

The interval branch-and-prune algorithm for the protein structure determination by NMR

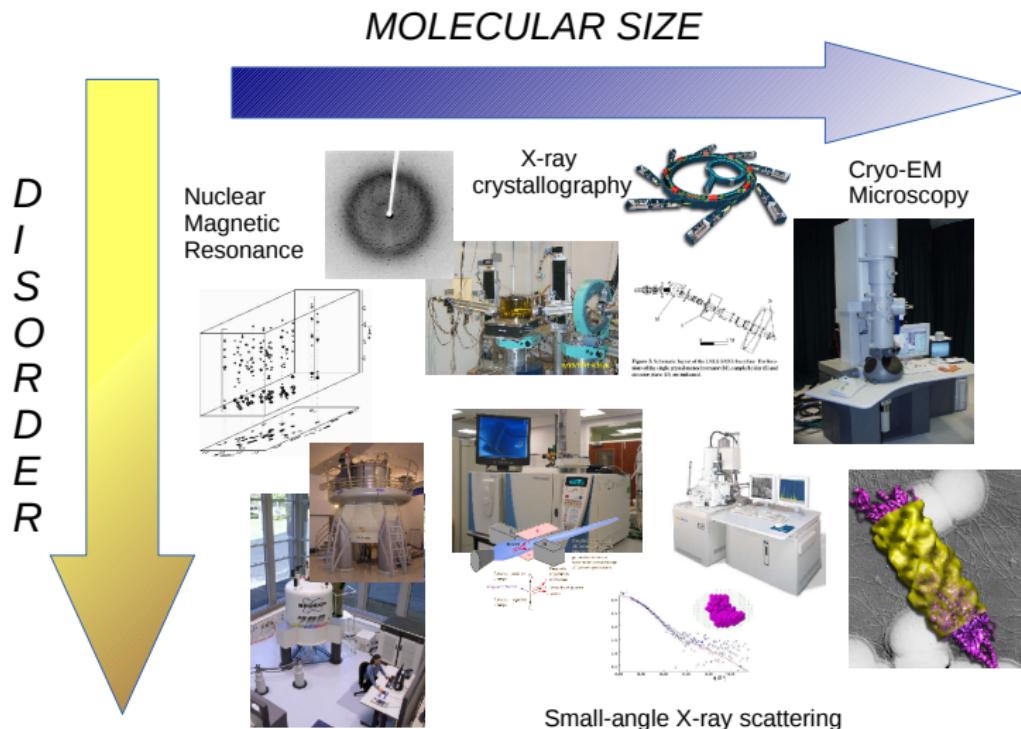
Thérèse E Malliavin

Unité de Bioinformatique Structurale
Institut Pasteur and UMR CNRS 3528
Paris, France

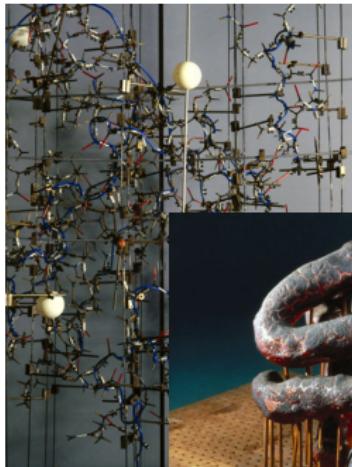
DIMACS Workshop on Distance Geometry: Theory and Applications
Rutgers University, 26-29 July 2016



Experimental techniques for structural biology



The infancy of structural biology



Model of pig insulin:
Dorothy Hodgkin, 1967
(Image credit: Science
Museum).

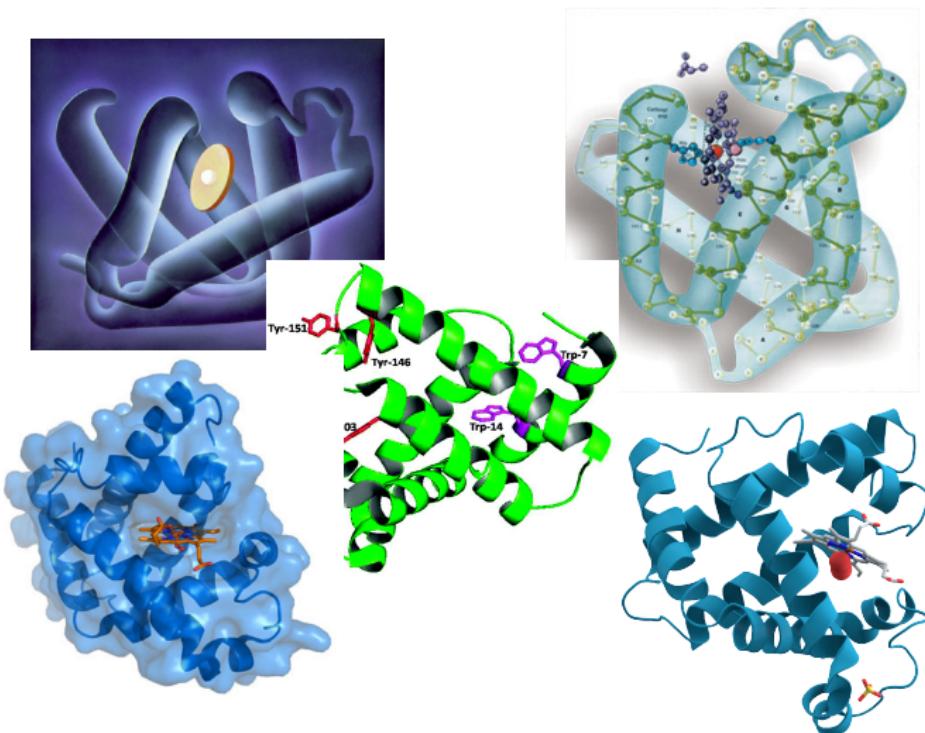


John Kendrew with the 'forest of rods'
model of myoglobin (Image credit: MRC
Laboratory of Molecular Biology)

Sausage model of myoglobin, John
Kendrew, 1957 (Image credit: Science
Museum).

kathryngamer.co.uk/blog

Structural bioinformatics



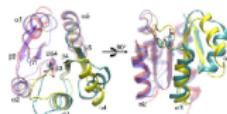
Low ordered or disordered biomolecular structure

« Unique »
conformation



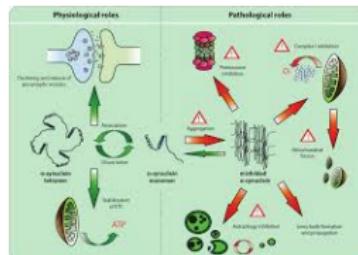
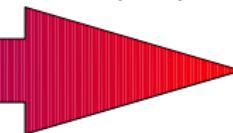
Conotoxin, 1IE
Sharp...Lewis
Nat Neurosc 2001

Conformational
exchange



nitrogen regulatory protein C (NtrC). Vanatta...Pande,
Nat Comm 2014

Intrinsically
Disordered
Proteins (IDP)



Bobela... Schneider, Biomolecules 2015

X-ray crystallography

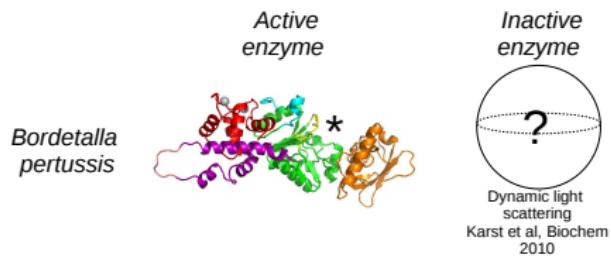
Nuclear Magnetic Resonance (solid-state, solution)

Small-angle X-ray scattering

Fluorescence resonance energy transfer

Exploration of AC conformational space

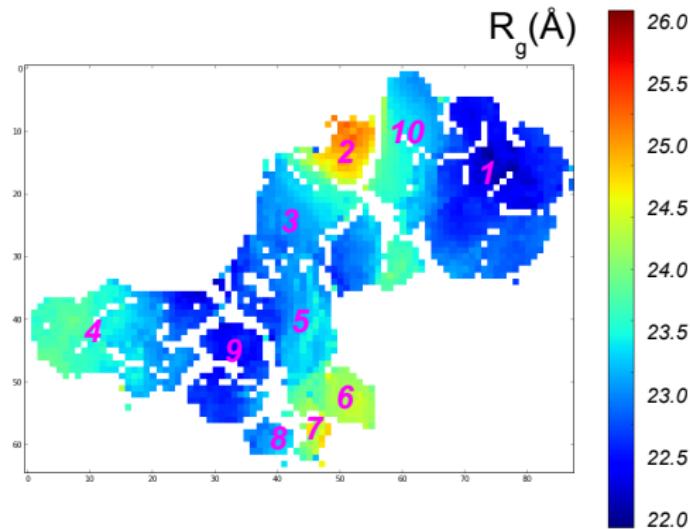
- AC inactive state
- Larger range of explored gyration radii



Cortes-Ciriano, Bouvier, Nilges, Maragliano, Malliavin. Temperature Accelerated Molecular Dynamics with Soft-Ratcheting Criterion Orients Enhanced Sampling by Low-Resolution Information. *J Chem Theory Comput* 2015.

Exploration of AC conformational space

- AC inactive state
- Larger range of explored gyration radii
- Clustered compact conformations

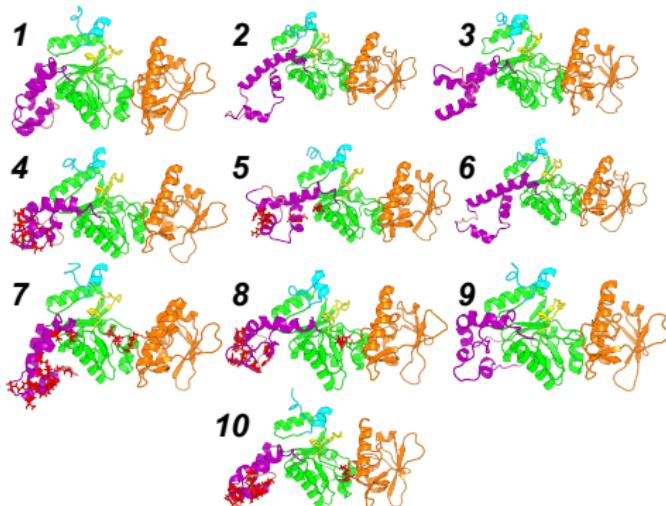


Cortes-Ciriano, Bouvier, Nilges, Maragliano, Malliavin. Temperature Accelerated Molecular Dynamics with Soft-Ratcheting Criterion

Orients Enhanced Sampling by Low-Resolution Information. J Chem Theory Comput 2015.

Exploration of AC conformational space

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Orients Enhanced Sampling by Low-Resolution Information. J Chem Theory Comput 2015.

Global optimisation

Global optimization is distinguished from regular optimization by its focus on **finding the maximum or minimum over all input values**, as opposed to finding local minima or maxima



Martin,

Zhou, Donald. Systematic solution to homo-ligomeric structures determined by NMR Proteins 2015.

Distance Geometry problem

- Problem
- Spheres intersection

At the beginning of this discussion, we will suppose that all distances in G are precise. In this case, the MDGP can be seen as the problem of finding a conformation $x = (x_1, x_2, \dots, x_n)$ such that all constraints:

$$\|x_u - x_v\| = d(u, v) \quad \forall (u, v) \in E \quad (16.1)$$

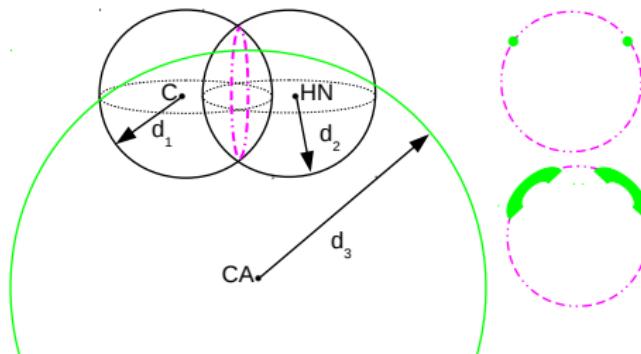
are satisfied. In the formula, $\|\cdot\|$ represents the computed distance between two atomic coordinates belonging to the conformation x , whereas $d(u, v)$ represents the known distance between the two atoms (the weight associated to the edge). The MDGP is a constraint satisfaction problem.

Malliavin, Mucherino, Nilges. Distance geometry in structural biology: new perspectives in: Distance Geometry: Theory, Methods and Applications, Mucherino, Lavor, Liberti, Maculan (Eds.), Springer 2013.

Distance Geometry problem

- Problem
- Spheres intersection
- Tree: branch and prune

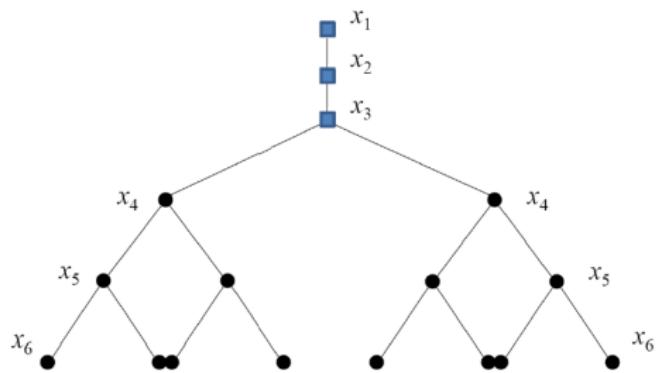
Search for the position of an atom X such that:
 $\text{dist}(X,C) = d_1$, $\text{dist}(X,HN) = d_2$, $\text{dist}(X,CA) = d_3$



Malliavin, Mucherino, Nilges. Distance geometry in structural biology: new perspectives in: Distance Geometry: Theory, Methods and Applications, Mucherino, Lavor, Liberti, Maculan (Eds.), Springer 2013.

Distance Geometry problem

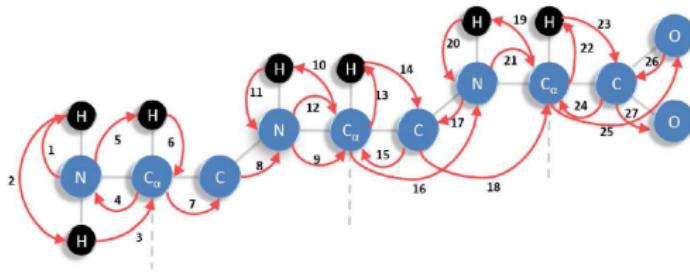
- Problem
- Spheres intersection
- Tree: branch and prune
- Atoms recursive ordering



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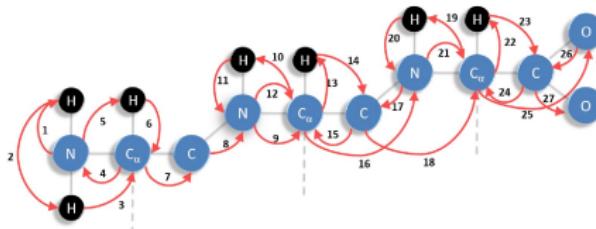
Distance Geometry problem

- Problem
- Spheres intersection
- Tree: branch and prune
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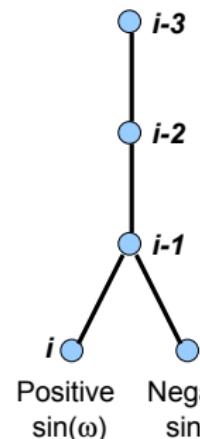
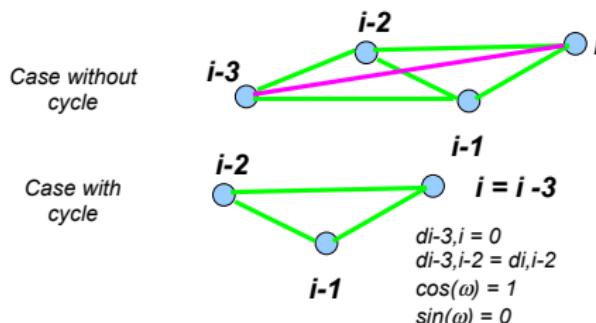


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Atom recursive ordering and branching distances

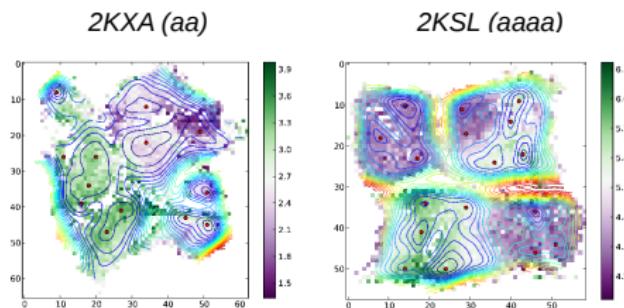
Atom ordering
and branching

- Distances corresponding to chemical bond, or to 2 chemical bonds connected by a bond angle
- Distances that can be exact or interval



Helical peptides with long-range distance restraints

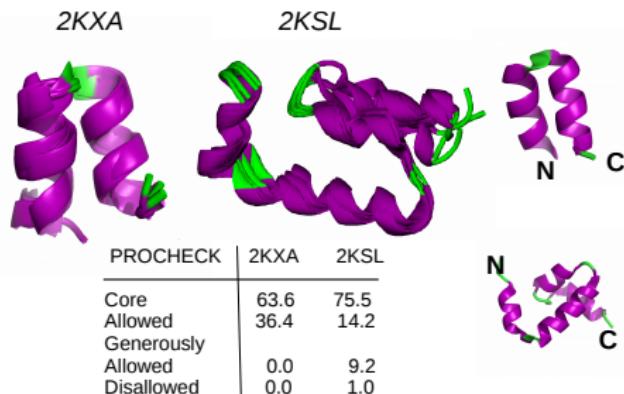
- Exploration of conformations using few long-range distance restraints
- Superposition to Protein Data Bank target structures



Cassioli, Bardiaux, Bouvier, Mucherino, Alves, Liberti, Nilges, Lavor C, Malliavin TE. BMC Bioinformatics 2015

Helical peptides with long-range distance restraints

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Cassioli, Bardiaux, Bouvier, Mucherino, Alves, Liberti, Nilges, Lavor C, Malliavin TE. BMC Bioinformatics 2015

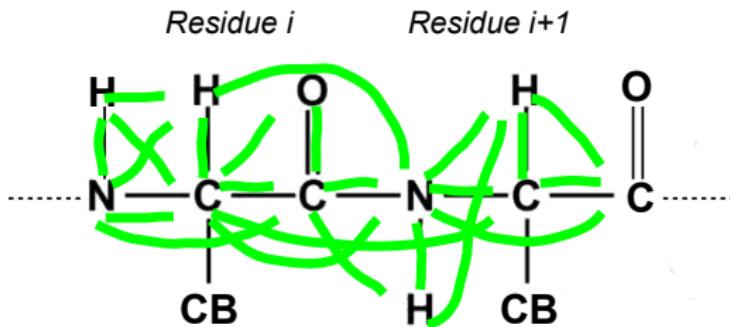
Validation set of proteins

PDB	Nres	SecStruct	EXP
1CEY	128	ababababab	NMR
2F05	85	aaaa	NMR
2KSL	51	aaaa	NMR
2KXA	24	aa	NMR
2LJ0	65	bbbbbb	NMR
2LVR	30	bba	NMR
2LXZ	32	bbb	NMR
2M5X	40	bbab	NMR
2MC6	73	bbba	NMR
2MDI	56	bbb	NMR
2MGV	65	abbb	NMR
2MH2	64	abaabb	NMR

PDB	Nres	SecStruct	EXP
2MJ6	90	aabbba	NMR
2MLA	37	babb	NMR
2MNI	92	baabba	NMR
2MP1	77	bbba	NMR
2MW9	33	bbb	NMR
2MXE	47	bbaab	NMR
2N17	56	bbab	NMR
2N2Q	54	babb	NMR
2RUP	58	bbb	NMR
4BYA	75	aaaa	NMR
4OU0	66	abaabb	XR
4RBX	32	bbb	XR

Calculations using exact distances and intervals, determined from a limited informative set of restraints.

Short-range exact distance are used



Exact branching distances

Exact pruning distances: involved residues

$$p = 5,4: (i,i) (i,i+1)$$

$$p = 6,4: (i,i) (i,i+1)$$

$$p = 7,4: (i,i) (i,i+1)$$

$$p = 8,4: (i,i) (i,i+1) (i,i+2)$$

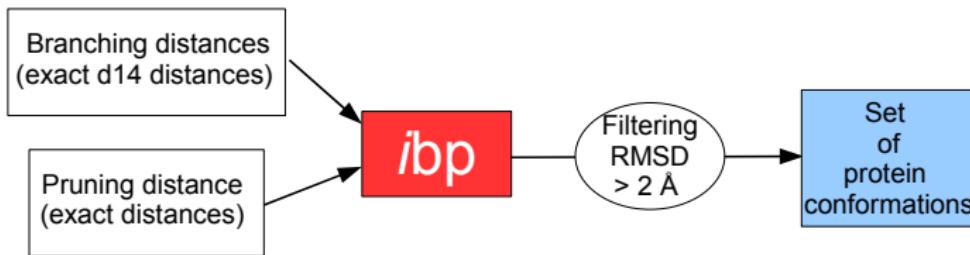
$$p = 9: (i,i+1)$$

$$p = 10: (i,i+1) (i,i+2)$$

$$p = 11: (i,i+1) (i,i+2)$$

$$p = 12: (i,i+1) (i,i+2)$$

Calculation scheme for exact distances



Found: One conformation found by iBP has an $\text{RMSD} < 2\text{\AA}$ w.r.t. the PDB structure.

Mirror found: One conformation found by iBP has an $\text{RMSD} < 2\text{\AA}$ w.r.t. the mirror image of the PDB structure.

Partially found: At least 50% of the structure of one conformation found by iBP has an $\text{RMSD} < 2\text{\AA}$ w.r.t. the PDB structure.

Not found: None of the previous cases.

Detection of PDB structure if five conformations are generated

Restraint types			i,i+1			i,i+1,i+2		i,i+1		i,i+1,i+2		
PDB	Nres	SecStruct	p=5,4	p=6,4	p=7,4	p=8,4	p=9	p=10	p=11	p=12		
1CEY	128	babababab	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2F05	85	aaaa	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2KSL	51	aaaa	blue	blue	blue	blue	blue	blue	blue	blue	blue	blue
2KXA	24	aa	blue	orange	orange	orange	blue	blue	blue	blue	blue	blue
2LJ0	65	bbbbbb	magenta	magenta	magenta	magenta	blue	blue	blue	blue	blue	blue
2LVR	30	bba	blue	blue	blue	blue	blue	blue	blue	blue	blue	blue
2LXZ	32	bbb	blue	blue	blue	blue	blue	blue	blue	blue	blue	blue
2M5X	40	bbab	orange	orange	orange	orange	orange	blue	blue	blue	blue	blue
2MC6	73	bbb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2MDI	56	bbb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2MGV	65	bbbbbb	magenta	magenta	magenta	magenta	magenta	magenta	magenta	magenta	magenta	magenta
2MH2	64	abaabb	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
2MJ6	90	aabb	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
2MLA	37	babb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2MN1	92	baabba	orange	orange	orange	orange	blue	blue	blue	blue	blue	red
2MP1	77	bbba	orange	orange	orange	blue	blue	blue	blue	blue	blue	blue
2MW9	33	bbb	orange	orange	orange	blue	blue	blue	blue	blue	blue	blue
2MXE	47	baaab	orange	orange	orange	orange	orange	blue	blue	blue	blue	blue
2N17	56	bbab	orange	orange	orange	orange	orange	blue	blue	blue	blue	blue
2N2Q	54	babb	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
2RUP	58	bbb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
4BYA	75	aaaa	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
4OU0	66	abaabb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
4RBX	32	bbb	blue	blue	blue	magenta	blue	blue	blue	blue	blue	blue

Not found Partially found Found Mirror found

Detection of PDB structure if *chirality* is switched off

Restraint types			i,i+1			i,i+1,i+2		i,i+1		i,i+1,i+2		
PDB	Nres	SecStruct	p=5,4	p=6,4	p=7,4	p=8,4	p=9	p=10	p=11	p=12		
1CEY	128	ababababab										
2F05	85	aaaa										
2KSL	51	aaaa										
2KXA	24	aa										
2LJ0	65	bbbbbb										
2LVR	30	bba										
2LXZ	32	bbb										
2M5X	40	bbab										
2MC6	73	bbb										
2MDI	56	bbb										
2MGV	65	bbbbbb										
2MH2	64	abaabb										
2MJ6	90	aabbba										
2MLA	37	babb										
2MN1	92	baabba										
2MP1	77	bbba										
2MW9	33	bbb										
2MXE	47	bbaab										
2N17	56	bbab										
2N2Q	54	babb										
2RUP	58	bbb										
4BYA	75	aaaa										
4OU0	66	abaabb										
4RBX	32	bbb										

Not found Partially found Found Mirror found

Detection of PDB structure if five conformations are generated

Restraint types			i,i+1			i,i+1,i+2		i,i+1		i,i+1,i+2		
PDB	Nres	SecStruct	p=5,4	p=6,4	p=7,4	p=8,4	p=9	p=10	p=11	p=12		
1CEY	128	babababab	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2F05	85	aaaa	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2KSL	51	aaaa	blue	blue	blue	blue	blue	blue	blue	blue	blue	blue
2KXA	24	aa	blue	orange	orange	orange	blue	blue	blue	blue	blue	blue
2LJ0	65	bbbbbb	magenta	magenta	magenta	magenta	blue	blue	blue	blue	blue	blue
2LVR	30	bba	blue	blue	blue	blue	blue	blue	blue	blue	blue	blue
2LXZ	32	bbb	blue	blue	blue	blue	blue	blue	blue	blue	blue	blue
2M5X	40	bbab	orange	orange	orange	orange	orange	blue	blue	blue	blue	blue
2MC6	73	bbb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2MDI	56	bbb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2MGV	65	bbbbbb	magenta	magenta	magenta	magenta	magenta	magenta	magenta	magenta	magenta	magenta
2MH2	64	abaabb	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
2MJ6	90	aabb	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
2MLA	37	babb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
2MN1	92	baabba	orange	orange	orange	orange	blue	blue	blue	blue	blue	red
2MP1	77	bbba	orange	orange	orange	blue	blue	blue	blue	blue	blue	blue
2MW9	33	bbb	orange	orange	orange	blue	blue	blue	blue	blue	blue	blue
2MXE	47	baaab	orange	orange	orange	orange	orange	blue	blue	blue	blue	blue
2N17	56	bbab	orange	orange	orange	orange	orange	blue	blue	blue	blue	blue
2N2Q	54	babb	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
2RUP	58	bbb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
4BYA	75	aaaa	magenta	magenta	magenta	magenta	orange	blue	blue	blue	blue	blue
4OU0	66	abaabb	orange	orange	orange	orange	blue	blue	blue	blue	blue	blue
4RBX	32	bbb	blue	blue	blue	magenta	blue	blue	blue	blue	blue	blue

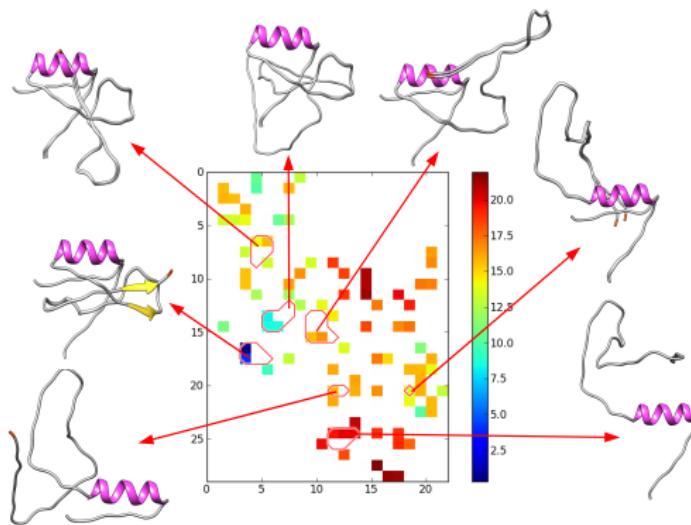
Not found Partially found Found Mirror found

Conformational exploration for short-range restraints

PDB	nbres	SecStruct	rank	RMSD (Å)	Number of saved conformations	Number of parsed leaves	CPU
2F05	85	aaaa	5.37×10^3	0.19	3.75×10^7	5.36×10^8	3d20h
2M5X	40	bbab	1.66×10^3	0.08	4.09×10^3	1.63×10^5	10s
2MGV	65	abbb	5.07×10^2	0.09	5.12×10^2	1.63×10^5	19s
2MXE	47	bbaab	1.92×10^3	0.11	2.04×10^3	3.27×10^3	30s
2N17	56	bbab	2.04×10^5	0.17	10^6	$> 9 \times 10^6$	6d5h
2N2Q	54	babb	1.77×10^3	0.42	1.79×10^3	2.68×10^8	1d19h
2RUP	58	bbb	22	0.09	64	64	9s
4BYA	75	aaaa	9.99×10^3	0.19	10^4	$> 8 \times 10^5$	90s
4OU0	66	abaabb	1.10×10^5	0.12	10^6	$> 1 \times 10^7$	21mn

Pruning distances p=8,4: (i,i) (i,i+1) (i,i+2)

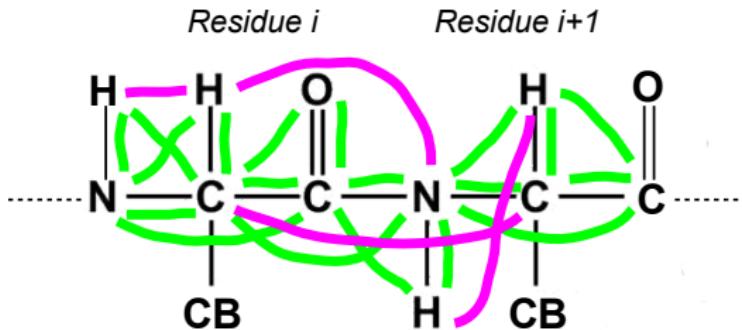
One example of exploration



Bouvier, Desdouits, Ferber, Blondel, Nilges. Bioinformatics 2015

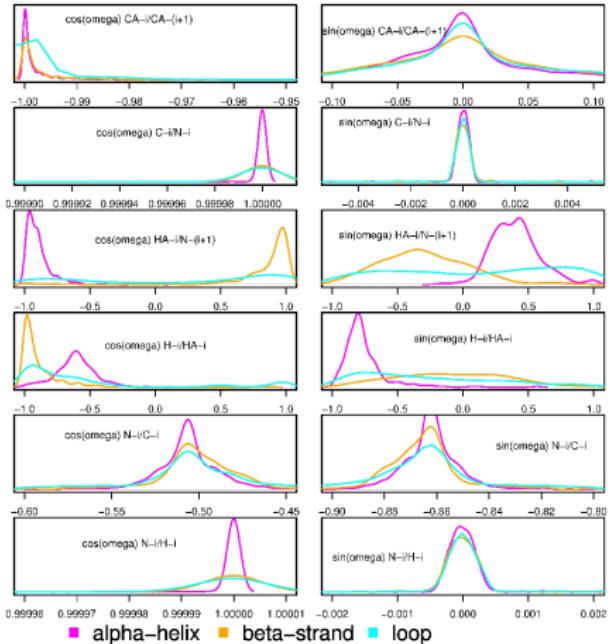
Bouvier, Duclert-Savatier, Desdouits, Meziane-Cherif, Blondel, Courvalin, Nilges, Malliauvin. JCIM 2014

Which distance intervals?

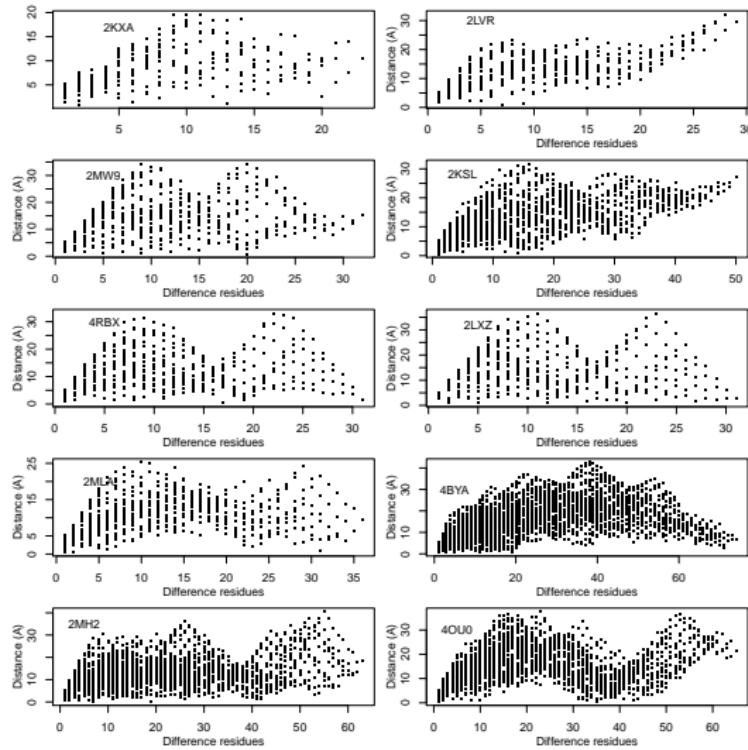


- Exact branching distances due to bond and bond angle geometry
- Interval branching distances
 $H-i/HA-i$, $HA-i/N-(i+1)$, $CA-i/CA-(i+1)$
- Interval pruning distances between C_α atoms

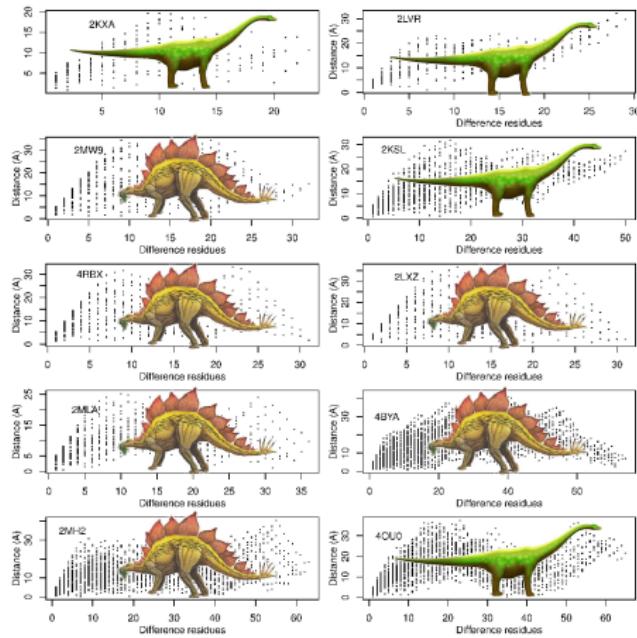
Strict branching intervals obtained using ω distributions in secondary structure elements

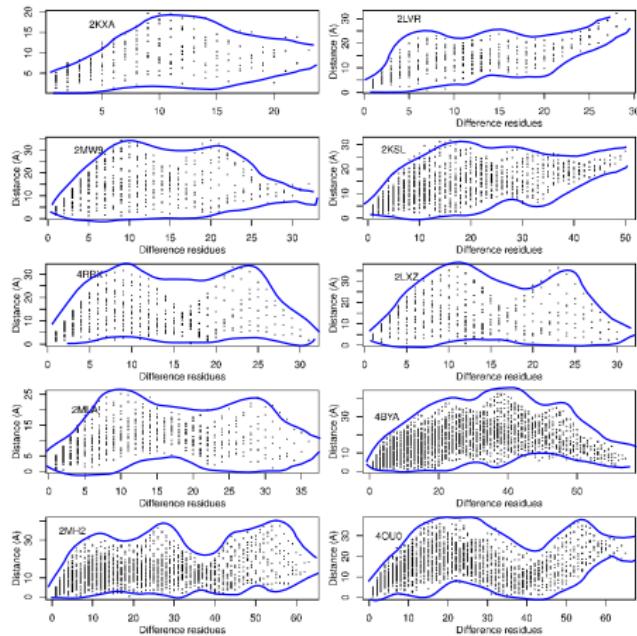


	$\cos(\omega)$	$\sin(\omega)$
HA-i/N-(i+1)	H [-1,-0.9]	+
HA-i/N-(i+1)	E [0.9,1]	+/-
HA-i/N-(i+1)	L [-1,1]	+/-
H-i/HA-i	H [-0.75,-0.4]	-
H-i/HA-i	E [-1,-0.9]	+/-
H-i/HA-i	L [-1,-0.9]	+/-
CA-i/CA-(i+1)	H [-1,-0.97]	+
CA-i/CA-(i+1)	E [-1,-0.97]	+
CA-i/CA-(i+1)	L [-1,-0.97]	+
N-i/C-i	H bond	-
N-i/C-i	E bond	-
N-i/C-i	L bond	-
N-i/H-i	H bond	+
N-i/H-i	E bond	+
N-i/H-i	L bond	+

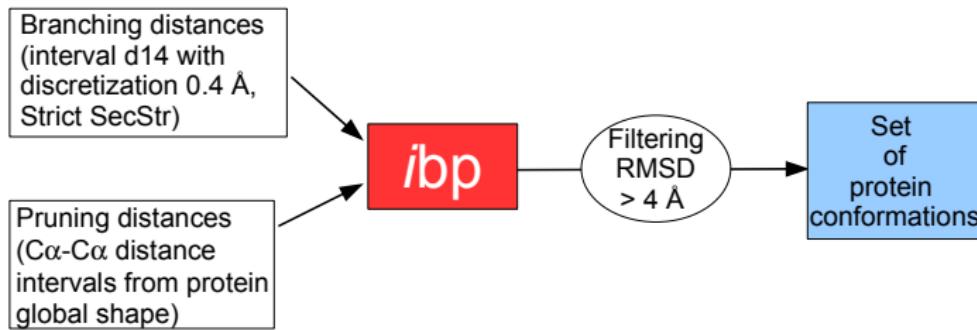
Distribution of distances between atoms Ca 

Distribution of distances between atoms $C\alpha$



Distribution of distances between atoms $C\alpha$ 

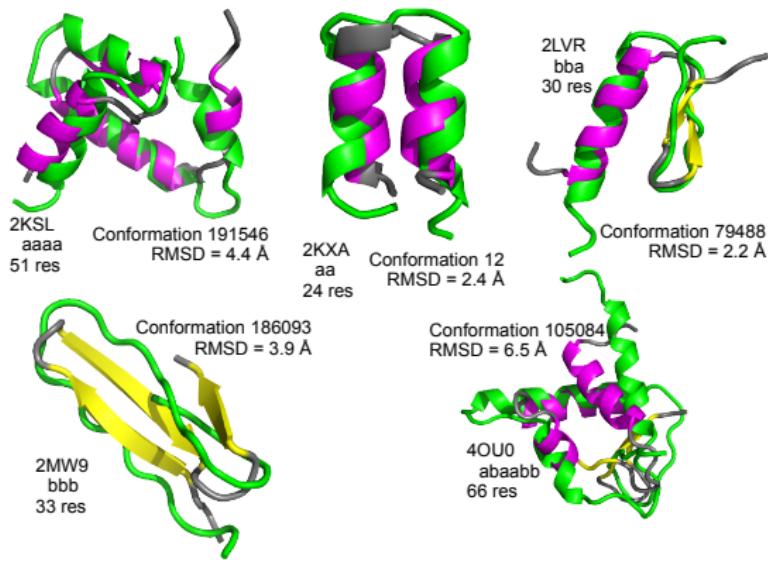
Calculation scheme for intervals



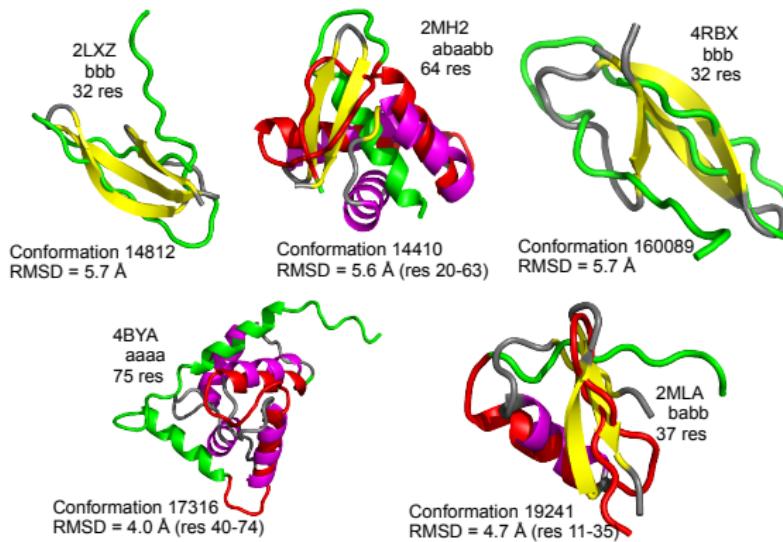
Conformational exploration for short-range restraints

PDB	nbres	SecStruct	rank	RMSD (Å)	Number of saved conformations	Number of parsed leaves	CPU
2KXA	24	aa	12	2.36	512	3.27×10^5	1 mn
2LVR	30	bba	7.95×10^4	2.23	200000	2.88×10^8	15h55mn
2MW9	33	bbb	1.86×10^5	3.93	200000	3.14×10^8	11h35mn
2KSL	51	aaaa	1.91×10^5	4.39	200000	8.49×10^7	16h20mn
4RBX	32	bbb	1.60×10^5	4.77	200000	1.84×10^9	4d15h40mn
2LXZ	32	bbb	1.48×10^4	5.69	200000	2.15×10^9	5d8hrs
2MLA	37	babb	1.92×10^4	5.33	200000	2.68×10^9	6d9h50mn
4OU0	66	abaabb	1.05×10^5	6.55	200000	1.64×10^9	6d14h20mn
2MH2	64	abaabb	1.44×10^4	8.48	200000	1.34×10^9	6d1h55mn
4BYA	75	aaaa	1.73×10^4	8.68	200000	1.05×10^7	8h18mn

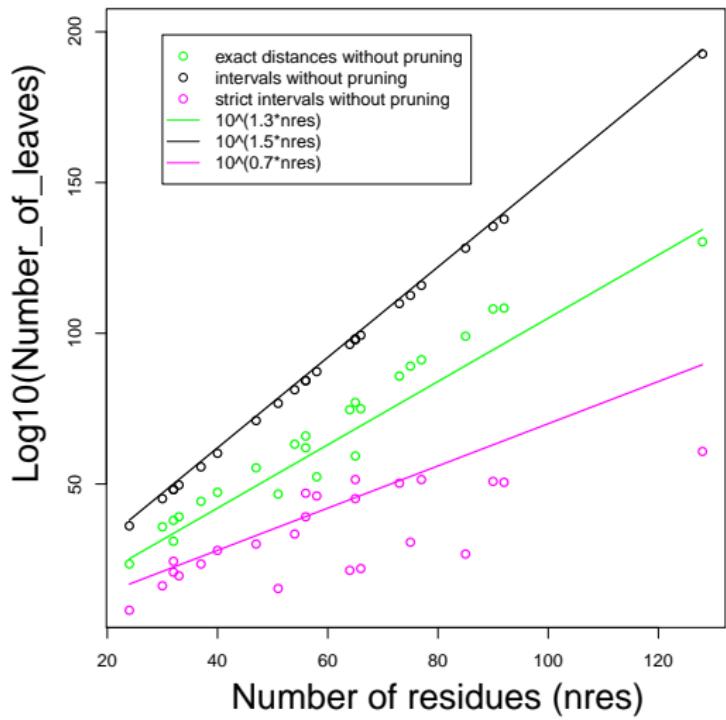
Some examples of calculations with intervals and pruning



Some examples of calculations with intervals and pruning

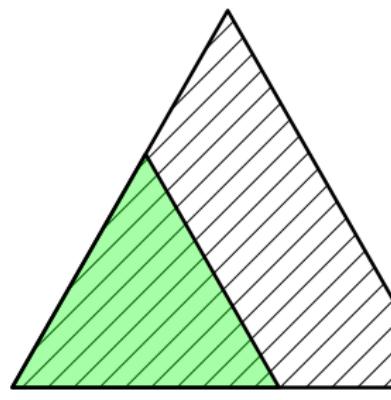


Problem complexity



discretization factor: 0.4 Å

Problem complexity



Number of parsed leaves
without pruning = N/NF

Reduction factor due to pruning:
 $F = ns/(N/NF)$

Predicted maximum number of
leaves with pruning = $F \cdot N$

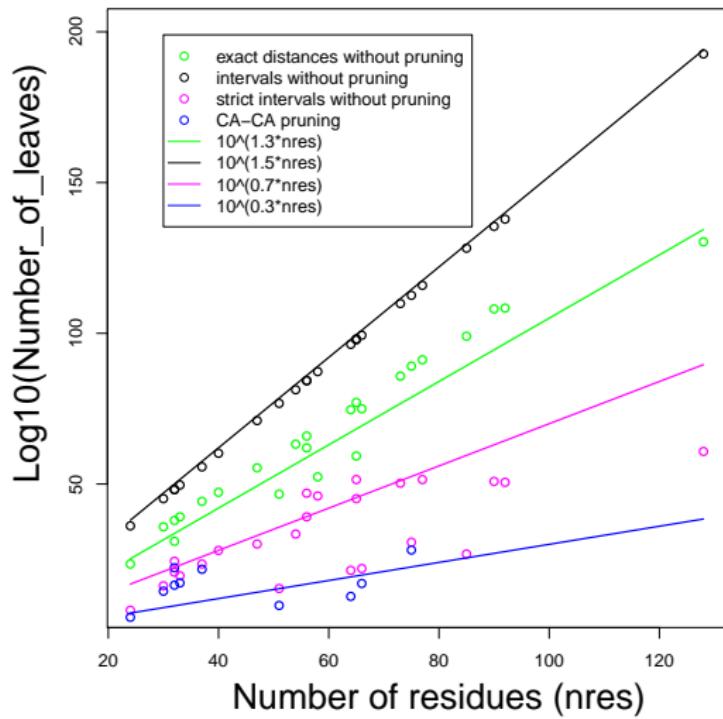
N = maximum number of
leaves without pruning

ns = number of parsed
leaves using pruning

NF = number of leaves to be
parsed without pruning

discretization factor: 0.4 Å

Problem complexity



discretization factor: 0.4 Å

Conclusions and perspectives

- *ibp* provides an algorithm designed for the systematic exploration of the configuration space of protein conformation
- *ibp* is efficient for the exploration of protein conformational space with limited sets of exact short-range inter-atomic distances
- the case of distance intervals could be addressed using strictly definition of secondary structure elements coupled to pruning based on global distance distributions

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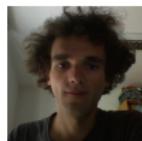
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