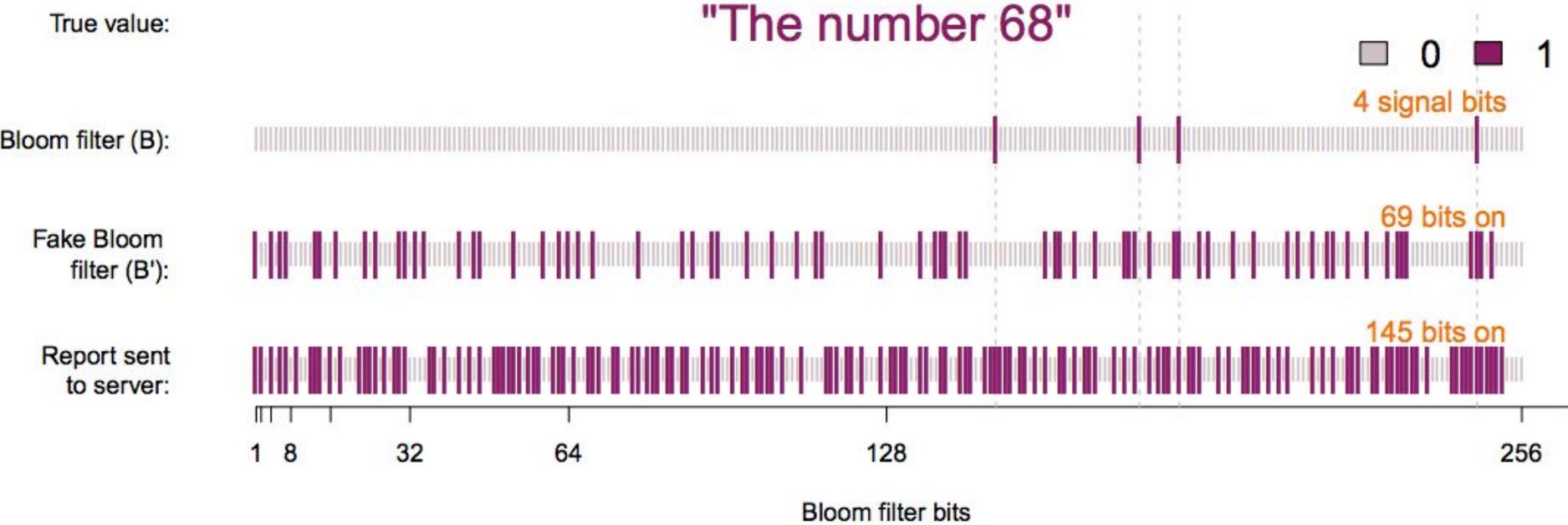
Any questions?

—pseudorandom@google.com—

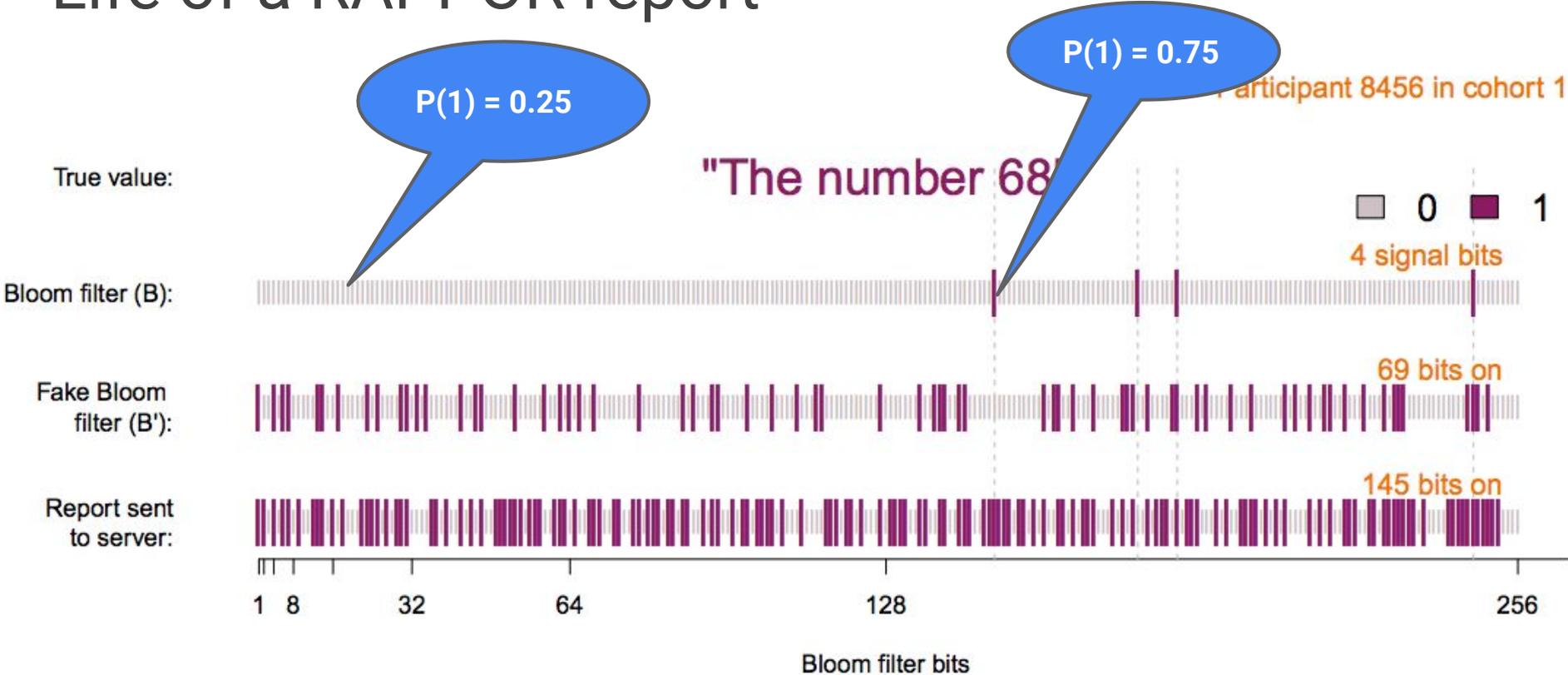
Backup

Life of a RAPPOR report

Participant 8456 in cohort 1

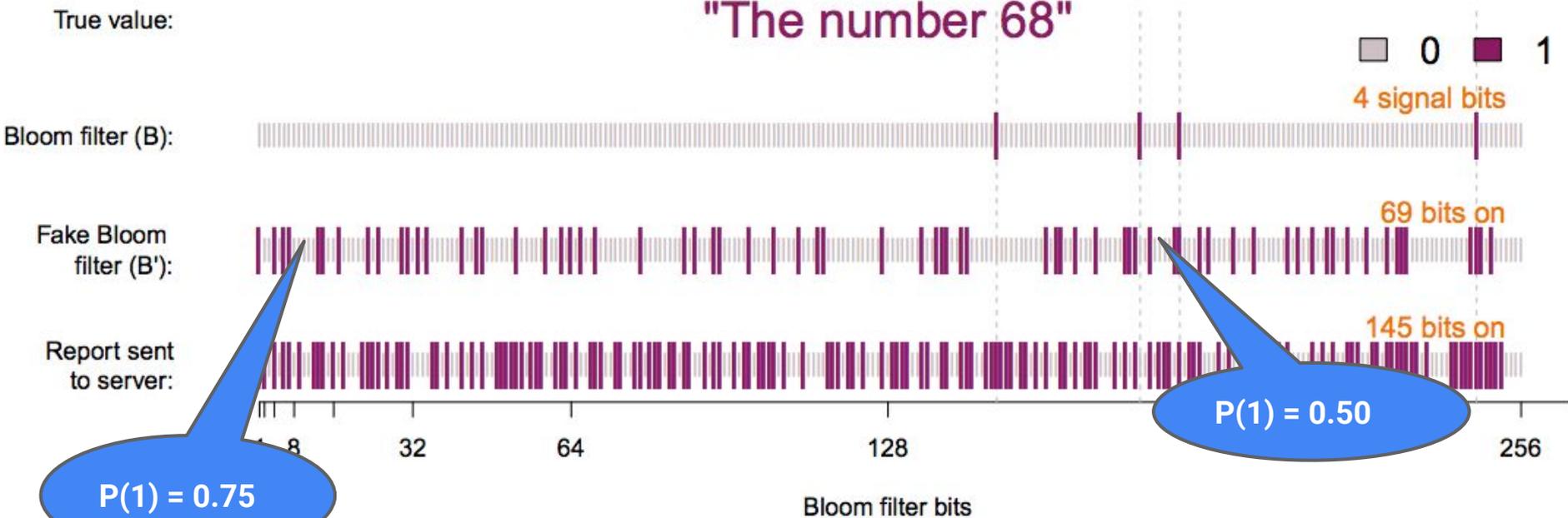


Life of a RAPPOR report



Life of a RAPPOR report

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Differential Privacy of RAPPOR

- **Permanent Randomized Response** satisfies differential privacy at

$$\epsilon_{\infty} = 2h \ln \left(\frac{1 - \frac{1}{2}f}{\frac{1}{2}f} \right)$$

- **Instantaneous Randomized Response** has differential privacy at

$$\epsilon_1 = h \log \left(\frac{q^*(1 - p^*)}{p^*(1 - q^*)} \right)$$

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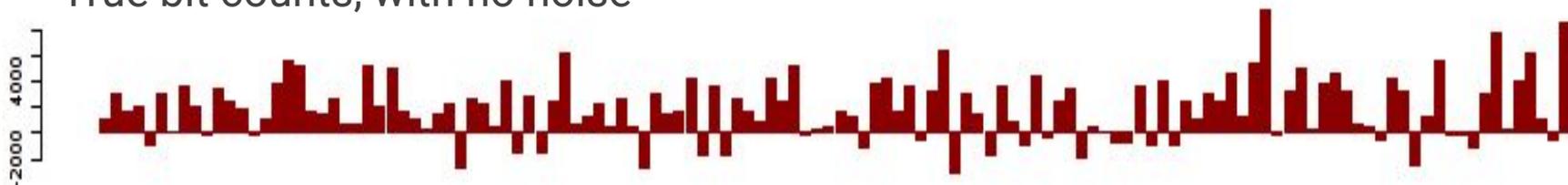
$$\epsilon_{\infty} = 2h \ln \left(\frac{1 - \frac{1}{2}f}{\frac{1}{2}f} \right) = \mathbf{4 \ln(3)}, \text{ for example}$$

- **Instantaneous Randomized Response** has differential privacy at

$$\epsilon_1 = h \log \left(\frac{q^*(1 - p^*)}{p^*(1 - q^*)} \right) \approx \mathbf{\ln(3)}, \text{ for example}$$

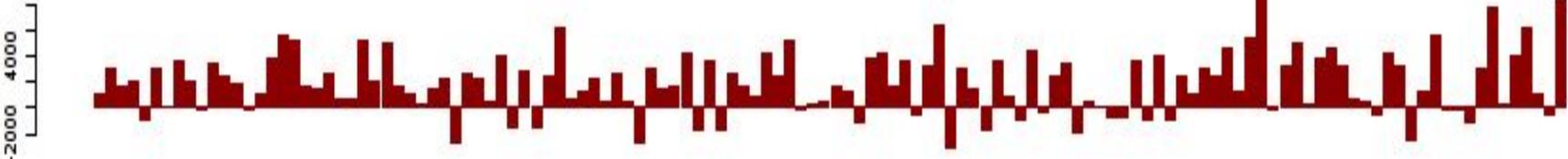
Decoding RAPPOR

True bit counts, with no noise

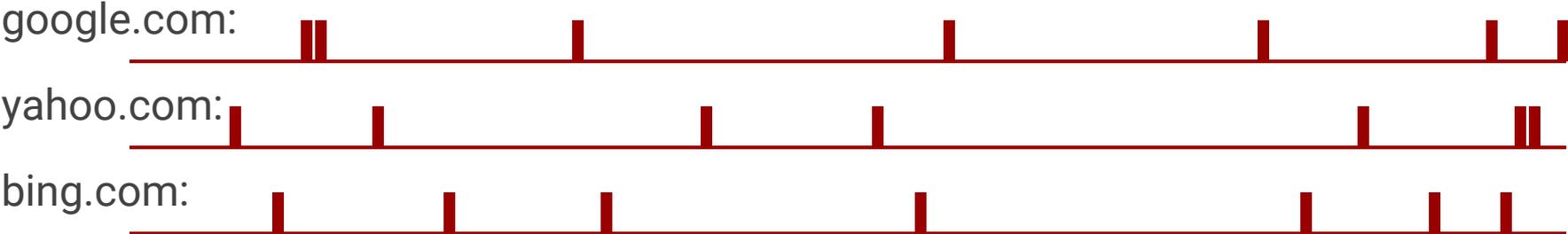


Decoding RAPPOR

True bit counts, with no noise



De-noised RAPPOR reports



From denoised counts to distribution

Linear Regression:

$$\min_X \|B - A X\|_2$$

LASSO:

$$\min_X (\|B - A X\|_2)^2 + \lambda \|X\|_1$$

Hybrid:

1. Find support of X via LASSO
2. Solve linear regression to find weights